

## Coronal heating by MHD waves

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**Abstract** The heating of the solar chromosphere and corona to the observed high temperatures, imply the presence of ongoing heating that balances the strong radiative and thermal conduction losses expected in the solar atmosphere. It has been theorized for decades that the required heating mechanisms of the chromospheric and coronal parts of the active regions, quiet-Sun, and coronal holes are associated with the solar magnetic fields. However, the exact physical process that transport and dissipate the magnetic energy which ultimately leads to the solar plasma heating are not yet fully understood. The current understanding of coronal heating relies on two main mechanism: reconnection and MHD waves that may have various degrees of importance in different coronal regions. In this review we focus on recent advances in our understanding of MHD wave heating mechanisms. First, we focus on giving an overview of observational results, where we show that different wave modes have been discovered in the corona in the last decade, many of which are associated with a significant energy flux, either generated in situ or pumped from the lower solar atmosphere. Afterwards, we summarise the recent findings of numerical modelling of waves, motivated by the observational results. Despite the advances, only 3D MHD models with Alfvén wave heating in an unstructured corona can explain the observed coronal temperatures compatible with the quiet Sun, while 3D MHD wave heating models including cross-field density structuring are not yet able to account for the heating of coronal loops in active regions to their observed temperature.

**Keywords** Sun: corona · Sun: waves

## 1 Introduction

Coronal heating is a long-standing problem. It is quite clear that the energy for the hot corona comes from the convective motions of the solar photosphere, and that the magnetic field plays a key role in it. However, how the energy is transported and dissipated is still not fully understood. Proposed heating mechanisms are classified based on the comparison of the convective time scales and the Alfvén transit time in the corona. Slow driving of the magnetic field that produces reconnection and energy release in current sheets and null points, is referred to as DC heating mechanisms (Parker, 1986). Fast driving of the magnetic field, is known as MHD wave heating (e.g. Alfvén, 1947) and AC heating mechanisms.

DC heating mechanisms consider the slow stressing of the coronal magnetic field. It leads to current sheets where Ohmic dissipation is at work, or to Parker’s idea of nanoflares. In the latter idea, the magnetic field is tangled because of the photospheric motions, so that it evolves into a non-potential state. This magnetic energy is then released into the plasma by reconnection, resulting in localised heating and thus nanoflares. DC heating mechanisms have received a lot of attention over the years in numerical modelling and observations (e.g. Gudiksen and Nord-

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lund, 2005; Reep et al., 2013; Rempel, 2017; Warnecke et al., 2017; Srivastava et al., 2019).

In this review, we focus on AC heating mechanisms. In these heating mechanisms, the convective motions launch disturbances that travel into the corona, usually in the form of magnetohydrodynamic (MHD) waves. In the corona, the wave energy has to be dissipated to heat the plasma. This is non-trivial, because many wave modes damp only on resistive time scales in a homogeneous plasma, and damping times are proportional to the magnetic Reynolds number. In the solar corona, the Reynolds number is very large, on the order of  $10^{14}$ , which would produce unrealistically long heating times, compared to the coronal cooling timescale. Cross-field inhomogeneity enables physical processes that produce a cascade of wave energy to small spatial scales where dissipative processes may act and heat the plasma more rapidly. In recent years, there has been a drive towards (1) observational characterisation of wave energy content in the corona, and (2) numerical modelling of wave heating, focusing on the energy input, the energy propagation and the energy dissipation. Here, we aim to give an overview of these recent results.

For material beyond the current review, we refer the reader to, for example, Aschwanden (2019).

## 1.1 Brief historical overview

The idea for heating the solar corona by MHD waves has been around for more than half a century. An overview of the early ideas before the 80s can be found in Kuperus et al. (1981). In those years, it was realised that it is necessary to generate small scales in order to damp the wave energy in a timely manner. Heyvaerts and Priest (1983) developed the theory of phase mixing, while resonant absorption (Chen and Hasegawa, 1974) was applied to the corona for the first time by Ionson (1978). Subsequently, the MHD wave energy input and transmission into coronal loops was studied in key papers such as Hollweg (1984). Later on, the efficiency of the heating by resonant absorption was calculated in 1D numerical models of loops (Poedts et al., 1990, among others), and in 3D models (Ofman et al., 1994, and follow-up works), even resulting in forward modelled coronal loops (Belien et al., 1996), motivated by early high resolution soft X-ray observations of coronal loops that became available from the Yohkoh satellite.

In hindsight, it is amazing that these early papers worked so well and were so relevant, given that no direct observational evidence was available back then on the presence of MHD waves in the solar corona. Indeed, although substantial, only indirect evidence existed of the potentially important role of MHD waves in the solar atmosphere. Such evidence was based on the strong emission and broad non-thermal line widths in the upper chromosphere, transition region and corona with observations from Skylab (Feldman et al., 1988) and HRTS (High-Resolution Telescope and Spectrograph, Dere and Mason, 1993). This changed dramatically with the launch of SOHO (Solar and Heliospheric Observatory) and TRACE (Transition Region And Coronal Explorer). Data from the former were used to show the presence of slow waves in the corona (Chae et al., 1998; Ofman et al., 1999; Berghmans and Clette, 1999), while data from the latter revealed the presence of transverse, post-flare loop oscillations (Nakariakov et al., 1999; Schrijver et al.,

1999; Aschwanden et al., 1999). An overview of the contextualisation of earlier models with those observational findings is given in Walsh and Ireland (2003); Ofman (2005).

LCR models (named after the usual symbols in electric components for inductance  $L$ , capacitance  $C$  and resistance  $R$ ) were also developed extensively for MHD waves in coronal loops (see Stepanov et al., 2012, and reference therein). In such models, the magnetic twist in the loop behaves as a current system with its source in the photosphere and equivalent electric resistivity and inductance in the corona (see e.g., Spicer, 1977; Carlqvist, 1979). However, it is still unclear how this LCR model relates to MHD models of coronal loop oscillations (based on e.g. Edwin and Roberts, 1983). Moreover, since no development of these models was made in the last years, we will omit them from this review.

## 1.2 Observational motivation

Starting with the advent of high resolution space-based observations of the solar corona in soft X-ray and EUV in the 90s, there is now an avalanche of new MHD wave modes detected in the solar corona, as described in detail by De Moortel and Nakariakov (2012). Their consequences for heating the corona are discussed in Arregui (2015).

Another major paradigm change in our perception of MHD waves in the solar atmosphere came from ground-based observations with *CoMP* (Tomczyk et al., 2007), which showed the omnipresence of these waves in the solar corona, and spectroscopic and imaging from space with *Hinode*, which, thanks to its high resolution, allowed to better quantify the amount of energy available for the corona (De Pontieu et al., 2007). Moreover, *SDO/AIA* revealed the existence of many new wave modes and made more detailed observations of previously observed coronal waves (for a review, see Liu and Ofman, 2014).

The improvement in spatial, spectral and temporal resolution of instrumentation also meant that MHD waves could be characterised in terms of their slow, fast or Alfvén nature, as well as their wave numbers (see the review by De Moortel and Nakariakov, 2012). Indeed, high spatial resolution and high sensitivity allows to distinguish transverse motions of the waveguides as well as the compressibility of the gas from density diagnostics, while high spectral and temporal resolution allows to relate these quantities to the evolution of the Doppler and non-thermal velocities, thereby determining the 3D motion of the plasma produced by the waves (see e.g. Fujimura and Tsuneta, 2009; Kitagawa et al., 2010; Wang, 2016; Hinode Review Team et al., 2019, chapter 6.1).

Lastly, multi-wavelength observations with instruments such as those of *Hinode* and *IRIS*, or through coordinated observations with space and ground-based observatories allowed to simultaneously scan several layers of the solar atmosphere. Although a complicated task, this provides the propagation history of the wave, which is essential to determine wave processes such as reflection and refraction, and in particular mode conversion and dissipation of MHD waves for coronal heating (Arregui, 2015).

**Table 1** Overview of detected wave energy fluxes. The first column shows the structure in the solar atmosphere with the observed wave mode (second column) and the observing instrument (third column). The fourth column shows the estimated energy flux, as found by the reference mentioned in the fifth column. If a cell is left empty, the value from the previous line are meant.

Structure	Wave mode	Instrument	Energy flux ( $\text{W m}^{-2}$ )	Reference
coronal arcade	propagating kink	CoMP	100	Tomczyk et al. (2007)
coronal funnels	quasi-periodic fast wave trains	AIA	$(0.1 - 2.6) \times 10^4$	Liu et al. (2011)
		simulations	$3.7 \times 10^5$	Ofman et al. (2011)
		AIA	$1.8 \times 10^2$	Ofman and Liu (2018)
magnetic pores	Alfvén waves	ROSA	$1.5 \times 10^4$ (locally) 240 (globally averaged)	Jess et al. (2009)
	propagating slow sausage	DST	$3.5 \times 10^4$	Grant et al. (2015)
fibrils	propagating kink	ROSA	$4.3 \times 10^3$	Morton et al. (2012)
	propagating fast sausage		$1.17 \times 10^4$	
spicules	Alfvén waves	SST	$10^5$	Srivastava et al. (2017)
	kink		$10^2 - 10^4$	this review, based on De Pontieu et al. (2012)

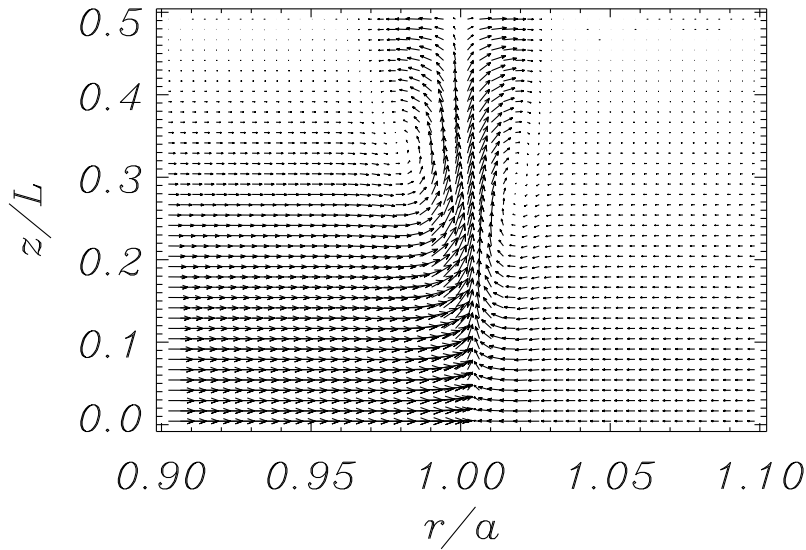
## 2 Observations

Below, we describe recent detections of wave power in the solar atmosphere. We summarise the energy fluxes in Table 1 to give a clear overview.

### 2.1 Impulsively excited standing kink waves

Often flares and low coronal eruptions (LCEs) are seen to excite standing kink waves in coronal loops (Zimovets and Nakariakov, 2015). Goddard et al. (2016a) and Nechaeva et al. (2019) performed a statistical study of these types of events and found that the loops oscillate with an amplitude between 1-10 Mm and periods between 1-28 min. While the coronal impulsive event that causes the oscillations is apparent, the exact mechanism for their excitation is not well understood. Several possibilities were investigated in the literature: internal and external (gas or magnetic) pressure drivers (Terradas et al., 2007; McLaughlin and Ofman, 2008; Pascoe et al., 2009; Selwa and Ofman, 2009; Pascoe and De Moortel, 2014), loop contraction (Russell et al., 2015; Pascoe et al., 2017), or collision of flows (Antolin et al., 2018a; Pagano et al., 2019, even though these would result in propagating waves). More information about observations of impulsively excited standing waves can be found in the review by Nakariakov et al. (2021).

The energy available in impulsively excited standing waves and the fraction that is dissipated remains to be characterised from observations. An energy analysis based on bulk plane Alfvén waves is too simplistic because kink mode energy is localised in space (Goossens et al., 2013). Magnetic and plasma structures act as frequency filters, trapping part of the available energy and distributing it along and across the coronal field. Wave energy propagation, once filtered by the structure is localised in space. Energy flows into the resonance because of the jump in the radial component of the Poynting vector (Arregui et al., 2011), as shown in Fig. 1. Then, it propagates and dissipates along the field in a way determined by the density profile and dissipative coefficients.



