

Tectonic predictions with mantle convection models

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Abstract

Over the past 15 years, numerical models of convection in Earth's mantle have made a leap forward: they can now produce self-consistent plate-like behaviour at the surface together with deep mantle circulation. These digital tools provide a new window into the intimate connections between plate tectonics and mantle dynamics, and can therefore be used for tectonic predictions, in principle. This contribution explores this assumption. Firstly, initial conditions at 30, 20, 10 and 0 Ma are generated by driving a convective flow with imposed plate velocities at the surface. We then compute instantaneous mantle flows in response to the guessed temperature fields without imposing any boundary conditions. Plate boundaries self-consistently emerge at correct locations with respect to reconstructions, except for small plates close to subduction zones. As already observed for other types of instantaneous flow calculations, the structure of the top boundary layer and upper mantle slab is the dominant character that leads to accurate predictions of surface velocities. Perturbations of the rheological parameters have little impact on the resulting surface velocities. We then compute fully dynamic model evolution from 30 and 10 Ma to 0 Ma, without imposing plate boundaries or plate velocities. Contrary to instantaneous calculations, errors in kinematic predictions are substantial, although the plate layout and kinematics in several areas remain consistent with the expectations for the Earth. For these calculations, varying the rheological parameters makes a difference for plate boundary evolution. Also, identified errors in initial conditions contribute to first-order kinematic errors. This experiment shows the tectonic predictions of dynamic models over 10 My are highly sensitive to uncertainties of rheological parameters

and initial temperature field in comparison to instantaneous flow calculations. Indeed, the initial conditions and the rheological parameters can be good enough for an accurate prediction of instantaneous flow, but not for a prediction after 10 My of evolution. Therefore, inverse methods (sequential or data assimilation methods) using short term fully dynamic evolution that predict surface kinematics are promising tools for a better understanding of the state of the Earth's mantle.

1 INTRODUCTION

In the theory of plate tectonics, the surface of the Earth is assumed to be divided into perfectly rigid plates, such that sufficient geologic observations combined with geometric principles describe a coherent kinematic state. However, this revolutionary theory is not dynamic, hence it cannot be used to predict future and past states of the planet for which observations are too sparse or absent. Reconstructing past tectonics is therefore a difficult task (Gurnis et al. 2012), especially in areas where geological observations are lacking. For instance, 50% of the world's present-day ocean floor is younger than 55 Ma, and a large fraction of the Pacific Ocean had disappeared prior to 60 Ma (Rowley 2008). Interpretation of mantle seismic tomography can provide additional constraints, but the assumptions used still require testing (Van Der Meer et al. 2010; Domeier et al. 2016). Unfortunately, even quantifying forces acting on plates today (Forsyth and Uyeda 1975) does not give access to how plate boundaries are generated and evolve. Analysing the plate velocity in tectonic reconstructions, for instance in terms of toroidal-poloidal partitioning brings more questions on the origins of plate velocity changes (Lithgow-Bertelloni et al. 1993).

As a consequence, dynamic models are needed to fill observational gaps. They can also handle diffuse deformation, extending the concept of plate tectonics beyond that of pure rigidity. These models consider that the plates and mantle constitute a single complex system (Bercovici 2003). Over the past 20 years, numerical models of mantle convection have improved significantly through a better description of the rheology of the lithosphere (Trompert and Hansen 1998; Moresi and Solomatov 1998; Tackley 1998). The level of precision and **sophistication** is not at that of regional lithospheric models, but already allows for the localisation of stress and strain in narrow regions surrounding stiff and coherent areas. The pseudo-plastic approximation produces plate-like behaviour self-consistently over a restricted range of parameters (Van Heck and Tackley 2008; Foley and Becker 2009). Such models reveal the dynamic origin of some fundamental properties of plate tectonics on Earth at the present-day, such as the size-distribution of plates (Mallard et al. 2016) and the seafloor age vs. area

28 distribution (Coltice et al. 2012, 2013). However, their potential for tectonic predictions and
29 reconstruction remains unexploited. Only Yoshida (2014) has explored the conditions required
30 for Pangea breakup, with limited success. Indeed, uncertainties in the initial temperature field
31 200 My ago together with the intrinsic limit of predictability of mantle convection (Bello et al.
32 2014) restrict the possibility to realistically simulate the breakup of Pangea.

