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PRECIPITATION EFFICIENCY
CONSTRAINT ON CLIMATE CHANGE

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18 **ABSTRACT**

19 Precipitation efficiency (PE) relates cloud condensation to precipitation and intrinsically binds
20 atmospheric circulation to the hydrological cycle. Due to PE's inherent microphysical
21 dependencies, definitions and estimates vary immensely. Consequently, PE's sensitivity to
22 greenhouse warming and implications for climate change are poorly understood. Here, we quantify
23 PE's role in climate change by defining a simple index ϵ as the ratio of surface precipitation to
24 condensed water path. This macroscopic metric is reconcilable with microphysical PE measures
25 and higher ϵ is associated with stronger mean Walker circulation. We further find that state-of-
26 the-art climate models disagree on the sign and magnitude of future ϵ changes. This sign
27 disagreement originates from models' convective parameterizations. Critically, models with
28 increasing ϵ under greenhouse warming, in line with cloud-resolving simulations, show greater
29 slowdown of the large-scale Hadley and Walker circulations and a two-fold greater increase in
30 extreme rainfall than models with decreasing ϵ .

31 Precipitation efficiency (PE) quantifies the fraction of condensed water in a cloud to reach the
32 surface as precipitation. In the tropics, precipitation is dominated by highly transient, spatially
33 restricted, deep convective events driving intense upwards mass fluxes that, in aggregate, compose
34 the ascending branches of the meridional Hadley and zonal Walker circulations. As an air parcel
35 rises within a cumulus cloud and some of the water vapor it contains condenses, it rains out a
36 fraction of its water content leaving the remaining condensate to interact with incoming and
37 outgoing radiation. Some of the precipitation evaporates as it falls back through the atmosphere,
38 which cools the air and directly drives local downward mass fluxes. A higher PE implies lower
39 evaporation of hydrometeors and greater net latent heat release by convective towers. Total cloud
40 condensation and re-evaporation of falling precipitation are both macrophysical manifestations of
41 inherently microphysical processes. PE can be applied to larger scales by considering a *cloud*
42 *ensemble* - the statistical average over multiple transient deep-convective updrafts and downdrafts
43 [1].

44 Environmental controls on PE can be combined into three groups: cloud microphysics,
45 entrainment and convection dynamics [2], but work to understand how these controls relate to
46 climate and anthropogenic influence is only now coming to the fore. A recent local-scale
47 observational study at Darwin, Australia found that PE increases with free-tropospheric humidity
48 and decreases with both surface temperature (T_s) and convective available potential energy [3]. In
49 contrast, limited domain cloud-resolving model (CRM) studies of radiative convective equilibrium
50 indicate that PE increases with T_s [4, 5]. Further, aerosol loading can also modulate PE in shallow
51 and deep clouds by modifying microphysical processes [6, 7].

52 Changes in PE are of significant interest because they could relate to a number of changes
53 at planetary and smaller scales in contemporary climate. Firstly, since PE controls the relationship

54 between upward and downward convective mass fluxes and aggregate convective mass fluxes
55 result in large-scale overturning, PE may provide insight into how the tropical circulation responds
56 to greenhouse gases [1]. Secondly, limited-domain cloud resolving modeling indicates that the
57 microphysical processes encapsulated by PE [4, 8] may be useful in understanding projections of
58 increases in precipitation extremes with warming [9]. Lastly, since higher PE results in less
59 detrainment of cloud condensate at high altitudes, PE has been hypothesized to play a role in cloud
60 feedback [10-14].

61 In a warmer atmosphere, it is unclear whether PE will decrease [3], remain constant [15,
62 16], or increase [4, 5, 17]. A theoretical constraint on PE based on an entraining plume model is
63 that PE should be greater than or equal to one minus relative humidity [18]. This is, however, only
64 a weak constraint for PE as updrafts are typically near saturation. With higher temperature and
65 more radiative cooling, precipitation increases and convective mass flux decreases [1]. This
66 implies an increase in the intensity of precipitation or increase in PE, but this expectation is
67 unconfirmed in observations and models alike. Global Climate Models (GCMs) predict a robust
68 increase of 2-3% in global precipitation per degree Celsius ($^{\circ}\text{C}$) of warming [19, 20]. Meanwhile,
69 cloud condensation is sensitive to a multitude of environmental conditions such as tropospheric
70 temperature, humidity, and stratification, and may increase [5] or decrease [21] with warming at
71 different altitudes. Thus, changes to PE – being the ratio of precipitation to condensation – are
72 equivocal.

73 The question of how PE will change with warming is challenging to address, due to the
74 wide diversity in PE definitions across studies using observations, CRMs, and GCMs (see [22] for
75 the latest review). Definitions of PE can be generally categorized into large-scale PE ϵ_{ls} and cloud
76 microphysical PE ϵ_m [23]. ϵ_{ls} , the ratio of surface precipitation P_s to the sub-cloud water vapor

77 convergence, has been widely used to study thunderstorms. ϵ_{ls} takes values ranging from 0.1 to
78 greater than 1 [24] depending on environmental factors, such as vertical wind shear, sub-cloud
79 humidity, and cloud base areal extent [25]. However, this measure of PE is limited to studying
80 individual convective events. When averaged over space and time, ϵ_{ls} is by definition equal to
81 unity since what goes up must come down. As ϵ_{ls} is sensitive to the spatial and temporal scales
82 considered [26], it is inappropriate for climatological PE analysis.