**Fig. 1** Spatial distribution of the Poynting vector in the  $(r, z)$ -plane around the resonant position at  $r/a = 1$  for a standing kink mode in a loop with a density contrast of 10 and a non-uniform layer of length  $l/a = 0.2$ . The magnetic Reynolds number is  $R_m = 10^6$ . Figure modified from Arregui et al. (2011).

Terradas and Arregui (2018) considered each part of the sequence of physical processes that would enable to heat a typical coronal waveguide from the energy contained in a typical transverse oscillation. Each part of the sequence has its characteristic time and spatial scales. The damping time is determined by the cross-field plasma and field structuring. The energy cascade to small scales is determined by a phase mixing length that also depends on the cross-field variation of the Alfvén speed. The onset of resistive dissipation and its duration depend on the Reynolds number and the cross-field plasma variation. Considering typical values of these quantities we cannot expect resistive diffusion to operate during the oscillation process. Any observational evidence about wave heating by resistive damping of impulsively excited standing waves will come from the observation of indirect consequences. According to (Terradas and Arregui, 2018), for a loop displacement of the order of the radius and typical loop parameters, all the kinetic and magnetic energy of a typically observed single kink mode is of the order of  $10^{19}$  J. Simple energy conservation calculations indicate that, even if we were able to concentrate in a typical resonant layer and transform into internal energy all the kinetic and magnetic energy of a typically observed single kink mode, we could just obtain a temperature increase of about  $10^5$  K (Terradas and Arregui, 2018).

When an ensemble of mini-tubes are considered, filling factors can be employed (Van Doorselaere et al., 2014), which leads to an energy flux reduction directly related to the filling factor. Although resonant damping and mode coupling are robust in coronal loop models with rather arbitrary continuous plasma distributions,

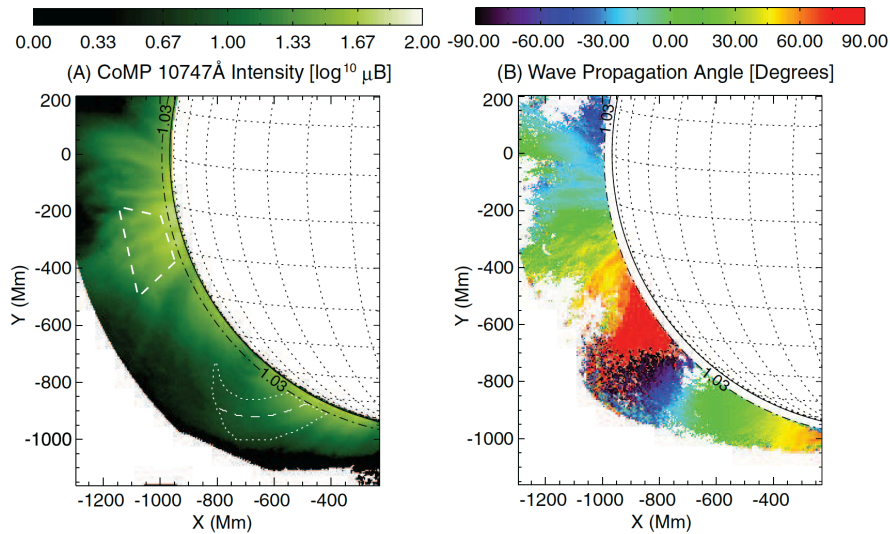
the multi-strand structure of loops could be quickly destroyed due to instabilities in individual strands and their interaction (Magyar and Van Doorselaere, 2016).

## 2.2 CoMP waves

Prevalent propagating waves were reported (Tomczyk et al., 2007; McIntosh et al., 2011) from observations of both the Coronal Multi-channel Polarimeter (CoMP, Tomczyk et al., 2008) and the Atmospheric Imaging Assembly (AIA, Lemen et al., 2012) on board the Solar Dynamics Observatory (SDO). Using CoMP observations, Tomczyk et al. (2007) found ubiquitous upward propagating disturbances along off-limb coronal loops in the Doppler shift of the Fe XIII 10747 Å line (Figure 2). Since the Doppler shift refers to the motion along the line of sight (LOS) and the magnetic field lines in the off-limb corona are largely perpendicular to the LOS, these disturbances are essentially signatures of transverse MHD waves. The propagation speed was found to be from a few hundred km s<sup>-1</sup> to 2000 km s<sup>-1</sup>, which is on the order of the coronal Alfvén speed. Based on these characteristics, Tomczyk et al. (2007) and Tomczyk and McIntosh (2009) interpreted these transverse waves as Alfvén waves. They found a power-law spectrum of the Doppler shift with a spectral index of about 1.5, consistent with isotropic MHD turbulence. The power spectrum of the observations shows a peak around 3.2 mHz (period of 5 minutes). The velocity amplitude is only 0.5 km s<sup>-1</sup>, and the energy flux of these waves appears to be at least three orders of magnitude lower than that required to balance the radiative losses of the quiet corona. The low-amplitude is likely due to the low spatial resolution of CoMP ( $\sim 9''$ ) and the line-of-sight integration resulting in spatial averaging of the waves. Similar results were also found in open-field regions (Morton et al., 2015). By carefully analyzing the displacement of coronal structures observed by the much higher-resolution AIA instrument ( $\sim 1.5''$ ), McIntosh et al. (2011) found much larger velocity amplitudes, i.e.,  $\sim 20$  km s<sup>-1</sup>, for these transverse waves. They estimated the energy flux of the waves as  $\sim 100$  W m<sup>-2</sup> and found that the waves have sufficient energy to power the quiet corona and fast solar wind. However, the observed wave energy flux is still much lower than that required to heat the active region corona ( $\sim 2000$  W m<sup>-2</sup>).

The interpretation of these waves as Alfvén waves was controversial. As argued by Van Doorselaere et al. (2008), in cylindrical plasma structures these waves appear to be more appropriately interpreted as fast-mode kink waves rather than Alfvén waves. However, others claimed that these waves could be called Alfvénic waves as the major restoring force for these waves is definitely magnetic tension (Goossens et al., 2009; McIntosh et al., 2011), they carry parallel vorticity (Goossens et al., 2012) and they are inherently coupled to the local azimuthal Alfvén waves (Pascoe et al., 2010). This mode is also called surface Alfvén wave or resonantly damped kink mode. At the end, the heating will come from azimuthal Alfvén wave dissipation. The global eigen-mode just plays the role of trapping/channelling the energy from around/below. A well defined structure is not needed, as shown by Terradas et al. (2008b); Rial et al. (2010); Pascoe et al. (2011).

Despite the debate on the nature and terminology for these waves, the discovery of these propagating transverse waves has caught the attention of many researchers in the field. There are at least two reasons for this. First, they allow us to map

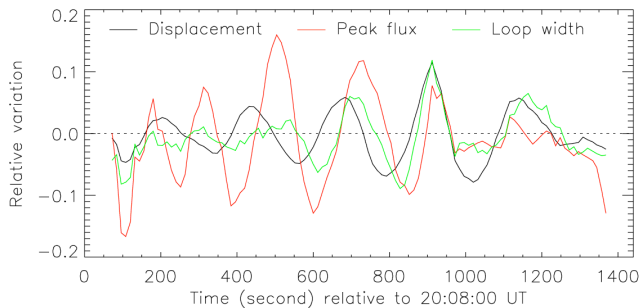


**Fig. 2** Images of the Fe XIII 10747 Å line intensity and the wave propagation angles derived from the Doppler shift of Fe XIII 10747 Å in part of the corona observed by CoMP. Adapted from Tomczyk and McIntosh (2009).

the global coronal magnetic field based on the technique of coronal seismology (Magyar and Van Doorselaere, 2018; Anfinogentov and Nakariakov, 2019; Yang et al., 2020a,b). Second, their ubiquity means they could potentially play an important role in coronal heating. The observed waves show a discrepancy between the outward and inward wave power (Tomczyk and McIntosh, 2009), a property that resonantly damped wave models seem to capture well (Verth et al., 2010; Pascoe et al., 2010), and that is also observed in-situ in the solar wind (see the review by Bruno and Carbone, 2013). A recent study by Montes-Solís and Arregui (2020) considers a distinct power generated at loop foot-points as an additional source of discrepancy. It shows that, if present, it would affect obtaining quantitative evidence for resonant damping.

The origin of the waves detected by CoMP has recently been linked to the Sun’s internal acoustic oscillations, and in particular to p-modes. Indeed, Morton et al. (2019) have shown that there is a distinct excess of wave power at the usual p-mode frequency of 3–5 mHz, across the solar cycle and different coronal structures (or regions) in the Sun (Morton et al., 2016). The authors further show that the usual Alfvénic fluctuations observed with SDO/AIA (McIntosh et al., 2011) have the same characteristics in their power spectra as the CoMP waves. Evidently, p-modes contain orders of magnitude more power than required for coronal heating. The physical mechanism proposed to explain the ubiquity of these waves is the double mode conversion process of p-modes during their propagation across the low atmospheric layers, during which their energy is transferred to Alfvénic modes (Cally and Hansen, 2011; Felipe, 2012; Cally, 2017). A strong consequence of this is





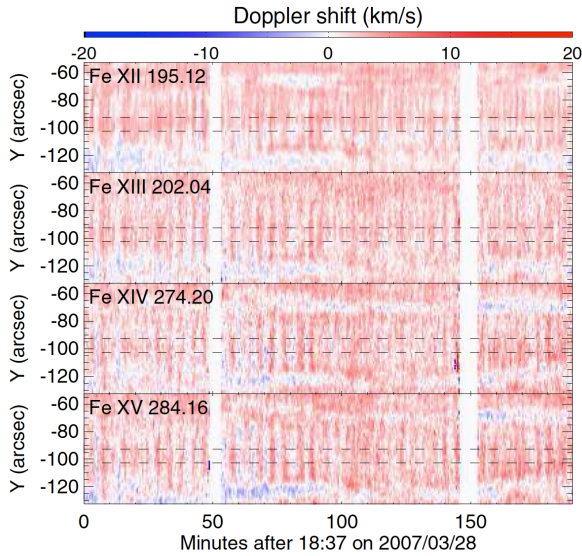
**Fig. 3** Decayless oscillations of coronal loops seen in the loop displacement, peak flux and loop width estimated from the AIA 171 Å images. Adapted from Wang et al. (2012).

that solar and stellar coronae have a non-negligible energy source in their internal acoustic oscillations. Although direct observations of this process are still lacking, these results also suggest that p-modes may play a role in the onset of standing or propagating Alfvénic modes.

### 2.3 Decayless oscillations

Decayless oscillations normally refer to standing waves without obvious observed damping in coronal loops. In coronal lines<sup>1</sup>, these oscillations were first reported independently by Wang et al. (2012) and Tian et al. (2012) through imaging and spectroscopic observations, respectively. The transverse oscillations reported by Wang et al. (2012) from SDO/AIA observations appear to be triggered by a coronal mass ejection. They lasted for more than ten cycles and even revealed growing amplitudes (Figure 3). Tian et al. (2012) performed a survey of decayless (referred to as “persistent” in their paper) Doppler shift oscillations using three-month spectroscopic observations from the EUV Imaging Spectrometer (EIS, Culhane et al., 2007) on board Hinode. They found that such decayless oscillations, with a period of 3–6 minutes and a velocity amplitude of 1–2 km s<sup>-1</sup>, are very common in quiet coronal loops and can be observed in several coronal emission lines formed in the temperature range of 1.3–2 MK (Figure 4). These oscillations generally reveal no obvious damping during the whole observed time interval, which often last for a few hours. They were interpreted as standing kink oscillations by these authors. Since 2012, these decayless oscillations have been frequently reported for a variety of different observations (e.g., Nisticò et al., 2013, 2014), and it was found that their periods scale with the loop length (Anfinogentov et al., 2015), strongly supporting the standing wave interpretation.

<sup>1</sup> Small amplitude decayless oscillations were also observed in a prominence with *Hinode*/SOT (Ning et al., 2009), and of significant and increasing amplitude in a coronal loop with rain (Antolin and Verwichte, 2011). Due to the presence of chromospheric material and the associated processes specific to the formation of prominences and coronal rain, the processes responsible for such oscillations may likely be different than those observed in coronal lines.