33 The following work presents tectonic predictions of instantaneous and dynamic evolution
34 of 3D spherical models of convection with plate-like behaviour. The goal is to explore the
35 conditions of these models to reproduce plate boundaries and surface velocities of the Earth.
36 Model errors and uncertainties on initial conditions play different roles whether instantaneous
37 or dynamic predictions are considered.

38 **2 METHOD**

39 In this section, we detail how we generate the predictions of tectonic structures and kinemat-
40 ics (see also flow chart in Fig. 1). We use 3D spherical models of mantle convection with
41 plate-like behaviour, but at lower convective vigour than the mantle so it can be computa-
42 tionally tractable. First, we produce a guess of the thermal evolution of the mantle through
43 imposing plate motions at the surface of the model. Then, we compute instantaneous and
44 time-dependent flows starting from the guessed thermal states, without imposing any addi-
45 tional plate structure. Then we analyse the deformation at the surface of the models in terms
46 of plate boundaries and kinematics.

47 **2.1 Physical and numerical model**

48 We model the evolution of temperature, pressure and flow velocity in the Earth's mantle by an
49 approximation of its dynamics. Numerical solutions of the equations of conservation of mass,
50 momentum and energy, and advection of material properties are computed, together with a
51 pseudo-plastic rheology and a Boussinesq approximation for the equation of state. The physics
52 of phase changes, compressibility, melting, and deep dense chemical anomalies are neglected
53 and the rheology is simplified. Such a model is already at the limit of current computational
54 capabilities. Computing the guess of the thermal evolution, once parameters were fixed, took
55 about two months on a supercomputer.

56 We use the code StagYY (Tackley 2008) to solve the set of equations in a 3D spherical
57 geometry over a Yin-Yang grid (Kageyama and Sato 2004). StagYY handles several orders
58 of magnitude of viscosity contrasts between adjacent nodes (Tackley 2008) and has been

59 benchmarked for pseudo-plasticity in 2D (Tosi et al. 2015). The average resolution is 30 km,
 60 refined in the vertical direction close to boundary layers of up to 10 km, the lateral resolution
 61 being 35 km at the surface and 19 km at the core-mantle boundary. Improving the average
 62 resolution to 20 km produced consistent results in the dynamic predictions over 30 My of
 63 evolution. Viscosity increases with depth by a factor of 20 according to an activation volume.
 64 We impose a viscosity jump by a factor of 30 at 660 km, consistent with the viscosity structure
 65 of the Earth inferred from geoid anomalies (Ricard et al. 1993). An additional viscosity increase
 66 at around 1000 km depth has been proposed (Rudolph et al. 2015) but is not incorporated
 67 here. Uncertainties in the radial viscosity structure translate into errors in the modeling of
 68 deep mantle heterogeneity, especially in the sinking rate of slabs.

Viscosity is temperature-dependent:

$$\eta(z, T) = \eta_0(z) \exp\left(\frac{E_a}{RT}\right),$$

69 with an activation energy E_a of 142 kJ mol⁻¹. R is the gas constant and T the absolute
 70 dimensional temperature. Accounting for the full complexity of mantle rheology (King 2016)
 71 in such 3D spherical models is a computational challenge, since extreme viscosity contrasts
 72 are difficult to resolve accurately.

73 The non-dimensional reference viscosity of 1 corresponds to a non-dimensional temper-
 74 ature of 0.64 at zero pressure. This value is chosen before the calculation is realised such as
 75 to correspond to the expected temperature at the base of the upper boundary layer. We set
 76 a cut-off for the maximum value of the non-dimensional viscosity at 10⁴ to limit viscosity
 77 variations. As a consequence, the viscosity contrast across the upper boundary layer is ex-
 78 pected to be 10⁴, before the calculation is performed. After the calculation, the average value
 79 of the non-dimensional temperature at the base of the upper boundary layer is 0.75, i.e.
 80 hotter than expected a priori. However, it is stable in the initial stage without imposed plate
 81 motions and in the stage with imposed plate motions (see next subsection). Hence, the typical
 82 non-dimensional viscosity in the upper mantle (except in slabs) is around 10⁻¹ as seen from
 83 Fig. 2.