83 By contrast, ϵ_m – the ratio of P_s to the column-integrated condensation rate C – is typically
84 less than unity over various spatiotemporal scales owing to the evaporation of falling hydrometeors
85 before they reach the surface as precipitation. However, ϵ_m is difficult to directly observe due to
86 its inherent microphysical dependence. The typical range of ϵ_m averaged over a limited domain
87 CRM in radiative convective equilibrium is 0.2 to 0.5 [5, 27, 28], which is similar to that inferred
88 in observational studies of tropical convection [29], mid-latitude squall lines [30], and mid-latitude
89 cyclones [31]. The magnitude of ϵ_m is sensitive (up to 50% relative change) to the computational
90 implementation of condensate removal in the CRM [5], which occurs at multiple levels
91 simultaneously.

92 Given the inherent problems in using ϵ_{ls} and ϵ_m across different models and observations,
93 the goal of this paper is to introduce a simple physical measure of PE applicable across different
94 spatial scales to serve as a metric linking the macro and microphysical approaches. We will then
95 quantify the relation between PE and the mean climatological state in the tropics and investigate
96 the role of PE in climate change.

97

98 **DEFINING A PRECIPITATION EFFICIENCY MEASURE**

99 In this study, we define a PE measure as:

100
$$\epsilon = \frac{P_s}{CWP} [\text{units: } s^{-1}] \quad (1)$$

101 where CWP is the condensed water path, i.e., the column integrated cloud liquid and ice content.
 102 See *Methods* for a brief discussion of the uncertainties. Similar expressions have been used in
 103 previous studies for water vapor cycling [31] and warm clouds [17, 32]; ϵ differs from those in
 104 that it uses the total condensate budget. Since PE is a manifestation of microphysical processes, it
 105 is critically important that an index quantifying it can be linked to this microphysics. Limited
 106 domain CRM studies have been able to explicitly compute microphysical ϵ_m by outputting
 107 condensation rates at each vertical level [5]. However, this is not feasible in climatological
 108 observations of nature nor in GCMs. Therefore, we validate the use of ϵ as a measure of PE by
 109 running a set of CRM experiments (Methods) and computing both ϵ and ϵ_m . The macrophysical
 110 ϵ of Equation (1) is tightly correlated to the microphysical ϵ_m ($r = 0.86$; Extended Fig. 1 and
 111 Extended Fig. 2). The exclusive use of macrophysical variables in ϵ enables comparison between
 112 observations, CRMs, and GCMs.

113 Unlike the parameter ϵ_m , the present formulation for ϵ is dimensional. As such, it is a
 114 general measure or index of PE and not an efficiency defined as a fraction of unity. For brevity
 115 and given the tight correlation of ϵ with ϵ_m , we herein refer to the parameter ϵ as PE.

116 The ϵ metric could be calculated at various spatial and temporal resolutions. Within time-
 117 space aggregated values, the average is composed of a variety of cloud types, such as non-
 118 precipitating shallow clouds and mixed-phase clouds. Within each of these cloud types, PE will
 119 vary in correspondence with the relevant cloud physics. We use climatological ϵ to represent the
 120 net effect of these clouds within the tropical cloud ensemble.

121 The inverse $\epsilon^{-1} = \tau$ is a characteristic residence timescale for the total condensed cloud
 122 water across an ensemble of cloud types, or a characteristic drying timescale for the atmosphere if

123 condensation has stopped. Satellite-based observations indicate a tropical-mean τ of about 46
124 minutes (Fig. 1; [33]). This low τ value reflects the vigorous hydrological cycling of the
125 atmosphere, constantly requiring high rates of condensation to maintain the atmospheric stock of
126 CWP. In this timescale interpretation, precipitation is assumed to be a first-order process within
127 the CWP budget (*Methods*). This assumption holds well in satellite observations (Fig. S1) and, to
128 some degree, in GCMs. As such, we think of ϵ as an emergent diagnostic linked to the drying
129 timescale of the atmosphere. Its value is close to, but slightly different from the e-folding rate of
130 condensed water removal.

131 The spatial pattern of annual-mean observed ϵ is broadly correlated with regions of high
132 climatological precipitation (Fig. 1a). Regions of high ϵ ($> 0.8 \times 10^{-3} s^{-1}$) are tropical
133 convergence zones with intense time-mean precipitation, such as the Indo-Pacific warm pool (WP;
134 20S–20N, 80E–170E). Low ϵ ($< 0.2 \times 10^{-3} s^{-1}$) is found in subsidence regions such as the
135 Eastern Pacific (EP; 20S–20N, 140W–80W) and Atlantic subtropics. Local ϵ can be large due to
136 small CWP, such as on the coast of the Arabian Peninsula, but these arid regions have little
137 climatological precipitation and ϵ is thus not a suitable index there. Over the WP, ϵ increases
138 spatially with T_s . Deep convection preferentially occurs over warm SSTs and this favors stronger
139 updrafts and more precipitation. From 26 to 29°C, ϵ doubles from $0.4 \times 10^{-3} s^{-1}$ to 0.8
140 $\times 10^{-3} s^{-1}$, halving the residence time (Fig. 1b). With reduced residence time, microphysical
141 processes such as re-evaporation of raindrops and entrainment of dry and less buoyant air are less
142 effective at reducing the flux of hydrometeors reaching the surface. This corresponds to weaker
143 downdrafts and greater net latent heat release by convective updrafts.