**Fig. 4** Decayless oscillations of quiet coronal loops seen in the Doppler shift of four coronal emission lines. The Y-axis is roughly aligned with the corona loop. Adapted from Tian et al. (2012).

The decayless behavior of these waves suggests a continuous supply of energy to the system. Several different ideas have been proposed to maintain these decayless or persistent oscillations. For instance, Nakariakov et al. (2016) interpreted these decayless kink oscillations as a self-oscillatory process (a process in which the driver is a consequence of the oscillation itself, see Jenkins, 2013), driven by interaction between the loops and quasi-steady flows at the loop footpoints. Antolin et al. (2016) have shown that the decayless pattern could also be an apparent effect produced by the combination of low instrumental resolution and the periodic brightening generated by TWIKH rolls (Transverse Wave Induced Kelvin-Helmholtz rolls, cf. Sec. 3.3). In this interpretation, the decayless character reflects the low damping character of the azimuthal Alfvén waves resonantly coupled to the kink mode at the boundary layer. Another theory is through continued footpoint driving (Karamelas et al., 2017) providing an upward Poynting flux balancing the resonant and non-linear damping of the kink waves. Recent numerical experiments (Karamelas et al., 2019b; Guo et al., 2019b) reproduce the observations of decayless oscillations very well. More recently, Afanasyev et al. (2020) developed a one-dimensional and time-dependent analytical model by considering kink oscillations of coronal loops driven by random motions of loop footpoints. They have managed to reproduce a number of observational facts about these decayless kink oscillations, such as the quasi-monochromaticity, period-length relationship and excitation of multiple harmonics.

## 2.4 Available energy in quasi-periodic fast mode wave trains

The high cadence and spatial resolution of SDO/AIA in EUV enabled the discovery of quasiperiodic fast mode propagating wave trains (QFPs) (see, Liu et al. (2010, 2011), the review Liu and Ofman (2014)). The waves were observed to be associated with flares and propagate at a high speed of 1000-2000 km s<sup>-1</sup> with periods in the range of minutes and intensity variations  $\delta I/I \sim 5\%$ . The waves were modeled first by Ofman et al. (2011) using a 3D MHD model of a realistic bipolar active region structure and identified as fast-mode magnetoacoustic waves. Since the initial discovery, these waves were observed, studied, and modeled in many events associated with flares (see, e.g. Liu et al., 2012; Shen and Liu, 2012; Shen et al., 2013, 2017, 2018; Yuan et al., 2013; Kumar and Manoharan, 2013; Nisticò et al., 2014; Zhang et al., 2015; Goddard et al., 2016b; Qu et al., 2017; Ofman and Liu, 2018). Evidently, the QFPs carry some of the energy flux produced by the flares, and the observed dissipation of the QFP waves should result in coronal heating. The energy flux of the waves was estimated first using the parameters observed by SDO/AIA on 2010/08/01 by Liu et al. (2011) and was found to be in the range  $(0.1 - 2.6) \times 10^4$  W m<sup>-2</sup>, which is of the same order as the steady-state heating requirement of active region loops. The QFP wave energy flux estimate was based on the WKB approximation given by  $E = \rho \delta v^2 v_{ph} / 2 \geq \rho (\delta I / I)^2 v_{ph}^3 / 8$  (Aschwanden, 2004), where the intensity of the line emission,  $I \propto \rho^2$ , and the phase speed  $v_{ph}$  were determined directly from SDO/AIA observations ( $v_{ph} = 1600$  km s<sup>-1</sup>), and the number density is taken to be the typical coronal electron density  $\sim 10^8$  cm<sup>-3</sup>. The QFP wave trains lasted on the order of  $\sim 0.5$  hr and were repeatedly produced in the 2010/08/01 event. However, the divergence of the magnetic funnel in the active region and apparent dissipation of the waves reduced the apparent energy flux away from the flaring source.

Ofman et al. (2011) used the 3D MHD model results in an idealized bipolar active region of QFP wave trains combined with the WKB approximation to estimate the energy flux as  $E = \rho \delta v^2 V_f / 2 = 3.7 \times 10^5$  W m<sup>-2</sup>, where  $\rho$  is the coronal density,  $\delta v$  is the wave velocity amplitude, and  $V_f$  is the fast magnetoacoustic speed. The model energy flux was an order of magnitude greater than the direct estimate by Liu et al. (2011). However, the model estimate was based on idealized AR parameters in qualitative agreement with observations. In a recent study by Ofman and Liu (2018) of the double QFP event observed by SDO/AIA on 2013-5-22 the lower limit of the wave energy flux was estimated as  $1.8 \times 10^2$  W m<sup>-2</sup> high in the corona. The authors concluded that, taking into account coronal loop expansion, the wave energy flux could be at least one to two orders of magnitude higher near the source of the QFPs.

Statistical study of QFP waves indicates that these waves are quite common and often observed to be associated with C-class flares, although they can also result from stronger and weaker flares (Liu et al., 2016). Thus, combined with the challenging detection of these waves for lower energy flares, the contribution of QFP wave trains to coronal heating and to the energy flux requirement may be more significant than initially estimated. Thus, the problem of QFP wave train heating parallels the coronal heating problem by flares, where small energy flares (i.e., undetected nanoflares) are required for coronal heating and possibly their associated QFP waves are not directly detected (Aschwanden, 2004).

## 2.5 Observations and energy estimates of MHD waves in the lower solar atmosphere

The lower solar atmosphere (photosphere and chromosphere) plays an important role in the transmission of wave energy from the solar interior to the corona. Therefore, the assessment of wave energy content in this layer is crucial in understanding the coronal heating problem. Moreover, it is well established that the solar chromosphere requires substantially more energy flux than the corona ( $10^3$ – $10^4$   $\text{W m}^{-2}$ ) to compensate for its huge radiative losses (Withbroe and Noyes, 1977).

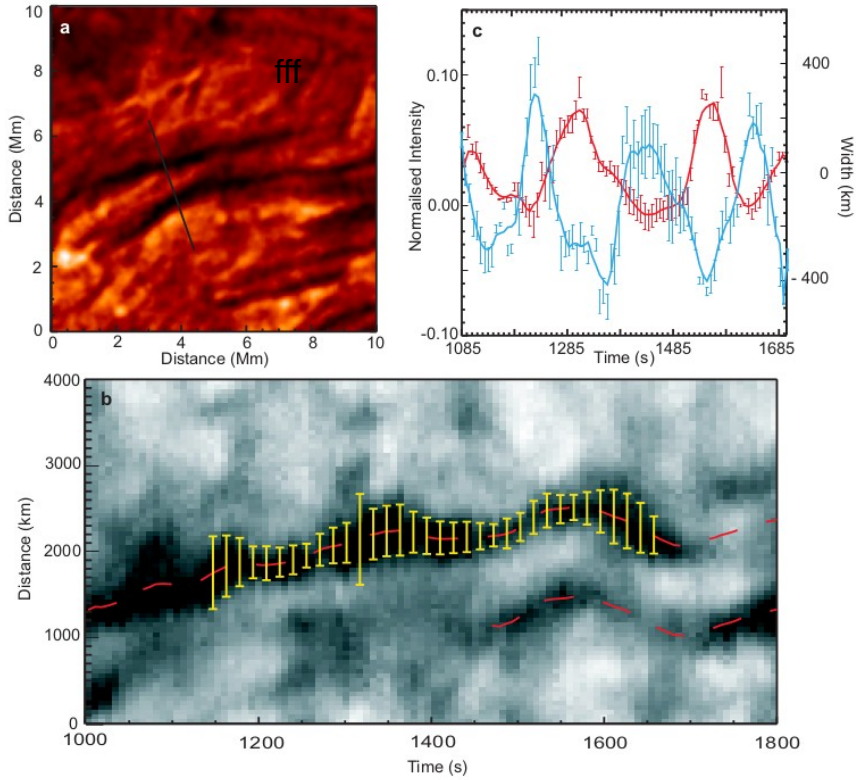
Recent observational findings from high-resolution ground (e.g., 1m-Swedish Solar Telescope, ROSA – Rapid Oscillations in the Solar Atmosphere) and space-based (e.g., IRIS – Interface Region Imaging Spectrometer, SDO – Solar Dynamics Observatory) observations reveal the presence of a high amount of energy flux associated with different MHD modes in a variety of magnetic structures coupling the various layers of the solar atmosphere.

In the photosphere, wave behaviour is found in pores and sunspots. Jess et al. (2009) reported the detection of Alfvén waves with periods of the order of 126–400 s associated with a large bright-point group. The energy flux associated with these wave modes is found to be  $1.5 \times 10^4$   $\text{W m}^{-2}$  in the chromosphere, which partially fulfills the chromospheric energy requirements. Using that 1.6% of the solar surface is observed to be covered by bright-points and assuming that they support such torsional waves with a 42% transmission coefficient (which may be on the high side), Jess et al. (2009) have estimated the global average energy in the corona as  $240$   $\text{W m}^{-2}$ , which is sufficient to heat it locally.

Grant et al. (2015) have detected upwardly propagating slow sausage waves in magnetic pores, which initially carry an energy flux of  $3.5 \times 10^4$   $\text{W m}^{-2}$ . The sausage wave energetics show a substantial decrease up to the chromosphere. These observations make it evident that magnetic pores transport waves to the higher layers, while also releasing energy in the local chromospheric plasma. However, it is not well quantified how much wave energy undergoes mode conversion, reflection or refraction. Aside from the frequently observed sausage modes, higher order magnetoacoustic oscillations ( $m \geq 1$ ) have also been observed in photospheric waveguides (e.g. Jess et al., 2017; Stangalini et al., 2018, and references cited there), including body and surface modes (Keys et al., 2018). Furthermore, Grant et al. (2018) presented evidence of Alfvén wave heating of the chromospheric plasma in an active region sunspot umbra. They showed the presence of mode conversion and the formation of magnetoacoustic shocks.

In conclusion, the random buffeting motions in the photosphere generate many MHD modes in the photospheric magnetic flux tubes along with a sufficient amount of energy flux. However, one has to bear in mind that these magnetic flux concentrations constitute only a small part of the photosphere, and it is unclear if these wave motions also propagate to the corona in quiet regions, where such photospheric magnetic flux tubes are less prevalent.