84 We consider a stress dependence of the viscosity through a pseudo-plastic approximation
 85 in order to produce plate boundaries surrounding strong plate interiors (see for instance Rolf
 86 et al. 2012). This choice leads to stiff slabs and one-sided subduction with imposed plate
 87 kinematics, as described by Bello et al. (2015). Viscosity also depends on the type of material,
 88 which is tracked with markers. We use three types of materials. Ambient mantle corresponds
 89 to the largest fraction of the spherical shell. Continental nuclei are 175 km thick, approximat-

90 ing continental shields (Fig. 3.) They are buoyant, with their buoyancy number being -0.4
 91 (200 kg m^{-3} lighter than underlying mantle). They are 100 times more viscous than ambient
 92 mantle and their non-dimensional yield stress is 10 times larger than ambient mantle. The
 93 continental lithosphere that immediately surrounds the continent nuclei are 115 km thick and
 94 their buoyancy number is -0.3 (150 kg m^{-3} lighter than underlying mantle). They are 50
 95 times more viscous than underlying mantle and they have a 10 times larger yield stress. The
 96 Tibetan region of Eurasia, prior to collision, is similarly thick and buoyant as the surrounding
 97 belts. This specific continental block is modelled here by 50 times more viscous material but
 98 2.5 times larger yield stress than ambient mantle. The goal here is to parameterise efficient
 99 ductile deformation during the collision (Zhang et al. 2004). The physical parameters of the
 100 model are listed in Table 1.

101

102 The solution is computed with an energy contribution from the core of 25% of the total
 103 surface heat flux, the rest being internal heating. Both the surface and the bottom are isother-
 104 mal, defining the temperature drop for the Rayleigh number Ra of 10^6 , based on the reference
 105 viscosity defined above. The effective Rayleigh number based on averaged viscosity is here
 106 $5.9 \cdot 10^6$. The average surface velocity obtained with these physical parameters at statistical
 107 steady-state, without imposing surface velocities, is 1.2 cm y^{-1} when scaled with a thermal
 108 diffusivity of $10^{-6} \text{ m}^2 \text{ s}^{-1}$. This is a factor of three lower than the Earth today. Unfortunately,
 109 computational cost limits the study to a lower Ra than that which would produce Earth-like
 110 velocities. Since convective velocities are proportional to $Ra^{2/3}$, this factor of three suggests
 111 that increasing Ra by a factor of 5 would generate appropriate Earth-like velocities with our
 112 approximation and keeping our dimensional value of thermal diffusivity. Another consequence
 113 of our low Rayleigh number is that convective structures are larger than for the Earth. The
 114 dimensional time is then scaled: dimensional velocities produced by the model are multiplied
 115 by three and the model time is divided by three, so that the values of velocities and time/age
 116 can directly be compared to the Earth for practical purposes.

117

118 2.2 Building guessed temperature fields with a convection reconstruction

119 The goal here is to build guessed temperature fields at 30, 20, 10 and 0 Ma using a numerical
 120 model of convection and plate reconstructions as information on the state of the mantle
 121 today and in the past. We use the methodology explained in more detail in Coltice et al.
 122 (2017) and illustrated in the flow chart (Fig. 1): (Step 1) we build a temperature field for the

123 continent configuration at 200 Ma based on free convection with imposed and fixed continent
 124 configuration, (Step 2) we impose plate velocities as boundary conditions of the numerical
 125 model between 200 Ma and 30 Ma, 20 Ma, 10 Ma and 0 Ma in increments of 1 My, updating
 126 the continent shapes at 80 Ma to account for the moderate changes which happened in terms
 127 of continental growth and deformation (Fig. 3). We use the plate reconstructions of Seton
 128 et al. (2012), but since we performed the computations presented here, Müller et al. (2016)
 129 have published updates and improvements. Because convection in our model is less vigorous
 130 than on Earth, the imposed velocities at present-day are scaled to be consistent with the
 131 convective vigour of our model (Bello et al. 2015): the rms value of imposed present-day
 132 velocities equals the rms surface velocity of the model without imposed kinematics. Imposing
 133 plate motion history generates artificial stresses at the surface, contrary to more realistic
 134 free slip boundary conditions (Lowman 2011). A 3D snapshot of the thermal state of the
 135 reconstruction at 0 Ma is depicted in Fig. 4.