144 The observed interannual standard deviation of tropical ϵ is 2.8%. The 2002–2020 period
145 of these available observations includes the global warming hiatus [34], hindering the monitoring

146 of the temperature sensitivity of ϵ . Regional magnitudes of ϵ are sensitive to T_s , which is
147 dominated by the inter-annual variability of sea surface temperatures (SSTs) in the Pacific Ocean
148 (Fig. 2). During El Nino, when the EP warms due to suppressed ocean upwelling, the zonal SST
149 gradient is reduced. The atmosphere responds with more frequent deep convection, resulting in
150 more cloudiness and higher P_s in the central and eastern Pacific. This is corroborated by a positive
151 correlation ($r = 0.60$) between the Nino3.4 SST index and EP-mean ϵ , and a negative correlation
152 between the Nino3.4 index and ϵ averaged over the WP, ϵ_{WP} ($r = -0.74$; Extended Fig. 3).
153 During El Nino, ϵ_{WP} is lower and ϵ averaged over the EP is higher (Fig. 2). The regionally
154 different responses of ϵ to underlying SST, combined with the ENSO correlations, reveal the
155 significance of non-local dynamics on local PE.

156

157 **LINKING PE TO THE TROPICAL MEAN-STATE**

158 We find significant negative temporal correlations between the observed monthly Outgoing
159 Longwave Radiation (OLR) and ϵ_{WP} (Fig. 3a). The local OLR vs. ϵ_{WP} correlations are
160 particularly strong over the WP and equatorial South America, associating high PE with deep
161 convection of higher intensity or frequency. The sign of the observed convection-PE relationship
162 in the WP is captured by the ERA5 reanalysis and the majority of CMIP6 models (Fig. S2).
163 Consistent with these correlations, over the past two decades, there was an intensification of WP
164 precipitation [35] coinciding with trends of increased occurrence frequency of deep anvil clouds
165 [36].

166 The correlations between OLR and ϵ_{WP} in Fig. 3a display a similar spatial pattern to the
167 mean-state Walker circulation. This is seen in negative correlations in the dominant ascending
168 branches over the WP and northern South America and positive correlations in descending

169 branches over the subtropical eastern Pacific and equatorial Atlantic. The strength of the Pacific
170 Walker circulation, measured by the mean sea level pressure difference ($dSLP$) between the
171 western and eastern equatorial Pacific (*Methods*), is robustly correlated with ϵ_{WP} across CMIP6
172 models ($r = 0.63$; Fig. 3b). High PE implies a greater rate of net latent heat release by precipitation
173 per convective cloud. Concurrently, a stronger Walker circulation is sustained, with stronger
174 ascending motion in the WP. Although observationally-based ERA5 data also exhibits a positive
175 correlation between ϵ and Walker Circulation strength of similar magnitude (not shown), this
176 relationship is complicated by strong El Niño impacts on ϵ .

177

178 **CHANGES IN ϵ WITH GREENHOUSE WARMING**

179 During periods covered by satellite observations (2002-2020) and reanalysis (1979-2021) tropical
180 mean temperature variability is constrained to within 0.5 °C. These records are unfortunately
181 therefore limited guides to the sensitivity of ϵ to T_s , $\partial\epsilon/\partial T_s$. By contrast, the CMIP6 ensemble
182 explores tropical temperature increases up to 4 °C in a large number of individual models (Fig. 4).
183 We find very large dispersion between CMIP6 models in the slope of $\partial\epsilon/\partial T_s$. After 2 °C of
184 warming, the ensemble mean PE response is 2.5%, with an intra-model range of -7% to +12%.
185 This range reflects relative changes in both P_s and CWP (Extended Fig. 4). Intra-model diversity
186 in the representation of convection is a likely cause of this wide range in ϵ sensitivity. Given this,
187 we use a limited domain cloud resolving model SAM (*Methods*) in which convection is explicitly
188 resolved to explore the range of tropical temperatures found in the CMIP6 SSP5-8.5 simulations
189 of twenty-first century anthropogenic warming. In these SAM simulations, ϵ increases with
190 temperature (Fig. 4), consistent with a previous study [5] that used the same model but studied a
191 microphysical measure of PE.

192 While the relationship between convective aggregation and warming remains an unsettled
193 research question [37], convective aggregation prefers warmer SSTs and is associated with high
194 PE [38]. Within aggregated convection, precipitation falls through columns of high humidity air,
195 resulting in less evaporation and implying higher PE [39]. On the other hand, the abundance of
196 clear-sky regions in aggregated convection favors the presence of boundary layer clouds which
197 typically re-evaporate with near zero PE [5]. We investigate these competing effects upon cloud
198 ensemble PE by running two sets of SAM simulations – a large domain (1024 by 1024 km², SAM-
199 L) and a small domain (512 by 512 km², SAM-S). Self-aggregation of convection is known to be
200 inhibited in smaller domain sizes [37] and indeed the principal difference between SAM-L and
201 SAM-S is that convection is aggregated in the former and disaggregated in the latter (Extended
202 Fig. 5). In the absence of self-aggregation, ϵ increases with T_s at a rate of 2% per °C. When
203 convection is aggregated, $\partial\epsilon/\partial T_s$ increases to a rate of 5% per °C. This suggests that the impact
204 of reduced evaporation of rainfall (raising cloud ensemble PE) dominates over the impact of more
205 prevalent low clouds (lowering cloud ensemble PE). While the sign of these CRM-estimated
206 $\partial\epsilon/\partial T_s$ are positive, consistent with [5], its magnitude may depend on precipitation microphysics
207 in the CRM, requiring future work.