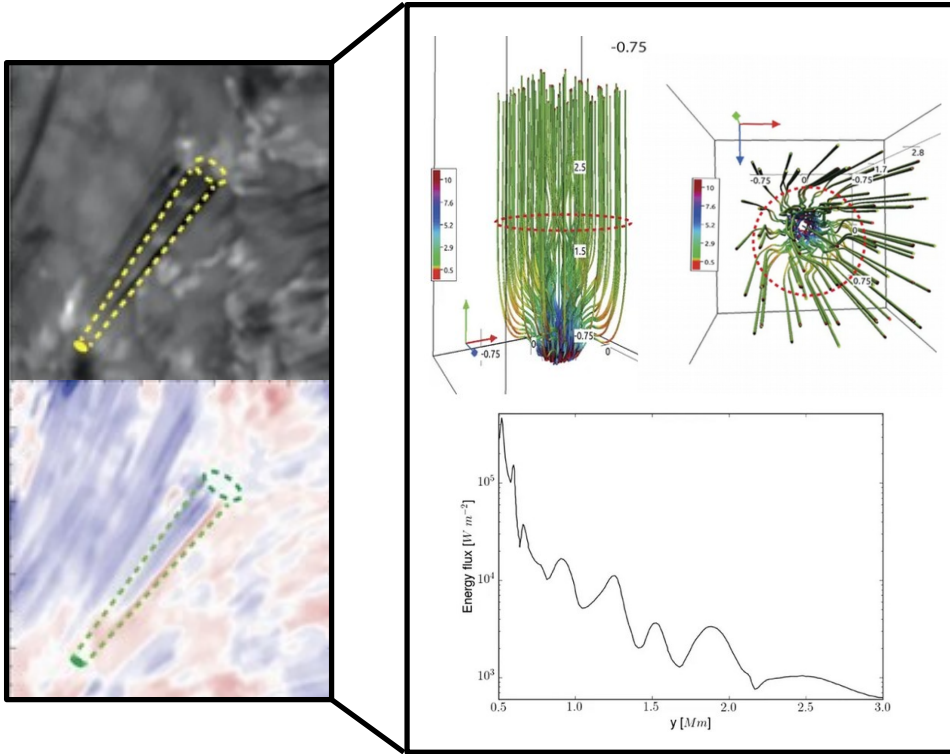
In the chromosphere, magnetic structures play a major role in guiding MHD waves. They are thus the prime structures in which waves are detected. In particular, Fig. 5 displays the results of Morton et al. (2012) who have observed the simultaneous presence of fast kink and sausage waves in mottles and fibrils using ROSA  $H_\alpha$  observations, and found that they carry an average energy of respec-



**Fig. 5** Simultaneous wave modes in a chromospheric magnetic flux tube using ROSA  $H_{\alpha}$  observations. Time-distance map ('b') exhibits the displacement of the tube's axis (red-dotted line) as a whole (kink waves), while its cross-section variation (sausage wave) is depicted by the yellow bars measuring the variation of tube's width. All measurement is done by Morton et al. (2012) from where this figure is adopted and displayed here. Kink wave respectively have period, upward propagation velocity, amplitude, and energy flux as  $\sim 232$  s,  $\sim 71$  km  $s^{-1}$ ,  $\sim 5$  km  $s^{-1}$ ,  $4300$  W  $m^{-2}$ . While, the same for the observed sausage wave are given respectively as  $\sim 197$  s,  $\sim 67$  km  $s^{-1}$ ,  $\sim 1-2$  km  $s^{-1}$ ,  $11700$  W  $m^{-2}$

tively  $4300$  W  $m^{-2}$ , and  $11700$  W  $m^{-2}$ , once again stressing the large amount of energy present in the lower atmosphere.

Going from the chromosphere to the transition region, spicules and their TR counterparts show ample evidence of wave dynamics. Observations of swaying motions in spicules with high-resolution imaging instruments such as *Hinode*/SOT and IRIS have long been attributed to propagating Alfvénic waves (De Pontieu et al., 2007; Tian et al., 2014). The amplitudes of the swaying motions are usually of the order of  $10 - 25$  km  $s^{-1}$ , although a factor of 5 larger motions have also been observed (Antolin et al., 2018b). In general, 1 or 2 oscillations of the spicules can be captured before the structure disappears, and a wide range of reported periods of  $100 - 500$  s and also high-frequency ( $20 - 50$  s Okamoto and De Pontieu, 2011). Srivastava et al. (2017) showed the ubiquitous presence of high frequency ( $\approx 12-42$  mHz) torsional motions in spicular-type structures in the chromosphere



**Fig. 6** The spicular-type structure (top panel of the left-box) shows periodic reversal of the velocity (snapshot shown in the bottom-panel of the left-box) indicating the presence of torsional Alfvén wave. The numerical simulation (top-panel of the right-box) exhibits similar torsional motions in the model fluxtube, that carry substantial energy (bottom-panel of the right-box) through the solar chromosphere, TR, and corona (Credit: Srivastava et al., 2017).

(Fig. 6, left box). Their numerical model showed that these observations resemble torsional Alfvén waves associated with high frequency drivers containing a huge amount of energy ( $\approx 10^5 \text{ W m}^{-2}$ ) in the chromosphere (Fig. 6, right-panel). It is important to note, however, that the observational signatures of TWIKH rolls can also explain these observations (Antolin et al., 2018b). Even after partial reflection from the transition region, Srivastava et al. (2017) found that a significant amount of energy ( $\approx 10^3 \text{ W m}^{-2}$ ) is being transferred into the overlying corona, which is sufficient to compensate the coronal radiative losses (Fig. 6, right panel). The propagation speeds of waves in spicules are often difficult to measure, due to their short lifetimes, the combination of (upward/downward) propagating and standing waves (Okamoto and De Pontieu, 2011) and also due to the rapidly increasing Alfvén speed at the observing heights. On average, speeds of  $200 - 300 \text{ km s}^{-1}$  are reported in these works.

The swaying motions of spicules suggest a transverse displacement of a waveguide and therefore such motions are often interpreted as kink waves. However,

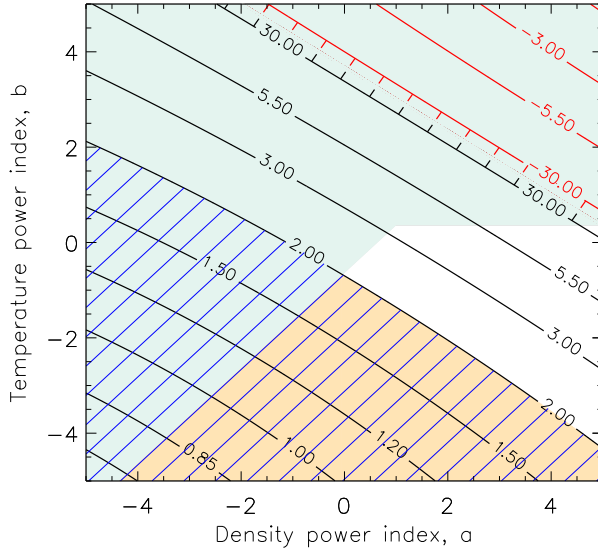
caution is required when only imaging information is available, since torsional Alfvén waves may also produce strand-like, swaying structures such as spicules (Antolin et al., 2018b). Moreover, additional to the swaying, torsional and longitudinal motions are observed in spicules (De Pontieu et al., 2012; Sekse et al., 2013), and are likely strongly connected to their generating mechanisms and to the nature of the wave. The nature of the Alfvénic wave (kink or torsional Alfvén wave) is important when trying to estimate the energy flux carried by the wave, since the collective or local nature distributes the wave energy differently across the waveguide (Van Doorselaere et al., 2014). Assuming a filling factor of 1 (a best case scenario), a typical spicule mass density of  $8 - 16 \times 10^{-14} \text{ g cm}^{-3}$  and based on the reported values, one can estimate the energy flux in swaying spicules as  $0.1 - 3 \times 10^3 \text{ W m}^{-2}$ , with the strongest cases at  $1 - 4 \times 10^4 \text{ W m}^{-2}$ . Usually, 3% of the energy is assumed to enter the corona, leading to average energy flux values of  $100 \text{ W m}^{-2}$  available for coronal heating, which is sufficient for the quiet Sun and for the acceleration of the solar wind (Tian et al., 2014).

## 2.6 Heating function assessment by slow waves

The presence of waves in the solar atmosphere may not only provide energy for heating the corona, but could also provide us with a tool to seismologically estimate the coronal heating function and the related dissipation coefficients, such as thermal conduction and viscosity (see the review by Wang et al., 2021, this issue). Here we forego that, more importantly, even the most basic property of the magnetized coronal plasma such as the magnetic field strength needed for any magnetically based heating function estimate is difficult to determine directly, and in some cases can only be estimated from coronal seismology. However, we keep this subject for the review of Nakariakov et al. (2021), this issue.

The impact on the dynamics of MHD waves of thermodynamic activity of the corona, i.e. processes of its continuous cooling via the optically thin radiation and thermal conduction, and resupply of energy by some yet unknown heating mechanism, was recently investigated by Nakariakov et al. (2017); Claes and Keppens (2019); Kolotkov et al. (2019, 2020). This allows for developing a new approach for a remote diagnostics of thermodynamic properties of the corona, including processes of its cooling and heating, by coronal seismology. For example, additional restrictions on the coronal heating mechanism can be obtained via accounting for perturbations of the thermal equilibrium of the corona by compressive, e.g. slow magnetoacoustic, waves. Indeed, assuming the plasma heating and cooling processes are some different functions of the plasma thermodynamic parameters, i.e. density and temperature, and potentially of the magnetic field too, both of them can be perturbed by the waves. Such a wave-caused destabilisation of the initial thermal equilibrium leads to the onset of a *heating/cooling imbalance* acting as an additional natural mechanism for the energy exchange between the plasma and the wave.

Kolotkov et al. (2019) showed that it is convenient to use specific thermal imbalance time scales  $\tau_1$  and  $\tau_2$  connected to the rates of change of the net energy gain  $H(\rho, T)$ , and loss  $L(\rho, T)$  including radiative cooling and field-aligned thermal conduction, through the function  $Q(\rho, T) = L - H$  with the plasma density  $\rho$  and temperature  $T$ ,  $Q_T \equiv (\partial Q / \partial T)_\rho$  and  $Q_\rho \equiv (\partial Q / \partial \rho)_T$ , as  $\tau_1 = \gamma C_V / [Q_T - (\rho_0 / T_0) Q_\rho]$

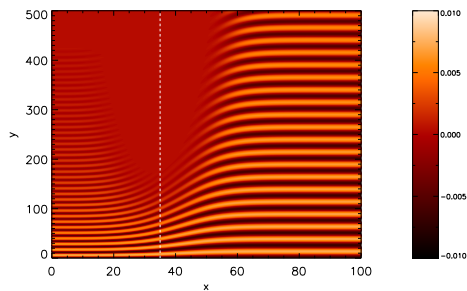


**Fig. 7** Dependence of the oscillation quality factor  $q$  on the density and temperature power indices used for parametrising the heating function as  $H(\rho, T) \propto \rho^a T^b$ , for the following values of the equilibrium parameters of the plasma:  $T_0 = 6.3 \times 10^6$  K,  $\rho_0 = 10^{-11}$  kg m $^{-3}$ , loop length  $L = 180 \times 10^6$  m, Spitzer conductivity  $\kappa = 10^{-11} T_0^{5/2}$  W m $^{-1}$  K $^{-1}$ , mean particle mass  $m = 0.6 \times 1.67 \times 10^{-27}$  kg,  $k_B = 1.38 \times 10^{-23}$  m $^2$  kg s $^{-1}$  K $^{-1}$ , and  $\gamma = 5/3$ . The black and red contours show the regimes of damping (positive  $q$ ) and amplification (negative  $q$ ), respectively. The blue-shaded region shows values of  $a$  and  $b$  where the time scales of the heating/cooling misbalance  $\tau_1$  and  $\tau_2$  become negative, for which other thermal instabilities may occur (see Field, 1965). The hatched region shows values of  $q < 2$  for slow-mode oscillations detected in observations (Nakariakov et al., 2019). The yellow-shaded region outlines heating models which are stable to thermal instability and for which  $q < 2$ . Figure modified from Kolotkov et al. (2019).

and  $\tau_2 = C_V/Q_T$  with  $C_V$  being the specific heat capacity. With this, the dispersion relation for linear slow waves describes the evolution of two acoustic and one thermal (entropy-related) modes. The 3rd order dispersion relation can be solved numerically for the real,  $\omega_R$ , and imaginary,  $\omega_I$ , parts of a complex frequency  $\omega$ , while allowing the value of  $\omega_I$  to be comparable to  $\omega_R$ . The  $q$ -factor (also known as quality factor) is computed as  $q = \tau_D/P$ , using the oscillation period  $P = 2\pi\omega_R^{-1}$  and damping time  $\tau_D = \omega_I^{-1}$ .

Using the radiative cooling  $L(\rho, T)$  from the CHIANTI atomic database (Dere et al., 1997, 2019), and a parametrised heating function  $H(\rho, T) \propto \rho^a T^b$ , Kolotkov et al. (2019) compute numerically the oscillation quality factor  $q$  as a function of the heating indices  $a$  and  $b$  and for the equilibrium parameters corresponding to hot and dense post-flare coronal loops. Direct comparison of the values of  $q$  shown in Fig. 7 with those usually seen in observations of slow magnetoacoustic oscillations of coronal loops (see e.g. Nakariakov et al., 2019, for the most recent statistical survey) by e.g. SOHO/SUMER and Yohkoh/BCS,





**Fig. 8** Snapshot of Alfvén wave velocity component out of the plane, for a periodic driver on the bottom boundary. The figure displays the turning of the wave fronts due to phase mixing in the middle region with the largest variation of the Alfvén speed, and the associated phase mixing damping in the region where the turning is the strongest, is indicated with the vertical white dashed line. Figure taken from McLaughlin et al. (2011).

shows that the heating models with  $a$  and  $b$  approximately delineated by a triangle with vertices  $(-3.5, -4)$ ,  $(0, -0.5)$ , and  $(5, -4)$  in Fig. 7, excluding the regions of the thermal mode instability, could be responsible for the observed rapid damping of slow waves in the corona (Wang, 2011). Thus, the proof-of-concept of Kolotkov et al. (2019) show that slow waves can indeed serve to put limits on (power indices of) the coronal heating function.