136 In the following paragraphs, we compare the lateral temperature anomalies of the convec-
 137 tion model at present-day to seismic anomalies in tomographic models. Such a comparison is
 138 limited because seismic velocity is dependent on the local mineralogy and not directly on the
 139 temperature. Our model does not explicitly take into account for phase equilibria, melting and
 140 variable mantle chemistry. Therefore, comparisons are hazardous in the transition zone where
 141 water and phases changes contribute substantially (Tauzin et al. 2013, for instance), and close
 142 to the core mantle boundary regions with **broad regions of seismic velocity anomalies**
 143 **resulting from a combination of thermal and compositional effects** (Garnero et al.
 144 2016). Considering these issues, we first compare the power spectrum of the tomographic
 145 model S40RTS (Ritsema et al. 2011) to that of the power spectrum of the temperature field
 146 of our convection model at present-day. The choice of S40RTS is somewhat arbitrary, but it
 147 captures the essential characters of the power spectrum we can discuss here, that are found
 148 in other models (Becker and Boschi 2002). The resolution of the convection model is sub-
 149 stantially finer than that of S40RTS (by more than a factor of 10), and therefore we refer to
 150 Coltice et al. (2017) for a discussion of structures of wavelength smaller than 1000 km i.e.
 151 harmonic degree >40 . Both power spectra show strong degree two, strong degrees < 10 in
 152 the upper mantle, and weak heterogeneity in the lower mantle. The principal disagreements
 153 we can interpret are the deepest mantle and the transition zone (see Fig. 5). Indeed, the
 154 convection model does not involve deep chemical anomalies that are suspected to generate
 155 a strong seismic signature in the lower 1000 km of the mantle (Garnero et al. 2016, for a
 156 review). The convection model does not account for phase changes, mineralogical complexity

157 (Nakagawa et al. 2012) and the water cycle (Richard et al. 2002), that would all otherwise
 158 produce seismic anomalies in the transition zone. In the spectrum of the convection model,
 159 the temperature field displays a substantially long wavelength peak around 1500 km depth,
 160 which corresponds to **the region** where slabs start to fold and accumulate. This feature could
 161 change if we would take compressibility and phase transitions into account.

162 We compare the location of slabs in the convection model to fast seismic anomalies in
 163 tomographic models. But tomographic models substantially differ: some are based on *S*-wave,
 164 some on *P*-waves which have different thermal sensitivities; they use different 1D reference
 165 model, seismic sources, seismograms and picking of phases in seismograms; some use finite-
 166 frequency approximation and some ray theory only; they use different inversion domain
 167 decompositions, methods and parameterisations **of the physics**. Therefore, we use the vote
 168 map description of Shephard et al. (2017), for fast and slow seismic anomalies. The number
 169 of votes at a given location corresponds to the number of models in which a seismic velocity
 170 anomaly faster than the average of fast anomalies at a given depth is present. Shephard
 171 et al. (2017) described a method for fast seismic anomalies, which we extend to slow velocity
 172 anomalies. As a consequence, this tool provides the robust features of 14 tomographic models,
 173 seven for *P*-waves (Montelli et al. 2006; Amaru 2007; Houser et al. 2008; Simmons et al. 2010,
 174 2012; Burdick et al. 2012; Obayashi et al. 2013), and seven for *S*-waves (Grand 2002; Montelli
 175 et al. 2006; Houser et al. 2008; Simmons et al. 2010; Ritsema et al. 2011; Auer et al. 2014;
 176 French and Romanowicz 2014).