208 Generally, there exists two groups of GCMs in Fig. 4, divided cleanly on the sign of their
209 sensitivity of ϵ to T_s : (1) models in which ϵ increases with T_s and (2) models in which ϵ decreases
210 with T_s . We find that this disagreement can be traced to whether or not precipitation is represented
211 as dependent (e.g. [40]) or independent (e.g. [41]) of ascending mass flux in a convective grid cell
212 within these GCM's convective parameterizations (see Supplementary Table 1). The mass-flux
213 dependence of convective precipitation allows higher ϵ when the environmental conditions favor
214 strong vertical ascent. This dependence is absent in GCMs with convective precipitation

215 proportional to cloud water only, which collectively show weak or negative sensitivity of ϵ to T_s .
216 The response of ϵ to warming in models that possess this mass-flux dependence is similar in
217 magnitude and slope to those predicted by CRM simulations. The magnitude of mean-state ϵ in
218 some models can be different up to a factor of 2-3 compared to observations and CRMs, which
219 should be noted and requires future work (Fig. S3). Thus, a longer record of ϵ is required to
220 confirm the positive $\partial\epsilon/\partial T_s$ relationship predicted by the CRM and the CMIP6 GCMs with
221 updraft dependent precipitation parameterizations.

222

223 **IMPLICATIONS FOR FUTURE CLIMATE**

224 Next, we investigate the role of precipitation efficiency in climate change, focusing on
225 several key interwoven questions: *What role does PE play in controlling the response of large-*
226 *scale atmospheric circulation, temperature distribution and precipitation extremes to greenhouse*
227 *warming? Does the sign of $\partial\epsilon/\partial T_s$ across CMIP6 models affect climate change projections?*

228 The tropical circulation is expected to weaken under anthropogenic climate change from
229 both dynamic [42] and thermodynamic [43] perspectives. GCMs generally predict the Hadley cells
230 will widen and weaken in the twenty-first century [44]. The Southern Hemisphere cell's response
231 is expected to be dominated by widening, while the Northern Hemisphere cell is predicted mostly
232 to weaken [45], consistent with the changes shown in Fig. 5. The predicted magnitudes of Northern
233 Hemisphere Hadley cell weakening are highly variable between models in CMIP5 [44] and CMIP6
234 (this lack of consensus is visualized as the absence of shading between 5–30°N in Extended Fig.
235 6). This range in predictions is not well understood [45]. We find here that much of this intra-
236 model disagreement in projected Northern Hemisphere Hadley cell slowdown (Extended Fig. 6)
237 is directly aligned with differences in the warming response of PE (Fig. 5b).

238 Binning GCMs into two groups based on the sign of $\partial\epsilon/\partial T_s$, we find that models with
239 positive $\partial\epsilon/\partial T_s$ exhibit stronger warming responses (Fig. 5a) and amplified reductions of the
240 zonal-mean mass streamfunction ψ under greenhouse warming (Fig. 5b). Robust weakening
241 signals are present in the Hadley Circulation northern and southern branches, indicated by the
242 opposite sign of present-day ψ and its warming response $\Delta\psi$. Regional differences in $\Delta\psi$ can be
243 as large as 30%. These results suggest that, all else being equal, models with positive $\partial\epsilon/\partial T_s$
244 possess efficient deep convective towers that collectively release more net latent heat (or
245 equivalently, have less evaporative cooling). On the other hand, deep convective towers become
246 less efficient in models with negative $\partial\epsilon/\partial T_s$, requiring a stronger circulation to sustain more
247 latent heating. This argument conforms to the mass flux view [43] of tropical circulation slowdown
248 Fig. S4). Considering the difference in the maximum overturning as a measure of Hadley cell
249 intensity, positive $\partial\epsilon/\partial T_s$ corresponds to 4.5% more weakening of the northern cell compared to
250 negative $\partial\epsilon/\partial T_s$ (Fig. 6). This difference in Hadley circulation weakening north of the equator,
251 reduced when normalized by temperature (Extended Fig. 7), is strongly coupled to the overall
252 planetary temperature response. Weakening of the southern cell is less pronounced in CMIP6 [45]
253 and hence the differences between model groups are not statistically significant.

254 The Pacific Walker circulation also exhibits relative changes different between the two
255 model groups. Measured by the subsiding pressure velocity in the eastern equatorial Pacific
256 (*Methods*), the Walker circulation weakens by 30% in positive $\partial\epsilon/\partial T_s$ models compared to 16%
257 in negative $\partial\epsilon/\partial T_s$ models, (Fig. 6). Thus, the demonstrated link between future changes in ϵ and
258 the large-scale circulation suggests that the assumption of constant PE in changing tropical
259 circulations is inadequate. After normalizing by temperature (Extended Fig. 7), these differences

260 are less pronounced but remain statistically significant, suggesting both dynamic and
261 thermodynamic contributions to the Pacific Walker cell response.

262 We also find that the expected increase in extreme precipitation under climate change [46],
263 measured as the 99.9th percentile of daily-mean precipitation ($P_{99.9}$), is more than twice as strong
264 in positive $\partial\epsilon/\partial T_s$ models than in negative $\partial\epsilon/\partial T_s$ models. Specifically, global $P_{99.9}$ increases
265 19.5% in positive $\partial\epsilon/\partial T_s$ models, versus only 9.4% in negative $\partial\epsilon/\partial T_s$ models. These differences
266 remain statistically significant after normalizing $P_{99.9}$ by effective climate sensitivity (Extended
267 Fig. 7). This implies that the CMIP6 ensemble estimate of precipitation extreme increase could
268 underestimate the true value by over a third, in line with the results of [47]. This result quantifies
269 the microphysical contribution to hydrological cycle sensitivity, generally divided only into
270 dynamic and thermodynamic contributions.

271 Aerosol and indirect greenhouse gas effects can add higher order complexity to the
272 temperature related effects on ϵ discussed in the present study. This can be further explored in
273 existing model intercomparison projects such as Ref [48], an avenue for future work.