The discussed misbalance between heating and cooling processes in plasma can cause additional phase shifts between density and temperature perturbations in slow waves, thus affecting, for example, estimates of the effective polytropic index. In particular, Zavershinskii et al. (2019) demonstrated analytically that the polytropic index, a coefficient linking the slow wave phase speed with the plasma temperature, can vary non-monotonically with temperature due to the effect of the thermal misbalance, so that it deviates from the adiabatic value  $5/3$  to 1.4-3.2. This can be a natural cause for higher values of the polytropic index at hotter plasma temperatures observed by Krishna Prasad et al. (2018), that cannot be explained by the classical Spitzer thermal conduction. Implication of these theoretical results for probing the corona is a promising future research avenue.

### 3 Models

#### 3.1 Phase mixing models

As already pointed out by Cowling (1953) and Piddington (1956), classical resistive or viscous dissipation of the Alfvén wave energy is not efficient in a homogeneous magnetized plasma and this slow dissipation rate remains a key obstacle in more advanced present day wave-based heating models (see e.g. Arregui, 2015; Cargill et al., 2016). The main problem is to rapidly transfer the wave energy from large to small length scales, where (classical) dissipation is effective. The concept of phase mixing as described by Heyvaerts and Priest (1983) aims to enhance this dissipation rate through the creation of small length scales in an inhomogeneous medium. Phase mixing occurs when a local gradient in the Alfvén speed is present; as waves propagate along field lines with different Alfvén speeds, the wave front

turns and the waves become increasingly out of phase. This is shown graphically in Fig. 8, displaying results of McLaughlin et al. (2011). This process generates increasingly smaller length scales (across the background magnetic field) and hence, more efficient dissipation. Although resonant absorption and phase mixing are often discussed as individual mechanisms, there is a natural link between these mechanisms, as both rely on the presence of a variation in the local Alfvén speed profile (Soler and Terradas, 2015). Hence, the small-scale oscillations in the resonant layer will naturally undergo phase mixing due to local variation in the Alfvén speed (see e.g. Ruderman et al., 1997a,b). However, the damping caused by phase mixing depends on the actual value of the resistivity, while the damping of resonant absorption does not (as resonant absorption itself is an ideal process). An extensive body of literature on both resonant absorption and phase mixing exist, for which we refer the interested reader to reviews by e.g. Aschwanden (2004); Goedbloed and Poedts (2004); Goossens et al. (2011).

Most theoretical (including computational) studies of phase mixing start from an equilibrium setup where a pre-existing profile in the Alfvén speed is present. Most often, this setup consists of a uniform background magnetic field, where a gradient in the density is balanced by a temperature variation to maintain pressure balance. Waves are then considered as perturbations of this equilibrium or injected through boundary driving. The process of phase mixing will lead to the most efficient dissipation of the Alfvén waves (and hence strongest heating) where the gradient in the density (Alfvén speed) profile is steepest.

The self-consistency of heating by phase mixing of Alfvén waves was investigated in more detail by Cargill et al. (2016) by analysing the evolution of the density profile. These authors showed that although phase mixing increases the efficiency of the wave energy dissipation where gradients in the local Alfvén speed occur, the resulting heating in this basic model cannot self-consistently sustain the required density profile in closed loops. As the local density in closed loops is related to the magnitude of the heating (see e.g. Klimchuk, 2006; Reale, 2014), the phase mixing heating profile is not consistent with the heating profile to sustain the density profile. Cargill et al. (2016) also investigated whether feedback of the heating on the density profile through evaporation would be able to modify the local density (see also Ofman et al., 1998). Although some local structuring of the density profile occurred, it only happened on timescales longer than the cooling and draining timescales and hence, does not help address the efficiency problem of wave-heating. In addition, the authors point out that transport coefficients need to be substantially enhanced to obtain effective heating in the first place. Using MHD simulations including thermal conduction and optically thin radiation, Van Damme et al. (2020) for the first time modelled the feedback process through evaporation entirely self-consistently (i.e. without the use of scaling laws) and also found that Alfvén wave phase mixing only leads to modest heating in the shell regions of the loop, where the mass increase through evaporation is not sufficient to modify the phase mixing process.

If the imposed density structure is not compatible with the heating profile resulting from phase mixing, how then is this assumed equilibrium structure supported? Is an alternative heating mechanism present that is compatible with the density structuring? And if so, does that immediately imply that the wave-based heating (through phase mixing) is comparatively small?

In addition to requiring the presence of a variation in the local Alfvén speed profile, the phase mixing model as it was originally introduced by Heyvaerts and Priest (1983) implies the presence of an ignorable coordinate, a setup which might not be representative of the highly inhomogeneous solar atmosphere (Parker, 1991; Ofman and Davila, 1995), although approximately similar conditions may occur in coronal holes.

Pagano and De Moortel (2017) investigated the heating by phase mixing in a 3D numerical model of a boundary-driven flux tube. The flux tube is modelled as a cylindrical density enhancement in a uniform magnetic field and transverse displacements of the footpoint of the cylinder generate kink modes which, as they propagate along the flux tube, couple to azimuthally polarised Alfvén modes in the boundary shell of the cylindrical flux tube. Due to the density gradient in the inhomogeneous boundary layer, the Alfvén waves phase mix but, even using (excessively) large values of magnetic resistivity and large-amplitude footpoint driving, the heating due to phase mixing was found to be insufficient to be relevant for coronal heating (i.e. to balance the expected losses through radiation and conduction), a conclusion similar to the remark made by Cargill et al. (2016) about the need to substantially enhance transport coefficients. By varying parameters such as the length of the non-uniform layer, the density structure, and the persistence of the driver, Pagano and De Moortel (2017) find that phase mixing of these propagating waves leads to temperature increases of the order of  $10^5\text{K}$  or less, a figure that is in agreement with the analytical estimate by Terradas and Arregui (2018), even though these were for standing waves.

When simulations are performed using 3 observed coronal loop oscillation harmonics as input, Pagano et al. (2018) found that the presence of these multiple harmonics causes drifting of the location of the heating. Still, the mechanism did not seem to provide enough energy to maintain the full thermal structure constrained by the observed coronal properties, and the multiple harmonics inhibited the formation of small scales. Pagano and De Moortel (2019) included an observed spectrum of transverse waves, using a boundary driver which consists of a series of 1000 superimposed random pulses was used drawn from a reconstructed spectrum. The results again indicate that it is unlikely that phase mixing of Alfvén waves generated by the observed power spectrum heats coronal loops, although, the waves could be important in the generation of small scales.

## 3.2 Alfvén wave heating models

### 3.2.1 Alfvén wave induced shock heating

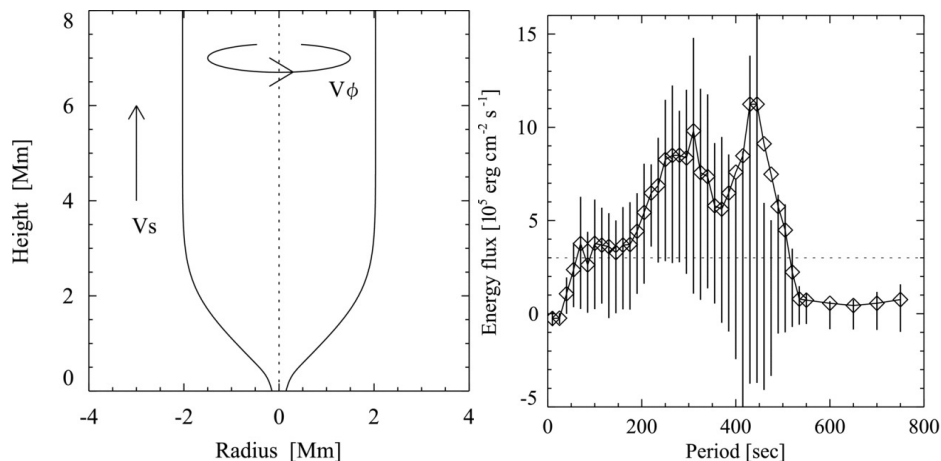
Alfvén waves have long been particularly attractive coronal heating candidates due to their ability to carry large amounts of energy throughout the solar atmosphere (Alfvén, 1947; Uchida and Kaburaki, 1974) and can potentially also lead to solar wind acceleration (Hollweg, 1990; Ofman, 2010). The Poynting flux upward from convective motions in magnetic concentrations at photospheric level is expected to be on the order of  $10^6\text{ W m}^{-2}$  (Parnell and De Moortel, 2012), although the strong magnetic expansion in the upper layers leads to an effective Poynting flux of  $10^4\text{ W m}^{-2}$  into the chromosphere. The ion-neutral friction due to the partial ionisation of the plasma in the chromosphere strongly damps the Alfvén waves,

in particular the high-frequency spectrum. Combined with reflection, these effects lead to only a 1–3 % effective transmission rate into the corona (Soler et al., 2017, 2019), similar to estimated footpoint leakage of coronal waves (De Pontieu et al., 2001). Overall, the energy budget from torsional Alfvén waves generated in the photosphere is estimated to be on the order of  $10^2 \text{ W m}^{-2}$  in the corona, which is just enough for the quiet Sun or coronal hole. The double mode conversion process from p-mode waves into Alfvénic waves in the chromosphere and transition region is expected to contribute similar energy rates (Morton et al., 2019).

Various models for Alfvén wave propagation in the solar atmosphere have a different nature depending on the region and wave guide under consideration. The geometry of the waves has been selected to be either planar (a.k.a linear, e.g., Suzuki and Inutsuka, 2005; Murawski and Musielak, 2010) or azimuthal (a.k.a circular, e.g., Zhugzhda, 1996; Vasheghani Farahani et al., 2010; Wójcik et al., 2017). For instance Alfvén wave propagation of waves with linear polarisation may be more appropriate in the relatively diffuse coronal holes, while the circular polarisation may be more applicable for the propagation in structures showing strong density contrast, such as solar jets, spicules, tornadoes, and loops (Vasheghani Farahani et al., 2011).

Alfvén waves need an efficient dissipation mechanism in order to play a dominant role in coronal heating. A first successful dissipative model was based on nonlinear mode conversion of these waves into compressive modes (evolving into shocks) due to the flux tube expansion (and associated centrifugal force) and the ponderomotive force (Hollweg et al., 1982; Lau and Siregar, 1996; Ofman and Davila, 1998; Antolin and Shibata, 2010). This idea has persisted through the decades thanks to the accompanying ability to generate spicule-like excursions of material into the corona (Kudoh and Shibata, 1999; Matsumoto and Shibata, 2010; Arber et al., 2016; Brady and Arber, 2016) and accelerate the solar wind (Matsumoto and Suzuki, 2014; Suzuki and Inutsuka, 2006). Furthermore, this model has demonstrated that waves can lead to small nanoflare-like intensity bursts during dissipation (Moriyasu et al., 2004; Antolin et al., 2008), thus placing caution when interpreting observations of these events or associating the nanoflare term solely to reconnection-based models. Although highly self-consistent in its ability to explain various features of the solar atmosphere, this model relies on the presence of density fluctuations, and sufficiently large transverse wave fluctuations (compared to the local Alfvén speed) for the relevant nonlinear effects to become important. A natural question is whether this matches observations and the answer yet unknown. Parker Solar Probe does indicate, however, that the density fluctuations in the open corona is far greater than previously thought (Bale et al., 2019).