177 Fig. 6 shows horizontal slices at depths of 500, 1500 and 2500 km. At 500 km, robust
 178 fast anomalies corresponds to the cold sinking slabs in the convection model. Some robust
 179 cold anomalies beneath Africa do not correspond to strong cold features in the convection
 180 model. The slow robust anomalies which are not associated with plumes do not correspond
 181 to any features in the convection model. One possibility is that the slow features represent
 182 chemical heterogeneities. At 1500 km deep, the agreement between robust fast anomalies and
 183 cold slabs is weaker. For instance, below North America, the position of the Farallon slab
 184 in the model is ~ 1000 km west of that in the vote map. This is a common feature of such
 185 convection models, in which low angle subduction is sometimes difficult to **obtain** (Bunge and
 186 Grand 2000). Another source of error can come from the radial viscosity distribution in our
 187 model, because it dictates how fast slabs sink in the lower mantle (Butterworth et al. 2014).
 188 At 2500 km depth, the disagreement is stronger. At this depth, the model lacks chemical
 189 heterogeneity, which is thought to be the source of the large slow velocity provinces, clearly
 190 seen on the corresponding vote map. The deepest structure in the convection model suffers

191 the most from the approximation in initial conditions, hypothesis of incompressibility, and
 192 from uncertainties of past subduction locations in plate reconstructions.

193 Fig. 7 shows cross-sections for the Farallon, Tonga and Tethyan slabs. The Farallon slab is
 194 continuous in the convection model, but its dip angle seems to low compared to the vote map
 195 of fast anomalies. Therefore, the convection model predicts an erroneous cold structure below
 196 North America and East Atlantic in the lower mantle. The Tonga slab shows some similar
 197 patterns in both the convection model and vote maps of fast anomalies. However, the slab
 198 is chopped off in different pieces in the convection model, and sinks as isolated chunks. We
 199 attribute this artefact to the method of imposing plate motions. Imposing velocities at the
 200 surface of convection models violates the free slip constraint, generating tangential stresses at
 201 the boundary (Nettelfield and Lowman 2007). These velocity gradients can break up down-
 202 wellings into several pieces at the trench, especially in intra-oceanic domain because both
 203 sides of the subduction can yield (Bello et al. 2015). Below India, the Tethyan slab in the
 204 convection model **winds round** up as expected from the vote map of fast anomalies. The
 205 slow seismic anomalies restricted to the transition zone do not correspond to hot anomalies
 206 in the convection model.

207 Overall, the computed temperature fields involve intrinsic errors. **Convection structures**
 208 **are too thick (by a factor of 2) because of the convective vigour being lower than**
 209 **that of the Earth. Also, the geometry of slabs is consistent with tomography**
 210 **models in the upper mantle but at first-order only, because of artificial break-**
 211 **offs. The position of slabs is less accurate, relative to that of tomographic models,**
 212 **as the depth increases. The location of plumes in the numerical solution does not**
 213 **necessarily correspond to hotspots on Earth (see Fig. 8) because plumes emerge**
 214 **freely from the basal boundary layer without a priori constraint. To finish with,**
 215 **the deep mantle thermal structure keeps a memory of the initial temperature**
 216 **field chosen at 200 Ma, which is uncertain.** Errors therefore come from uncertainties
 217 and approximation of (1) the physics of the model, (2) initial conditions and (3) imposed
 218 plate kinematics. Therefore, we limit the prediction time frame to 30 My.

219 **2.3 Instantaneous and dynamic predictions**

220 We compute instantaneous flows in response to the guessed temperature fields provided by the
 221 convection reconstruction. We do not impose mechanically any pre-existing plate boundaries
 222 or surface velocities. Continents are the only pre-existing structures that exist in the models.
 223 In the relevant models, a 15 km weak crust at the surface of the ocean floor may also be

224 incorporated. The weak crust is constantly created and disappears when it sinks into the
 225 mantle below 300 km depth. The viscosity and yield stress of the weak crust are 10 times
 226 lower than that of ambient mantle (see Table 1). It approximates hydrothermally altered
 227 rocks that are softer because of the presence of hydrated silicates like chlorite, amphibole and
 228 serpentine. The viscosity and the yield stress of this layer are set to 0.1 times the values of the
 229 ambient mantle. Such a layer is fundamental to the development of asymmetric subduction
 230 (Gerya et al. 2008; Cramer and Tackley 2014, 2015). It is here thicker than expected on Earth
 231 because the model has a lower Rayleigh number, hence thicker structures.

232 We also compute time-dependent convection evolution forward in time using guessed ther-
 233 mal states at 30 Ma and 10 Ma as initial conditions. The system is chaotic: model and initial
 234 condition errors propagate in time (Bello et al. 2014, 2015). In test cases, Bocher et al. (2016)
 235 showed that the interval between corrections in a sequential data assimilation scheme (using
 236 surface velocities and seafloor age distribution as the data to match) has to be ≤ 15 My for
 237 accurate inversions of the convective temperature field. Therefore we limit the prediction time
 238 frame to 30 My.