274 In summary, we have defined and explored the observed climatology of the PE index, ϵ ,
275 its temporal variation and link to the large-scale tropical circulation and precipitation extremes.
276 We find that the CMIP6 GCMs that have precipitation represented as independent of vertical mass
277 flux in their deep convection parameterization schemes all simulate decreasing ϵ with warming.
278 This opposes predictions by CRM simulations of projected twenty-first century tropical surface
279 temperatures. GCMs that predict positive $\partial\epsilon/\partial T_s$ show robust additional weakening of the Hadley
280 and Walker circulations, amplified atmospheric warming, and higher sensitivity of extreme
281 precipitation events. Consequently, constraining the sensitivity of ϵ to temperature is critical for
282 quantifying the climate response to anthropogenic forcing.

283

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294 **AUTHOR CONTRIBUTIONS STATEMENT**

295 RL and JS conceived the study, performed data analysis, data visualization. RL wrote the

296 original draft and all authors contributed to reviewing and editing the manuscript.

297 **COMPETING INTERESTS STATEMENT**

298 The authors declare no competing interests.

299 **FIGURE CAPTIONS**

300 **Fig. 1. Climatology and correspondence of precipitation efficiency index ϵ with temperature.**

301 (a) Spatial distributions of annual-mean ϵ in units $10^{-3}s^{-1}$ estimated from satellite observations.

302 Green contours outline regions with 6 mm per day or more surface precipitation in the annual

303 mean. (b) Annual-mean ϵ scattered against surface temperature T_s within the broad Indo-Pacific

304 warm pool region (defined as the left box in panel a). Satellite observations are derived from

305 MODIS and TRMM (see Methods) spanning July 2002 to September 2019.

306 **Fig. 2. Time evolution of ϵ .** Observed ϵ and T_s averaged over the entire tropics (30°S–30°N; solid
307 red and blue lines), the Indo-Pacific warm pool (20°S–20°N, 80°E–170°E; dashed lines), and the
308 Eastern Pacific (20°S–20°N, 140°W–80°W; dotted lines). 12-month smoothing is applied to
309 remove the annual cycle. Note several El Niño events, including in 2006, 2009 and 2015.

310

311 **Fig. 3. Precipitation efficiency ϵ and the large-scale tropical circulation.** (a) Temporal
312 correlation coefficients between outgoing longwave radiation (OLR) and annual-mean ϵ_{WP} in
313 satellite observations, with hatching where the p -value for the correlation is lower than 0.05. (b)
314 The strength of the Pacific Walker circulation versus ϵ_{WP} in 44 CMIP6 models, a reanalysis
315 (ERA5), and satellite observations. The line represents a linear regression over all blue points. ϵ_{WP}
316 denotes the spatial average of ϵ over the Indo-Pacific Warm Pool (Box in panel a). Here, east-west
317 sea level pressure difference along the equator, $dSLP$, is used as a measure of the Walker
318 circulation (Methods).

319

320 **Fig. 4. Sensitivity of ϵ to surface temperature.** Changes in precipitation efficiency index ϵ with
321 surface temperature T_s in observations (black squares), ERA5 reanalysis (grey squares), CRMs
322 (diamonds), and 30 CMIP6 GCMs with 22 mass-flux dependent models (Group 1; solid color lines)
323 and 8 mass-flux independent models (Group 2; dashed color lines) in their parameterizations of
324 deep convective precipitation (See Methods). Multi-model mean slopes are estimated by
325 regressing ϵ onto T_s , then taking the average, for Group 1 (solid black line), Group 2 (dashed black
326 line), and all models (dotted black line). Both ϵ and T_s are annual-means and averaged spatially
327 over the entire Tropics (30°S–30°N), with the exception of SAM-S (blue diamonds) and SAM-L
328 (red diamonds), which are 15-day and computational domain averages. 10-year smoothing is
329 applied to improve clarity.

330

331 **Fig. 5. Impact of ϵ on Changes in Temperature and Atmospheric Meridional Circulation**

332 **under Greenhouse Warming.** Difference in the anthropogenic response (defined here as the

333 2085-2100 average minus the 2015-2030 average in the SSP5-8.5 warming scenario) of (a) zonal-

334 mean temperature (ΔT) and (b) mass streamfunction ($\Delta\psi$; colors) between two groups of CMIP6

335 GCMs: models with positive $\partial\epsilon/\partial T_s$ (22 models) minus those with negative $\partial\epsilon/\partial T_s$ (8 models)

336 as displayed in Fig. 4. The multi-model-mean zonal-mean circulation averaged from 2015 to 2030

337 is shown in solid (positive and counter-clockwise) and dotted (negative and clockwise) contours.

338 Hatching represents p -values less than 0.1 using Student's t -test. Note the greater atmospheric

339 warming and more pronounced weakening of the northern Hadley cell for the models with positive

340 $\partial\epsilon/\partial T_s$.

341

342 **Fig. 6. Role of ϵ in Climate Change.** The response to greenhouse warming of the northern (ψ_{max}^N)
343 and southern branches (ψ_{max}^S) of the Hadley circulation, the Pacific Walker circulation (ω_{EP}), and
344 extreme precipitation (global 99.9th percentile daily precipitation, $P_{99,9}$) averaged among two
345 groups of CMIP6 models with positive $\partial\epsilon/\partial T_s$ (red) and negative $\partial\epsilon/\partial T_s$ (blue) under the
346 SSP585 scenario. Maximum zonal-mean streamfunction ψ and eastern equatorial Pacific pressure
347 velocity ω are used as measures of the Hadley and Walker circulations, respectively (*Methods*).
348 Changes are defined as years 2085-2100 minus years 2015-2030. Error bars show multi-model
349 spread. Differences in ψ_{max}^N , ω_{EP} and $P_{99,9}$ have p -values less than 0.05 using Student's t -test.
350 Models with increasing ϵ under greenhouse warming show greater large-scale atmospheric
351 circulation slowdown and a greater increase in extreme rainfall than models with decreasing ϵ .