A well established model is that of Suzuki and Inutsuka (2005) who describe the propagation of a low frequency Alfvén wave in coronal holes from the photosphere to an altitude of 0.3AU. The granular motion of the photosphere results in steady transverse motions perturbing the magnetic field lines and exciting Alfvén waves (Cranmer and van Ballegoijen, 2005). The 1D model provided by Suzuki and Inutsuka (2005) resembles a superradial open magnetic flux tube conserving magnetic flux, where the expansion is a two step superradial function with the use of two expansion factors. Their choice for a two step superradial function was due to the height dependence of the magnetic field strength reconstructed by Tu et al. (2005). They included the effect of field line curvature, radiative cooling and



**Fig. 9** Left: Sketch on the configuration of Alfvén wave heating models. Right: Alfvén wave energy flux as a function of period. The figures are taken from Matsumoto and Shibata (2010).

thermal conduction in the MHD equations. The solutions to these MHD equations enabled Suzuki and Inutsuka (2005) to compute the variations of the radial and tangential speeds together with the temperature and density as a function of altitude (see Fig. 9 for a sketch of the configuration). The results proved adequate for atmospheric heating due to two effects; the first stage of heating is due to the dissipation of low frequency Alfvén waves mainly heating the inner solar atmosphere, while the second stage of heating is due to the induction of compressive perturbations (especially slow waves) due to the nonlinear effects connected with the Alfvén wave propagation that causes wave steepening ending up in shock formation that mainly contributes towards coronal heating. The nonlinear effects connected with outward propagating Alfvén waves that experience shocks contributes in two ways; the first aspect is the heating due to the increase of wave amplitudes that is confirmed by the non-thermal broadening of the emission lines, the second aspect is the creation of shocks which rapidly dissipates the waves. The contribution of the second aspect towards heating is greater than the first aspect (Nakariakov et al., 2000). As a matter of fact, the efficiency of damping and hence heating due to low frequency Alfvén waves also depends on the activity of the region. In particular, the damping of surface Alfvén waves occurs on a shorter scale in active regions compared to quiet solar regions. This means that in quiet regions, the surface Alfvén wave is able to contribute towards heating the corona at higher altitudes (Evans et al., 2009). In addition, the period of the Alfvén wave itself is key in determining its contribution to coronal heating. This statement is backed by the simulations of Matsumoto and Shibata (2010) where nonlinear Alfvén waves were driven by photospheric convection towards the transition region in the presence of gravity and empirical chromospheric cooling. Their model showed that the region bounded between the photosphere and the transition region acts as a resonant cavity, a fact that has been recently observed above sunspots for the first time (Jess et al., 2019). It can be readily noticed from the right panel of Fig. 9 that waves with periods between 100 s to 500 s are able to transport flux to the corona, and that the maximum energy flux is carried when the period of the Alfvén wave

is around 400s coinciding with the resonant frequencies in the cavity (Matsumoto and Shibata, 2010).

Coronal resonances of Alfvén wave propagating in solar loops have also been reported in the model proposed by Antolin and Shibata (2010). The loop is a gravitationally stratified semitorus, with magnetic field expansion, similar to the left panel of Fig. 9. The advantage of this model is that it sheds light on the efficiency of heating taking into account the loop geometry in which Alfvén waves propagate. This enabled Antolin and Shibata (2010) to state that Alfvén waves provide efficient and uniform heating when propagating in thick loops where the area expansion between the photosphere and corona is greater than 2.5 orders of magnitude with lengths at least as long as 80 Mm. Since in the solar quiet regions the loops are both longer and wider compared to loops in active regions, the efficiency of Alfvén wave heating in quiet solar regions is more pronounced compared to active regions. Regarding the period of the waves, Antolin and Shibata (2010) concluded that the shocks connected with long-period waves increase the average temperature of the corona, while shocks connected with short-period waves are unable to further heat the corona despite being more numerous (Suzuki and Inutsuka, 2006). The short-period waves are only just strong enough to maintain the coronal temperature. Heating by the resonance cavity with a monochromatic driver matching the eigenfrequency of the loop was found to lead to temperatures close to 5 MK, but the loops were not in a state of thermal equilibrium.

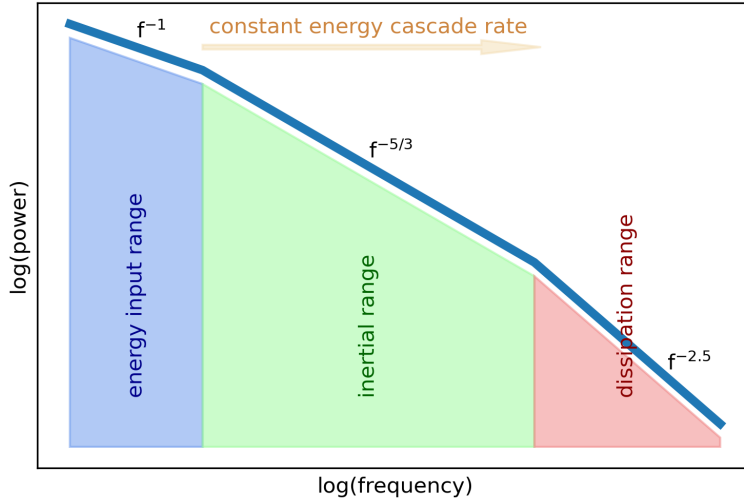
Regarding the contribution of the compressive shocks towards coronal heating, Matsumoto (2016) stated that shock compressive heating is very efficient below the altitude of 4 Mm, while above this height the incompressive heating due to direct dissipation of magnetic and velocity shear in Alfvén waves is dominant. Moreover, Matsumoto and Suzuki (2014) showed that these chromospheric compressive shocks generate curved wedge shaped Alfvén waves, which could play a role in heating the higher layers. Thus, the back reaction of the induced compressive perturbations on the Alfvén wave results in Alfvén wave shocks that also contribute towards coronal heating. The induced compressive perturbations are due to the nonlinear forces connected with Alfvén waves, namely the magnetic tension, centrifugal, and ponderomotive forces. It is worth noting that the ponderomotive coupling of Alfvén waves to slow modes creates shocks that dominates the heating due to resistive dissipation (Arber et al., 2016; Brady and Arber, 2016). The non-linear behaviour of Alfvén waves was described by e.g. Suzuki (2008); Vasheghani Farahani et al. (2011); Suzuki (2012); Vasheghani Farahani and Hejazi (2017). In particular, Vasheghani Farahani et al. (2012) implemented the second order thin flux tube approximation (Zhugzhda, 1996) and studied the parallel nonlinear cascade of torsional and shear Alfvén waves in open magnetic fields. They showed that the shock formation for shear Alfvén waves comes into play earlier than torsional waves in the lower solar atmosphere.

Another mechanism playing a role in chromospheric heating is Ohmic diffusion and ion-neutral collisions which strongly affects torsional Alfvén waves during their propagation in the chromosphere (Soler et al., 2019; Wójcik et al., 2020) and leads to heating. In any case, the chromosphere plays a crucial role for coronal heating, because of the resulting evaporation of material due to coronal heating and thus providing the mass source. The localised heating could result in thread structuring in the corona (Copil et al., 2008), which is in contradiction with the recent results of Cargill et al. (2016); Van Damme et al. (2020).

### 3.2.2 Alfvén wave turbulence heating

Turbulent heating models have gained popularity recently in the context of coronal heating (see the review by Bruno and Carbone, 2013, of this mechanism in the solar wind context). However, there is still no direct evidence that the corona is turbulent. This might change in the near future thanks to the Parker Solar Probe, which could confirm turbulence at heights around or below the Alfvén critical point. Still, the non-thermal broadening of the coronal spectral lines could already be indicative of turbulent fluctuations (Banerjee et al., 1998; Singh et al., 2006; Hahn and Savin, 2013, 2014). More indirect evidence is present in the CoMP observations through the measurement of a  $1/f$  spectrum in closed loops (Morton et al., 2016, 2019). Turbulent heating models are best categorized as wave or alternative-current (AC) mechanisms in the limit of weak turbulence, as the turbulent energy cascade is thought to be generated by nonlinear (self) interactions of waves. The underlying idea of energy conversion is similar to other wave-based heating mechanisms: increasingly smaller length scales are created, until dissipation becomes important and converts kinetic and magnetic energy into heat. The main difference compared to other mechanisms is that in turbulence small scales are created nonlinearly (unlike in phase mixing, resonant absorption, etc.), producing an energy cascade to smaller scales (although, in some scenarios inverse cascade can also take place). We differentiate three main scales or ranges in turbulence, as depicted schematically in Fig. 10. The largest scale is the energy containing scale, at which the forcing of the plasma takes place, e.g. the size of convective cells in the photosphere (depicted in blue in Fig. 10). The inertial range is an intermediate scale where the actual energy cascade is initiated. The dynamics are self-similar and independent of both the nature of forcing and dissipation (shown in green in Fig. 10), expected to correspond to Kolmogorov power law indices of  $-5/3$ . Lastly, at scales where dissipative terms are on the order of advective terms (Reynolds and/or magnetic Reynolds numbers  $\approx 1$ ), turbulence enters the dissipation range, where heat is generated (assuming collisional dissipation), displayed with the red zone in Fig. 10. In this last range, the power law index depends on the particular dissipation mechanism (e.g. electron or proton dissipation) that is considered, growing ever steeper.

The most researched turbulence-generating wave interaction is that of counter-propagating pure Alfvén waves in the incompressible limit. In this scenario, the Alfvén wave wavefronts are deformed in successive collisions, leading to a cascade towards higher wavenumbers (see Figure 11). In the corona, counter-propagating transverse or Alfvénic waves can exist in both closed structures, such as coronal loops, and open structures, due to wave reflection. Wave reflection occurs when the Alfvén speed varies along the propagation direction, i.e. along the background magnetic field, linearly coupling the outward and inward-propagating Alfvén waves (Leroy, 1980; Hollweg and Isenberg, 2007). Alfvén speed variations along the field exist in the corona because of gravitational stratification of the plasma, and the spherical/dipolar expansion of the magnetic field with height. In the turbulent heating models, the source of input energy is usually the convective flows in the photosphere, which generate waves and eventually turbulence by shuffling the magnetic field lines. There are numerous models of coronal heating based on turbulence for both coronal loops (van Ballegoijen et al., 2011; Downs et al., 2016; van Ballegoijen et al., 2017), and open structures (Perez and Chandran, 2013; Woolsey



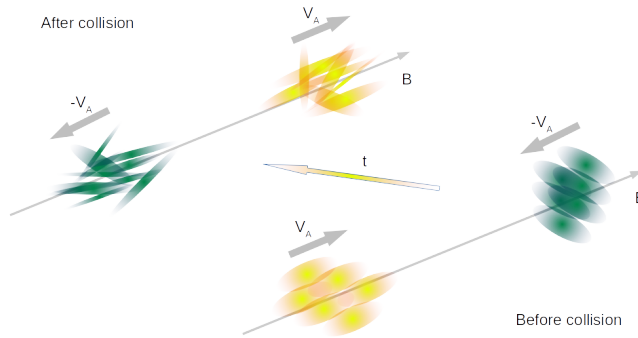
**Fig. 10** A schematic graph of the power law behaviour of turbulent fluctuations in the solar atmosphere and wind. The left, blue range shows the energy input range with a power law index of -1. The middle, green range shows the inertial range with a power law index of  $-5/3$ , where the energy cascade rate is independent of the scale. The right, red range shows the dissipation range, where the ever steeper power law slope depends on the specific dissipation process.

and Cranmer, 2015; Chandran and Perez, 2019), and also global models (van der Holst et al., 2014; Oran et al., 2017). The models for Alfvén wave heating of active regions (van Ballegoijen and Asgari-Targhi, 2018) show that temperatures reach maximally 2.5 MK, and that other heating mechanisms are needed to go beyond those temperatures.