239 To study the role of the viscosity parameters, We compute numerical solutions for the
 240 instantaneous and dynamic models for (1) the same **physical** parameters as the convection
 241 reconstruction, (2) the same as the reference but with a lower yield stress (10^4 i.e. 115 MPa in
 242 dimensional units) for ambient mantle, and (3) the same as the reference but with the weak
 243 crust.

To evaluate the quality of the predictions, the viscosity field just below the surface (5 km) is
 compared with the plate boundaries of the plate model used for the convection reconstruction
 (Seton et al. 2012). We also compare the kinematics emerging from the numerical model with
 that of the plate model, computing the mean squared error on the velocity field:

$$MSE = \frac{1}{N} \sum_{i=1}^N \left(\vec{V}(\mathbf{x}_i, T) - \vec{V}_{plates}(\mathbf{x}_i, T) \right) \cdot \left(\vec{V}(\mathbf{x}_i, T) - \vec{V}_{plates}(\mathbf{x}_i, T) \right),$$

244 where N is the number of nodes (414,144), $\vec{V}(\mathbf{x}_i, T)$ the predicted velocity vector at position
 245 \mathbf{x}_i and age T , $\vec{V}_{plates}(\mathbf{x}_i, T)$ the velocity vector in the plate model (Seton et al. 2012). We
 246 note MSE_t the tectonic mean squared error which measures the mean squared difference
 247 between the average velocity and plate velocities. Therefore, it is exactly the mean squared
 248 plate velocity in the no-net rotation reference frame (the average velocity vector being the
 249 null vector).

3 RESULTS

3.1 Instantaneous predictions

We compute instantaneous flows in response to the reconstructed temperature fields at present-day for the three parameterisations of the viscosity described above. Fig. 9 shows the surface viscosity fields and kinematics of the three solutions, compared to the plate tectonic reconstruction at present-day. The three models show plate-like behaviour with 90% of the deformation being concentrated in 11%, 10% and 8% of the surface for the low yield stress, reference and weak crust models, respectively. In the models, the network of very low ($< 10^{-1}$) viscosity bands corresponds to the plate boundaries emerging from the model. In the three models, ridges located away from trenches match the plate reconstructions. But ridges in back-arc basins do not emerge, or not at the right places. The location of trenches is also consistent with those of the Earth when subduction occurs below a continent. Intra-oceanic trenches are less accurately predicted close to New Zealand, Japan and the Caribbean. The model with the weak crust produces the strongest viscosity contrast between plate interiors and boundaries. The model with the low yield stress produces a slightly more diffuse viscosity distribution, because yielding may occur over a broader area of high stresses. Overall, the layout of large plates self-consistently emerges when imposing this temperature field, as long as pseudo-plasticity is introduced with the strong temperature dependence of the viscosity. The layout of small plates does not emerge here, whatever the viscosity parameterisation.

The same figure shows the differences between the predicted and expected plate velocities of Seton et al. (2012). To the first order, the predicted velocity directions and magnitudes are consistent with the expected ones. As shown in Fig. 10, the lower value of MSE/MSE_t is for the model with weak crust, being 0.32 (equivalent to the difference between plate velocities at 10 Ma and at present-day), while it is 0.39 for the low yield stress model and 0.66 for the reference. MSE/MSE_t for instantaneous flows produced with the weak crust model modestly increases with the age of the convection reconstruction within the past 30 My. Some specific plates have systematically lower predicted velocities than expected: the Pacific, Nazca and Indian plates. The model with weak crust produces the highest velocities for these domains. The model with lower yield stress displays the stronger errors on velocity directions (15°) for the Pacific. However, the directions of the Nazca Plate are more accurate for this latter model than the others.