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497

498 **METHODS**

499 *ϵ and the e-folding timescale of condensed water removal*

500 In a static atmosphere, assuming no sources and allowing complete dry out, condensate removal
501 can conceptually be represented by the power law relationship

502
$$\frac{d}{dt}(CWP) = \alpha(CWP)^\zeta, \quad (2)$$

503 for a power ζ and inverse timescale α . α in this idealized atmosphere is analogous to ϵ in the real
504 atmosphere. If $\zeta = 1$, Equation (2) becomes the exponential decay equation where CWP has an e-
505 folding timescale of α^{-1} . For $\zeta \neq 1$, the solution is

506
$$CWP(t) = [\alpha(\zeta - 1)t + 1]^{\frac{1}{1-\zeta}} \quad (3)$$

507 This leads to an e-folding timescale t_e of

508
$$t_e = \frac{1}{\alpha} \frac{e^{\zeta-1} - 1}{\zeta - 1} = \eta/\alpha,$$

509

510 Where η is the correction coefficient for the e-folding timescale of α^{-1} . As η approaches 1, the e-
511 folding timescale approaches α^{-1} . From the satellite observations, $\zeta = 0.64$ and η is 0.84 (Fig.
512 S1). The assumption in Equation (2) of zero condensation sources makes the ϵ^{-1} “drying”
513 timescale an upper bound. In reality, condensing clouds oppose this drying and depart from the e-
514 folding timescale ϵ^{-1} .

515

516 *Observations*

517 We use monthly liquid water path and ice water path data from the MODerate-resolution Imaging
518 Spectroradiometer (MODIS) Level 3 Atmosphere Monthly Product [49] at 1° by 1° horizontal
519 resolution. For surface precipitation data we use the Tropical Rainfall Measuring Mission (TRMM)

520 Multisatellite Precipitation Analysis 3B42RT daily precipitation product [50]. Its native horizontal
521 resolution of 0.25° by 0.25° was re-gridded to 1° by 1° to match the MODIS data. Measurements
522 of monthly top-of-atmosphere longwave radiative fluxes used in this study were from the Clouds
523 and Earth’s Radiation Energy System (CERES) SYN1deg-Ed4A product, which combines data
524 from Aqua and Terra [51]. Monthly gridded surface temperature data (land and ocean) are from
525 the Berkeley Earth Surface Temperatures dataset, available at
526 <http://berkeleyearth.org/archive/data/>. Monthly SLP data is from the Hadley Centre Sea Level
527 Pressure Dataset [52], available at <https://psl.noaa.gov/data/gridded/data.hadslp2.html>.

528

529 *Uncertainty in Precipitation and Cloud Water Path Observations*

530 Observed liquid water path (LWP) and ice water path (IWP) are in-cloud values. These are
531 weighted by cloud fraction to render them comparable with the models’ grid-box averaged cloud
532 water path, computed by the following expression at each grid point:

$$533 \quad CWP_{obs} = f_{obs}(IWP_{obs} + LWP_{obs})$$

534 Where the subscript *obs* indicates observational data and *f* is cloud fraction.

535 Uncertainty in ϵ can be estimated using the individual uncertainties in P_g and CWP .
536 MODIS sensors are calibrated with high accuracy. Ref [53] conducted an analysis of available
537 satellite estimates of LWP against passive microwave observations and found that MODIS
538 outperforms all other satellite observational products. In the three regions they analyzed, MODIS
539 estimates generally underestimate the monthly-mean LWP by 8-9% relative to terrestrial
540 microwave estimates. However, the correlation coefficient between monthly MODIS and
541 microwave data is 0.9. Similar estimates are unavailable for IWP. TRMM exhibits lower errors
542 than other real-time precipitation observational products at most temporal scales. Ref [54]

543 analyzed monthly surface precipitation (P_s) data over the maritime continents and found that
544 TRMM underestimates P_s by 6% compared to rain gauge measurements, with a monthly
545 correlation coefficient of $r = 0.86$. Using the error estimates, 6% in P_s and 9% in CWP (assuming
546 that IWP uncertainties are similar magnitude to the LWP range), we estimate the uncertainty of ϵ

$$547 \quad \frac{\Delta\epsilon}{\epsilon} = \left[\left(\frac{\Delta P_s}{P_s} \right)^2 + \left(\frac{\Delta CWP}{CWP} \right)^2 \right]^{\frac{1}{2}} \approx 11\%$$

548

549 *ERA5 Reanalysis*

550 Data from the ERA5 Reanalysis [55] are obtained from the Climate Data Store (available at
551 [https://cds.climate.copernicus.eu/cdsapp#!/dataset/reanalysis-era5-pressure-levels-monthly-](https://cds.climate.copernicus.eu/cdsapp#!/dataset/reanalysis-era5-pressure-levels-monthly-means)
552 [means](https://cds.climate.copernicus.eu/cdsapp#!/dataset/reanalysis-era5-pressure-levels-monthly-means)) and interpolated to the same grid as the observations (1° by 1° resolution).

553

554 *CRM experiments*

555 Idealized experiments of radiative convective equilibrium in limited domains are performed using
556 the System for Atmospheric Modeling (SAM; [56]), three-dimensional cloud resolving model that
557 employs the anelastic equations of motion. As in previous studies of convective self-aggregation
558 with SAM, we use a 1-moment microphysics package. The model grid is a staggered Arakawa C-
559 type grid with a uniform horizontal resolution of 2 km and stretched in the vertical. The lowest
560 model level is 37 m and the grid spacing is 75 m, increasing to 500 m above 3.5 km. The lateral
561 boundary conditions are doubly periodic. We achieve radiative-convective equilibrium by forcing
562 the model with perpetual sun (no diurnal cycle), no mean wind, no rotation, and no other external
563 forcing. Independent experiments were run with fixed SSTs at 299K, 300K, 301K, and 303K. The

564 two sets of experiments shown in Fig. 4 are SAM-S and SAM-L which employ a 512 x 512 km²
565 domain and a 1024 x 1024 km² domain, respectively.