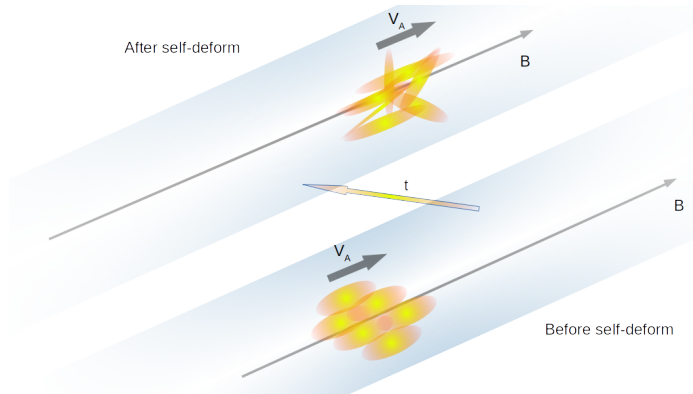
The ‘local’ models mostly use a reduced MHD treatment, which neglects density perturbations (i.e., are incompressible) and transverse inhomogeneities in the plasma, among other simplifications. For the global models, Alfvén wave equations are employed in van der Holst et al. (2014), containing heavily approximated terms for reflection and turbulent dissipation, and Reynolds-averaged mean flow equations with turbulent transport in Usmanov et al. (2018). All these models conclude that a multi-million K corona can be maintained by turbulent heating, while balancing radiative cooling and conductive losses. A common discrepancy between turbulent heating models and observed properties of the corona is the excessive non-thermal line broadening that results from the models (Brooks and Warren, 2016).

Recently, it was realized that the existence of counterpropagating waves is not the only way to generate turbulence (Magyar et al., 2017, 2019). In the presence of transverse inhomogeneities, propagating Alfvénic waves can nonlinearly self-deform, generating a cascade to smaller scales, called uniturbulence (see Figure 12). This can constitute an additional channel towards a turbulent cascade and can





**Fig. 11** Illustrating the mutual deformation of two counter-propagating Alfvénic wave-packets along some background magnetic field  $\mathbf{B}$ . The undisturbed wave-packets must collectively vary along both perpendicular directions for nonlinear interaction to occur (Howes and Nielson, 2013), depicted by the different orientation of the ellipsoid making up the packets. These ellipsoids can be considered isosurfaces of velocity perturbations. After the collision (on the upper left), the wave-packets are mutually deformed, leading to ellipsoids scattered to higher wavenumbers, i.e. appearing thinner.



**Fig. 12** Same as in Figure 11, but having only the wave-packet propagating parallel to the magnetic field. The background plasma is inhomogeneous across the field. This is causing the initial Alfvénic wave-package to self-deform nonlinearly as it propagates, leading to elongated ellipsoids, i.e. cascading to higher wavenumbers.

potentially enhance the dissipation rate, leading to more heating. However, there are no models of coronal heating incorporating the effects of uniturbulence, as of yet. Still, forward modelling of simulations with uniturbulence (Pant et al., 2019) can elegantly and self-consistently explain the observed correlation between wave Doppler shift and spectral line broadening (McIntosh and De Pontieu, 2012, as also explained in Nakariakov et al., 2021).

Full 2.5D and 3D MHD models are now available (e.g. Dahlburg et al., 2012; Shoda et al., 2019) that take into account both the nonlinear Alfvén wave heating via compressive effects, and the Alfvén wave turbulence, and initial results seem to

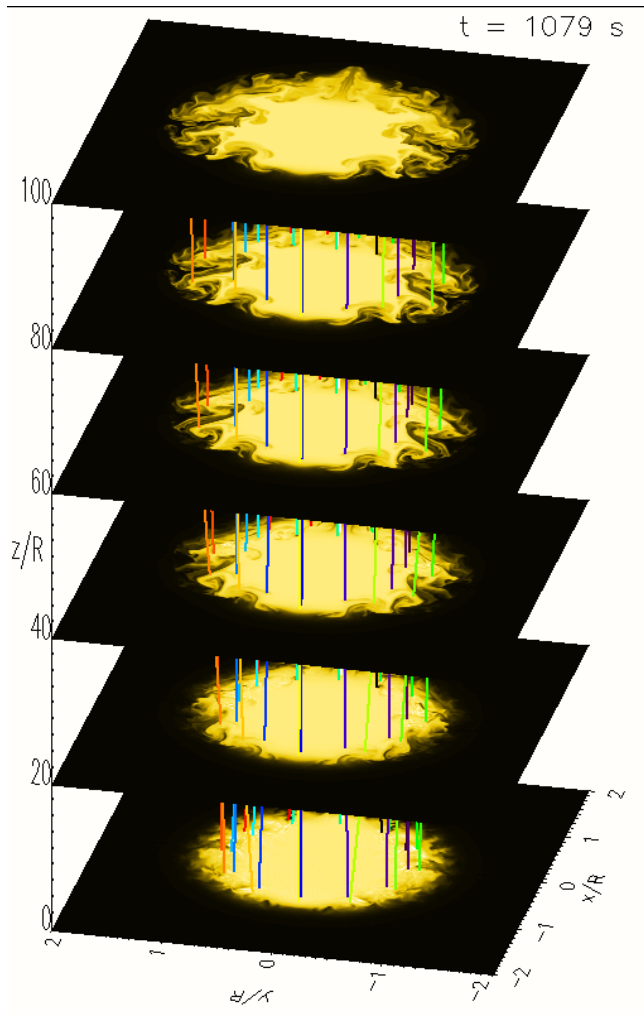
point to the dominance of Alfvén wave turbulence over the compressive heating in the corona, while the opposite is true at the lower heights of the magnetic canopy (Matsumoto, 2016, 2018). Since these models target quiet Sun conditions for the loops it is not yet clear whether the same holds for the denser and more dynamic active region loop conditions.

To date, all Alfvén wave heating models have been mostly successful at generating and sustaining a lower energy budget corona as in the quiet Sun or coronal holes, while they all seem to fall short of the  $10^4 \text{ W m}^{-2}$  average heating rate needed for active region coronal loops (see chapter 6.1 Hinode Review Team et al., 2019, for a more thorough discussion). In particular, the hot loops at the core of active regions with temperatures of 5 MK or more seem to be unexplained by wave models in general (van Ballegoijen and Asgari-Targhi, 2018). Furthermore, these models seem to generate preferentially uniformly heated coronae in line with the RTV scaling law (Rosner et al., 1978), rather than footpoint heating. In turn, Alfvén wave heating models do not seem able to explain thermal non-equilibrium and the associated coronal rain (Antolin et al., 2010). Comparison of results from the Alfvén wave turbulence model with *Hinode*/EIS observations of active region loops indicates that longitudinal flows are an important ingredient, suggesting that either compressive effects may become important or that a different mechanism is present (Asgari-Targhi et al., 2014). It is important to note, however, that the very demanding computational requirements needed in fully consistent wave models strongly limit the current predictions (see section 4)

### 3.3 Kink-mode driven turbulent heating models

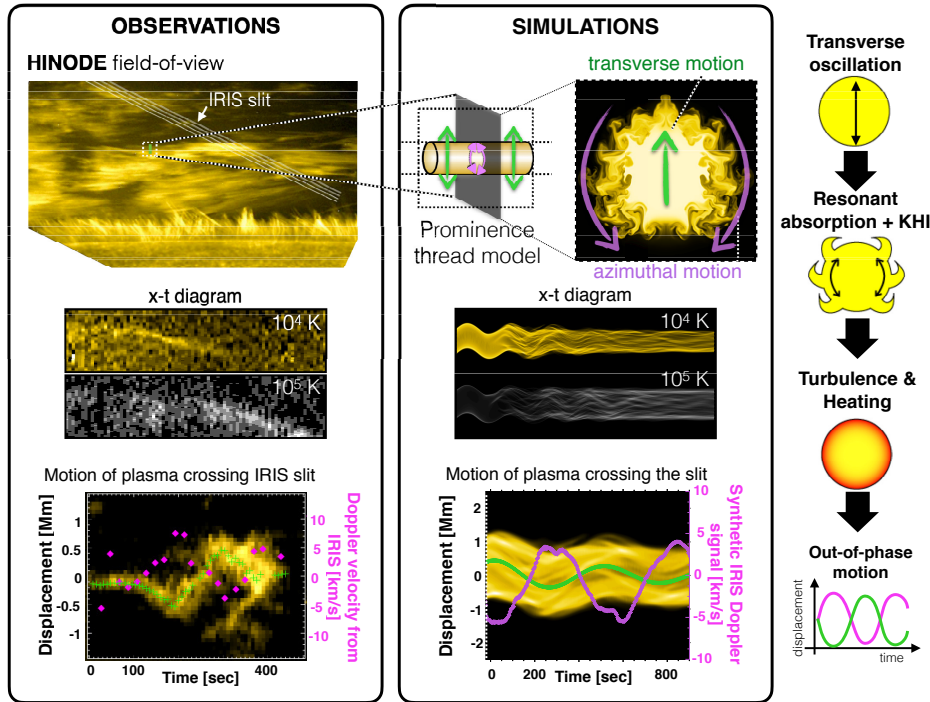
Standing transverse waves can be considered as superposition of counterpropagating waves, thus these can generate a turbulent cascade as well. In closed loops, initial perturbations such as flares, low coronal eruptions or shock waves can easily excite standing kink oscillations. Due to the shear motions between the loops and external corona, the Kelvin-Helmholtz instability can thus be induced near the loop boundary (Terradas et al., 2008a; Antolin et al., 2014, 2017; Magyar et al., 2015). Moreover, the generation of azimuthally polarised Alfvén waves due to resonant absorption increases the velocity shear with the external plasma, which can also enhance the instability (Antolin and Van Doorselaere, 2019). The effect of the instability is to generate transverse wave induced Kelvin-Helmholtz rolls (TWIKH rolls), extended along the magnetic field, as shown in Fig. 13. The wave energy can dissipate efficiently if the turbulent structures are sufficiently developed. Direct comparison of such a model with observations of a prominence (Okamoto et al., 2015; Antolin et al., 2015), gives an indication that the emission is indeed shifting from a temperature of  $10^4 \text{ K}$  to  $10^5 \text{ K}$  after the passing of the transverse wave, in accordance with the numerical model (see Fig. 14). Recent studies by Antolin and Van Doorselaere (2019) revealed that resonant absorption plays a key role in energizing and spreading the TWIKH rolls throughout a coronal loop.

The most basic setup that was used was a cylindrical loop with an initial velocity pulse, setting up a damped standing wave. This setup was used to show that the non-linearly developing KHI introduces an amplitude dependent damping (Magyar and Van Doorselaere, 2016), which matches reasonably well with observations (Goddard et al., 2016a). As intuitively understood, the magnetic twist provides a



**Fig. 13** A tomography of TWIKH rolls. Cross-sections of density (in yellow) are shown at different locations along half the length of a prominence oscillating with a standing kink mode after roughly 2 periods. The coloured lines correspond to selected magnetic field lines traced from the bottom. The TWIKH rolls drag the field lines, generating twisting and strong changes in magnetic field pressure in a wide layer around the boundary. The simulation corresponds to the high resolution run discussed in Antolin et al. (2015).

stabilising effect (Howson et al., 2017a; Terradas et al., 2018), which delays the development of the instability without completely suppressing it. This corresponds well with the predictions from analytical models (Hillier et al., 2019; Barbulescu et al., 2019). Moreover, the stabilising effect of viscosity and resistivity was investigated numerically (Howson et al., 2017b; Karampelas et al., 2019a). However, as explained in Sec. 2.1, simple calculations using basic estimates show that the directly observed standing waves in the solar corona do not seem to contain sufficient energy for heating it.



**Fig. 14** Evidence for resonant absorption and heating in a prominence. The left column provides a set of observables obtained with coordinated observations (top panel) between Hinode/SOT and IRIS of an active region prominence off-limb. (Left-middle) Prominence threads were seen oscillating transversely and fading in the Ca II H line of SOT ( $10^4$  K) and subsequently appearing in the hotter SJI 1400 channel of IRIS (dominated by Si IV emission at  $10^{4.8}$  K approximately). (Left-bottom) The prominence threads oscillate in the POS (yellow with green curve) out-of-phase with the Doppler velocity in Si IV captured by the IRIS slit (purple). The right column shows the forward modelling of a numerical simulation of a prominence thread with the observed characteristics. The thread oscillates transversely with a kink mode and triggers the KHI at the boundary (top-right). Resonant absorption is initially highly localised in the boundary, which fuels the KHI. TWIKH rolls are excited, whose dynamics reflect the resonant absorption and phase mixing dynamics but at a larger, observable scale. The TWIKH rolls mix the cold prominence plasma with the hot coronal surroundings and widen the boundary of the loop. A turbulent cascade is established which leads to wave dissipation and heating. As the prominence plasma is heated, its emission in the synthesised Ca II H line fades out and becomes stronger in the hotter Si IV line (right-middle). The resonant absorption and phase mixing dynamics become observable due to the KHI, leading to an out-of-phase relation between the POS motion of the thread and the Doppler velocity of the heated prominence plasma. A very good match is thus obtained with the observations. A sketch of the observed physical processes is given on the right. Adapted from Okamoto et al. (2015) and Antolin et al. (2015).