Fig. 8 shows the residual temperature at 370 km depth in the model together with the location of 21 plumes emerging from the reconstructed flow. These plumes emerge at locations

283 that are not imposed and therefore do not necessarily match those on Earth. However,
 284 they often correspond to regions of existing hotspots although the impact of deep chemical
 285 heterogeneities on plume onset is not taken into account. Indeed, the structure of downwellings
 286 already strongly constrains the onset locations of plumes (Davies and Davies 2009). The errors
 287 in the predicted plate boundaries and velocities do not correlate with the presence of plumes
 288 nearby or in terms of the numbers of plumes beneath a plate.

289 3.2 Dynamic flow predictions

290 We compute a dynamic model evolution starting from the convection reconstruction at 10 Ma.
 291 From 10 Ma to 0 Ma, the flow is self-organized and we do not impose any plate boundaries or
 292 tectonic constraints. After 10 My of evolution, Fig. 11 shows the present-day viscosity field at
 293 the surface and the predicted kinematics for the low yield stress model and the model with
 294 weak crust. Both models show ridges at the expected locations except in back arc basins.
 295 The major discrepancy comes from the North Atlantic ridge, which is no longer a ridge after
 296 10 My of evolution, but rather a shear band localising incipient convergence (Fig. 11). The
 297 model with a weak crust still displays the ridges surrounding the Bauer Plate close to the East
 298 Pacific Rise, while they should stop spreading. The Chile Ridge is progressively fading out
 299 in both models. Trenches are located at, or close to the expected locations. Back arc basins
 300 develop in the western Pacific, but with differences in plate boundary locations relative to the
 301 Earth. The plate boundaries in these regions differ from one model to the other, the weak
 302 crust model displaying sharper bands of low viscosity and smaller plates.

303 The kinematics of both models show similar errors in terms of velocity direction and
 304 amplitude for most plates. The direction of the Pacific is off by $<20^\circ$ for both models, but
 305 the model with weak crust predicts faster velocities, which are more consistent with the
 306 observations. The velocities of Africa and Antarctica are larger than expected for the Earth,
 307 especially for the weak crust model. Predicted kinematics for North America is the major issue
 308 of both models. The direction is more than 90° off, leading to a closing of the North Atlantic
 309 ocean basin. It comes from the break off of the slab as seen in the cross section Fig. 12. It
 310 profoundly modifies the kinematics beyond the region whatever the rheological parameters.
 311 The value of MSE/MSE_t at the final time is more than 4 times the initial value (1.2 and
 312 1.87 respectively) for the weak crust model and the low yield stress model respectively.

313 We compute a longer dynamic evolution for the weak crust model, which has the lower
 314 MSE/MSE_t for both the instantaneous and 10 My evolution tests. The numerical solution
 315 corresponds to a free evolution started from the initial condition set by the convection recon-

struction at 30 Ma, as depicted in Fig. 13. Over this time, the predictions of the locations of several plate boundaries degrade quickly. Only the South Atlantic ridge and the South Indian ridges remain precise, moving in the appropriate directions. The Galapagos ridge initiates as expected but further south of the location on Earth. The India-Eurasia collision continues, thanks to the low resistance of the Tibet block, and subduction on the West Pacific operates as well as under South America. However, subduction under North America quickly stops, because of the early break off (between 30 and 20 Ma) of the slab as for the 10 My dynamic evolution. Again, the North Atlantic starts to be in compression after the break off, shutting down the ridge system. Also, the subduction system north and east of Australia retreats fast until it reaches the ocean-continent boundary, instead of remaining at a similar position in the expected plate layout. As for the preceding calculations, back-arc basins are generated with rapidly evolving ridge systems in connection with the moving trench. However, the small plate pattern does not match the expected one on Earth.

The predicted kinematics show a progressive 20° change of direction of the Pacific Plate towards the south, while it is expected to remain constant on Earth. The direction of the Australian Plate also changes direction progressively to reach a 30° offset towards the east, leading to the opening of a ridge system south of Southeast Asia. These changes of directions correlate with the retreat of the trench in the South-East Pacific described above, modifying the force balance on the Pacific and Australian plates that are converging. As for the 10 My evolution, the North American motion is quickly inconsistent with Earth evolution, before changing back again at the end to produce kinematics more consistent with the expectations. However, the relative motion between North America and Eurasia still corresponds to a slowly converging boundary instead of a slowly diverging one. The MSE/MSE_t in Fig. 10 quickly grows as for the 10 My model, and stabilises at about twice its initial value, and 4 times the value of the instantaneous flow calculation at 0 Ma. The change of direction of the Pacific and Australian plates, as well as the incorrect kinematics of North America, produce the early peak of errors because of inaccurate trench evolution (fast retreat in the South East of the Pacific and slab break off under North America).