566 All SAM-L experiments self-aggregate to form a single cluster of convection after day 80
567 of the simulation. The SAM-S experiments do not self-aggregate due to the domain size limitation.
568 This domain size dependence of self-aggregation has been previously well studied [57, 58]. We
569 used the domain-size difference between SAM-L and SAM-S to isolate the effects of self-
570 aggregation while keeping the external forcing identical. Each experiment is averaged from day
571 80 to 100 after reaching statistical equilibrium.

572

573 *CMIP6 Models*

574 We use the CMIP6 archive [59] to obtain data for 44 GCMs in the preindustrial control simulation
575 (piControl) and 28 models in the SSP585 scenario. This represents all models with available output
576 to compute ϵ at the time of analysis. Warming responses are computed by taking the difference
577 between years 2085-2100 and years 2015-2030 in the SSP585 scenario.

578

579 *Parameterization of Convective Precipitation in CMIP6 Models*

580 The two representative convective parameterization schemes in CMIP6 are the Tiedtke scheme
581 ([42]; hereafter T89) and the Zhang and McFarlane scheme ([41]; hereafter ZM95). In T89, deep
582 convection is triggered when there is net water vapor convergence in the atmospheric column and
583 air lifted from the surface to above cloud base remains buoyant. The conversion from cloud
584 droplets to convective precipitation is given by:

$$585 \quad P_{T89}(z) = K(z)l$$

586 where $P_{T89}(z)$ is the precipitation rate at height z , l is the cloud water content in mm, and $K(z)$ is
587 a step function that takes the value of $0.002s^{-1}$ above a constant offset above cloud base and zero
588 elsewhere. P_{T89} depends only on the cloud water content.

589 In ZM95, deep convection is triggered in a column if the convective available potential
590 energy, after accounting for dilution from entrainment of dry air, exceeds $70 Jkg^{-1}$. Convective
591 precipitation is given by the following expression [60]:

$$592 \quad \rho P_{ZM95}(z) = C_0 M_u l$$

593 where $C_0 = 0.002m^{-1}$, M_u is the updraft mass flux, and ρ is the air density, and l is the cloud
594 water content. P_{ZM95} is proportional to both M_u and l .

595

596 *Strength of the Pacific Walker Circulation*

597 Following [61], to measure the mean strength of the Pacific Walker circulation (Fig. 3b) we
598 compute Sea Level Pressure (SLP) averaged over the equatorial Western Pacific (SLP_W ; $5^\circ S-5^\circ N$,
599 $80^\circ-160^\circ E$) and equatorial Eastern Pacific (SLP_E ; $5^\circ S-5^\circ N$, $160^\circ-80^\circ W$), and use their difference,
600 denoted as $dSLP$:

$$601 \quad dSLP = SLP_E - SLP_W$$

602 To measure projected changes in the strength of the Walker circulation, we compute the
603 average pressure velocity at $800hPa$ over the equatorial Eastern Pacific (ω_{EP} ; $10^\circ S-10^\circ N$,
604 $160^\circ E-100^\circ W$). This definition shows the strongest correlation with changes in the SST gradient
605 between the eastern and western equatorial Pacific, in which the Pacific Walker Circulation is
606 tightly coupled to. We find that this measure provides more robust results on future Walker cell
607 changes across different models as it is less dependent on the choice of the averaging boxes than
608 $dSLP$.

609

610 *Strength of the Hadley Circulation*

611 To measure the strength of the Hadley circulation, we firstly estimate the ITCZ location (ϕ_{ITCZ})
612 defined as the zeroth crossing of the zonal-mean mass streamfunction ψ closest to the equator. The
613 Hadley cell's meridional extent in each hemisphere is the distance between ϕ_{ITCZ} and the first
614 zeroth crossing of ψ poleward of ϕ_{ITCZ} . The strength of the Hadley Circulation in each hemisphere
615 is estimated by taking the maximum of ψ between 700 and 300 hPa throughout its meridional
616 extent [62].