It was soon realised that the TWIKH rolls could play an important role if waves are driven at a loop footpoint. In that configuration, the TWIKH rolls provide an elegant mechanism to move the energy from the input scales, to the smaller length scales of the inertial range, and on to the dissipation scales at which the plasma is heated, just as Alfvén wave turbulence would do. This damping mechanism in the inertial range is independent of transport coefficients. In doing so, the energy

cascade balances the input energy, creating a (statistically) steady state, indirectly feeding the driving energy into plasma heating. The steady state that is obtained in the numerical models could be a potential model for the observed decayless observations.

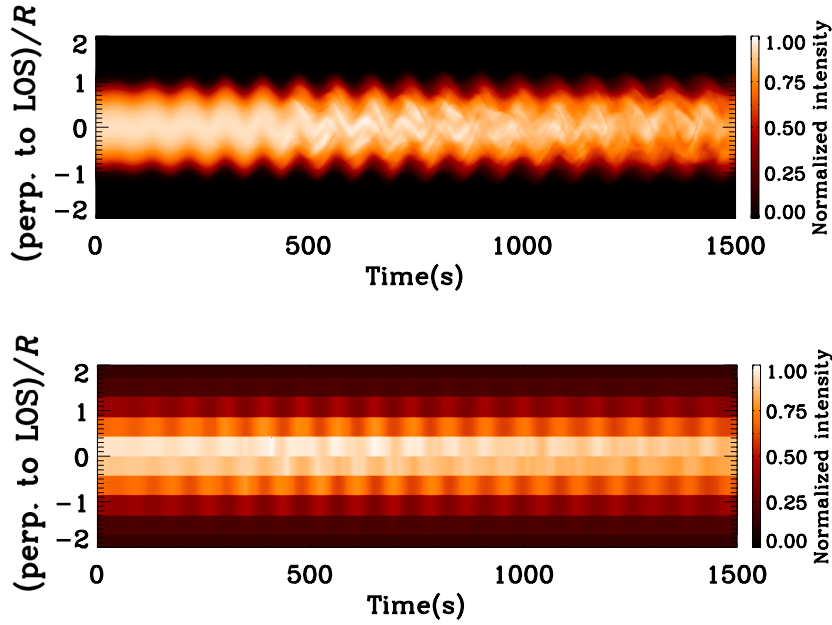
In the setup with the footpoint driver in a closed loop, Karampelas and Van Doorselaere (2018) obtained a fully deformed loop cross-section. Although the turbulence significantly changes the initial equilibrium, the loop structure can still be observed in forward models, meaning that turbulent loops probably exist in the real solar corona. Further studies (Karampelas et al., 2019a) considering gravity in a loop, stressed the importance of longitudinal stratification, which improves the efficiency of wave heating. The TWIKH roll formation dependence on the driver frequency was investigated by Afanasyev et al. (2019), who subsequently also considered the driving with a turbulent spectrum (Afanasyev et al., 2020).

Considering the turbulent motions at the footpoint of a coronal loop anchored in the photosphere, Guo et al. (2019b) employed a mixed transverse and torsional driver at the loop footpoint, going beyond the implicitly excited Alfvén waves in the simulations of Pascoe et al. (2011). Comparing with a pure kink driven loop and a pure torsional driven loop, they found that the KHI eddies are fully developed in the whole loop cross-section and that internal energy and temperature in the mixed driven loop are higher. This means that the mixed modes lead to a more efficient dissipation in the turbulent state of plasma and that the KHI acts as an agent to dissipate energy in both wave modes. In addition, forward models showed very similar images to the observations of decayless oscillations. This means that the ubiquitous decayless oscillations could play an important role in coronal heating. However, as is shown in Figure 15, due to the limited resolution of instruments, neither Alfvén modes nor the fine structures are observable. This means that although difficult to capture, Alfvén modes probably can coexist with kink modes, leading to enhanced heating.

A further study by Guo et al. (2019a) examined how such a mixed mode driver affects a tightly packed multi-stranded loop. By depositing almost identical input energy flux at the footpoint of a multi-stranded loop and a density equivalent monolithic loop, Guo et al. (2019a) found that the multi-stranded loop is more efficient in starting the heating process due to the quickly established turbulent state in this model.

Again using a model with footpoint driven loops, Karampelas et al. (2019b) computed the dependence of the wave amplitude as they would be observed from forward modelling, on the driver amplitude. They found that there is only a weak dependence between both. Thus, they showed that the amplitude of the decayless waves is actually an unreliable measure of the wave energy that is being dissipated in the solar corona, as studied in more detail by Hillier et al. (2020). Karampelas et al. (2019b) concluded that the spectral line broadening is a much more accurate quantity to give a measure of the wave energy that is being dissipated. This may influence assessments of energy content and flux of standing or propagating kink waves (as e.g. in Sec. 2.1).

Even though these models seem promising, at the time of submission, there is no published paper in which the non-linearly evolving, footpoint-driven transverse waves can compensate the radiative or thermal conduction cooling of the coronal plasma in a self-consistent model, contrary to DC heating models of the solar corona (e.g. Hansteen et al., 2015). But, it should be noted that the 3D MHD DC



**Fig. 15** Forward-modelling results for the numerical models in the Fe IX 171 Å line at the apex with an LOS angle of 45°. The upper row is obtained with the full numerical resolution and the lower row with a degraded resolution comparable to SDO/AIA. Figure taken from Guo et al. (2019b).

models usually employ unrealistically high resistivity and viscosity, which are the sources for the heating in them.

#### 4 Critical Assessment & Conclusions

This review provides an overview of the progress made in (roughly) the last decade in observations and models of wave heating in the solar corona. A lot of progress has been made in wave-based heating mechanisms using a combination of advanced high-resolution satellite and ground-based solar observations, and advances in computational MHD modeling.

From an observational point of view, we now have detailed observations of several wave modes that could play a role in heating the corona. Recent multi-wavelength studies of coronal loops have not found evidence of any significant heating following large-amplitude kink oscillations (Goddard and Nisticò, 2020; Pascoe et al., 2020). However, decayless kink oscillations and quasi-periodic propagating fast waves could potentially account for coronal losses in certain regions. We now have several observational characterisations of the wave energy content in the solar corona, based on imaging, spectroscopy or spectropolarimetry. In the chromosphere, a very large energy flux is found in waves, and if even only a fraction of that is dissipated in the corona, it is heated efficiently. In the corona itself, wave observations find energy fluxes comparable to the required heating rate, but also one or two orders of magnitude below it, particularly in the case of active regions.

This wide disparity in observational estimates of coronal wave energy points to a variety of wave activity manifestations, and probably indicates that the issue of coronal wave energy requires further study. The latter point is also underlined by the discrepancy between the energy flux in numerical models and their forward modelling (De Moortel and Pascoe, 2012; Van Doorselaere et al., 2014; Karampelas et al., 2019b).

From the modelling point of view, the computational models have been lifted to a new level in recent years thanks to advancement in computational power. Now, 3D MHD simulations are the norm. In addition to previously considered AC heating mechanisms by non-linear Alfvén waves, these 3D MHD simulations show that turbulence and development of small scales is important. Simulations of Alfvén wave turbulence in (perpendicularly) uniform plasmas are able to maintain coronal temperatures, even in 3D configurations. In order to take into account the perpendicular density structuring, studies have focused on phase mixing and the transverse wave induced Kelvin-Helmholtz instability. Despite the strong effort in these last two subjects, still no self-consistent simulation exists in which a density enhanced coronal loop is maintained against cooling by radiation or conduction, with resolved wave energy flux from the photosphere.

Self-consistent wave modelling studies are extremely demanding in computational power. The photospheric source (or sub-photospheric), the chromosphere (rich in wave processes due to its high- to low- $\beta$  variable conditions), the transition region (in which the Alfvén speed steepens leading to reflection, refraction and mode conversion) and the corona (in which small density inhomogeneities and wave-to-wave interaction are important) need to be included in the model. In addition, the resolution needs to be high enough to allow wave-associated instabilities and the turbulent spectrum to set in with the inertial range established for at least a decade in wave number. Through the decades, these limitations have favoured the investigation of wave dissipation in waveguides that are already well-defined (such as coronal loops) without the connection to other atmospheric layers (the latter is only recently changing, e.g. Van Damme et al., 2020). Although limiting, this approach has led to an essential categorisation of wave processes and wave dissipation locally, and to phase relations between observables for a direct comparison with high resolution observations (Hinode Review Team et al., 2019, chapter 6.1). It remains to be seen how these models connect to more advanced models of wave propagation in the lower atmosphere (e.g. Felipe et al., 2011).

This approach has also allowed to investigate the relative importance of specific wave mechanisms and the available energy at the coronal base (e.g. Soler et al., 2019). Improvements in numerical techniques and increased computation power are coming close to allowing self-consistent modelling which incorporates all the relevant wave processes in a large scale model (such as a whole active region). This would allow to fully account for nonlinear processes and, in particular, global observables of wave heating models for an easier comparison with observations.

These recent developments have made it clear that the omnipresent coronal waves also strongly influence DC heating models.

Firstly, due to the observed continuous influx of Alfvénic waves into the corona, it is expected that the resulting heating is more continuous and less impulsive than that obtained from magnetic reconnection alone. This long-standing assumption is only true if waves and reconnection act in a sufficiently independent way from each other. However, we can think of scenarios in which one facilitates the other. For

instance, reconnection-based nanoflares in the corona are based on the braiding scenario, through which the magnetic field is stressed to a certain degree before releasing these stresses through component (small-angle) reconnection, thus leading to impulsive, middle to low-frequency events (see chapter 6.2 in Hinode Review Team et al., 2019). Moreover, transverse wave induced Kelvin-Helmholtz rolls (see Sec. 3.3) create local twists and small-angle misalignments between the strands and, as in the magnetopause (Nykyri and Otto, 2004), magnetic reconnection is expected. In this scenario, the heating from reconnection is expected to be impulsive and act only when the KHI is triggered. Although twists delay the formation of the KHI, they do not inhibit the instability (see Sec. 3.3). Further investigation of this scenario is therefore needed.

Secondly, DC heating models are often based on stranded loop models, in which each magnetic field line is modelled independently from each other (Reale, 2014). The turbulence appearing in Alfvén wave and kink wave models of loops are very efficient at mixing plasma perpendicular to the magnetic field (Magyar and Van Doorselaere, 2016). This mixing induces adiabatic expansion and contraction of plasma elements, leading to (apparent) cooling and heating on particular field lines, which is not taken into account if they are completely decoupled. Moreover, additional magnetic pressure enhancements are introduced, leading to a restructuring of the plasma in the single fieldline models.

Thirdly, the nonlinearly induced perturbations due to Alfvén waves are not restricted to funnels and flux tubes with transverse or parallel structuring, but also feature in magnetic reconnection sites when Alfvén waves interact with a magnetic null point. As the Alfvén wave nears the magnetic null-point it induces magnetoacoustic waves which in turn contribute towards heating at the null point (Galsgaard et al., 2003; Thurgood and McLaughlin, 2013; Sabri et al., 2018). The fast and slow magnetoacoustic waves experience shocks in the vicinity of the null-point leading to enhanced dissipation there (McLaughlin et al., 2009; Sabri et al., 2018). Thus, despite the Alfvén wave being unable to reach the null point while travelling along the separatrices, their coupling to the magnetoacoustic waves provides an agent to their gradual dissipation and contribution towards heating near X-points (McLaughlin and Hood, 2004, 2006).

Overall, we conclude this review with the following one-liner: Motivated by plentiful recent observations of coronal waves, AC heating models have taken a leap forward in recent years, but have not yet managed to self-consistently maintain loops at the observed million degree temperatures. These models make it worthwhile to have a renewed look at DC heating models while including the cross-field effects induced by wave dynamics.

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