617

618

619 **DATA AVAILABILITY**

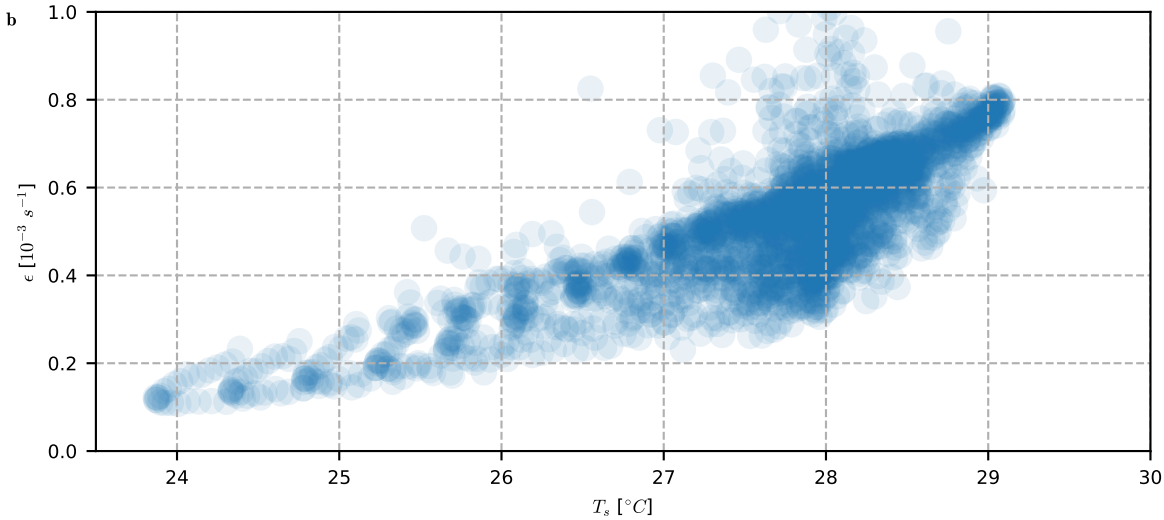
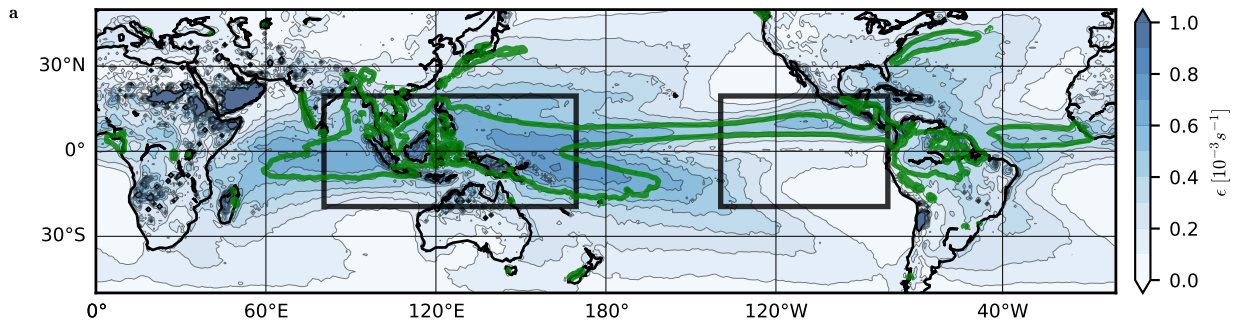
620 TRMM data is obtained from <https://gpm.nasa.gov/missions/trmm> are interpolated from their
621 native 0.25° by 0.25° resolution to 1° by 1° to match that of the MODIS monthly data available at
622 <https://atmosphere-imager.gsfc.nasa.gov/products/monthly>. Monthly surface temperature
623 (<http://berkeleyearth.org/archive/data/>) and SLP observations
624 (<https://psl.noaa.gov/data/gridded/data.hadslp2.html>) are also publicly available. Monthly-mean
625 Nino 3.4 SST data is obtained from:
626 <https://www.ncdc.noaa.gov/teleconnections/enso/indicators/sst/>. ERA5 data are downloaded from
627 [https://cds.climate.copernicus.eu/cdsapp#!/dataset/reanalysis-era5-pressure-levels-monthly-](https://cds.climate.copernicus.eu/cdsapp#!/dataset/reanalysis-era5-pressure-levels-monthly-means)
628 [means](https://cds.climate.copernicus.eu/cdsapp#!/dataset/reanalysis-era5-pressure-levels-monthly-means) and interpolated from their native 0.25° by 0.25° grid to 1° by 1° resolution. The CMIP6
629 data supporting this study are available from <https://pcmdi.llnl.gov/CMIP6/>. Data from the CRM
630 experiments and satellite derived observations of ϵ are available at
631 <https://doi.org/10.5061/dryad.g4f4qrfsr> [63].

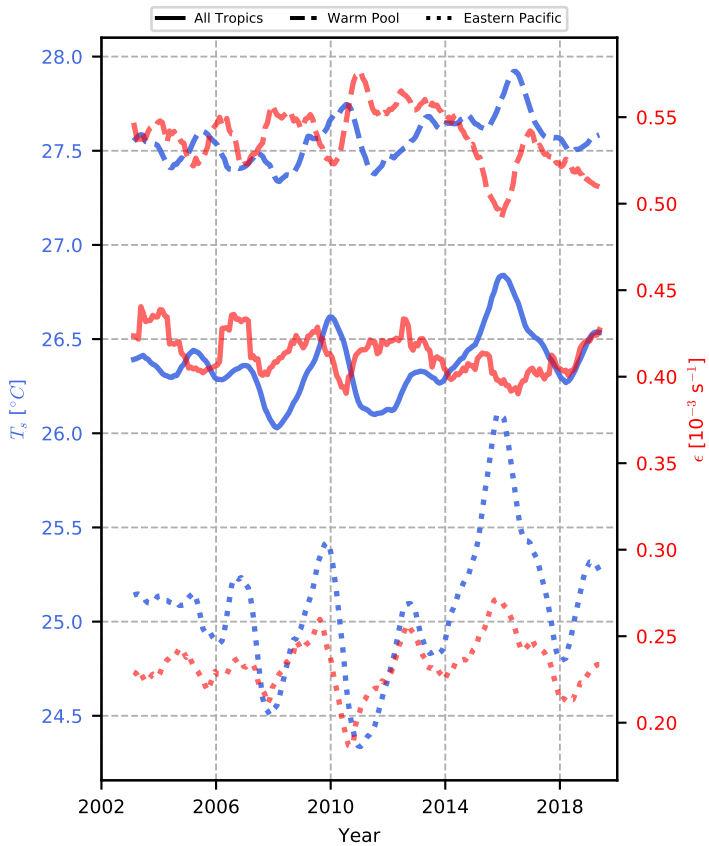
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OLR vs. ϵ_{WP} correlation