4 DISCUSSION

In this study, we compute first a reconstruction of convection in the mantle consistent with the physics and approximations used for the subsequent instantaneous and dynamic predictions. Most of the limitations are caused by computational power that is not yet sufficient to reach

348 more realistic parameterizations **of the physics**. From reconstructed thermal fields, we com-
349 pute instantaneous flows where plate boundaries and surface kinematics are not prescribed.

350 The plate layouts emerging from these flows are consistent with the ones expected for
351 the Earth, except close to subduction zones where the plate fragmentation does not produce
352 the observed plate boundaries. A substantial decrease of the yield stress or a weak crust at
353 the surface of the ocean floor have a minor impact on the resulting plate configuration. The
354 predicted kinematics follows the same conclusions for the instantaneous models: velocities have
355 directions and magnitudes close to what is expected on Earth. Discrepancies are again related
356 to selected subduction regions: the Pacific and Nazca plates are slower in the prediction than
357 expected, while they are of the correct magnitude elsewhere. Introducing a weak crust speeds
358 up these plates, by reducing the coupling between the sinking and upper plates. The direction
359 of the Nazca Plate can slightly vary with rheological parameters, but by an angle $<30^\circ$. These
360 results are confirmed for instantaneous calculations at 30, 20, 10 and 0 Ma. Therefore, surface
361 kinematics and plate boundary emergence are first order outcomes of the temperature field
362 in these models. The rheological parameters are second order. Extreme perturbations of the
363 rheological parameters used to build the guessed temperature fields would certainly change
364 this result, but would be inconsistent with the approach we develop, which aims at keeping
365 consistent physics for both guessing initial conditions and realizing predictions.

366 A clear observation is that plumes have no influence on the instantaneous kinematics
367 and plate boundaries here. They neither produce erroneous plate boundaries nor alter sur-
368 face kinematics. The viscosity contrast (6 orders of magnitude here) is so large between the
369 surface and hot plumes that in most cases they easily spread below the cold boundary layer,
370 slightly changing their thermal structure without modifying the force balance as proposed by
371 Monnereau et al. (1993).

372 Stadler et al. (2010) and Alisic et al. (2012) worked on models comparable to the ones
373 presented here since they also incorporated strong slabs and large lateral viscosity variations.
374 They proposed similar conclusions: the direction and magnitude of plate velocities remain con-
375 sistent varying the rheological parameters, except for the Nazca Plate and for small plates.
376 These models belong to a larger class of models, which differ from the models presented in
377 this paper because (1) rigid plates or plate boundaries are imposed while they self-consistently
378 emerge in this paper, and (2) the guessed temperature field at present-day derives from conver-
379 sion of seismic anomalies or imposed location of slabs in the interior of the mantle whereas they
380 are outputs of the models here. Within this class of geodynamic models (i.e. imposed mantle
381 initial conditions and/or plate kinematics), substantial differences in rheological parameterisa-

382 tions produce successful kinematic predictions. Ghosh and Holt (2012) predict accurate plate
 383 motions from a guess of the temperature field derived from seismology, taking into account
 384 lateral viscosity variations in the lithosphere and asthenosphere only. Ricard et al. (1989),
 385 Becker and O’Connell (2001) and Conrad and Lithgow-Bertelloni (2002) also predict accu-
 386 rate plate motions without lateral variations of viscosity, and with different types of guessed
 387 density inside the Earth’s mantle (these types of density models correlating with each other
 388 - see (Becker and Boschi 2002)). Becker and O’Connell (2001) showed that plate motions
 389 are mostly sensitive to the structure of the lithosphere and upper mantle slabs. Taking into
 390 account the contribution of lower mantle slabs slightly improves the predictions (Becker and
 391 O’Connell 2001; Conrad and Lithgow-Bertelloni 2002; Alisic et al. 2012). Since all these mod-
 392 els have a diversity of rheological parameters for slabs and the lithosphere, the results agree
 393 with the observation made here that rheology is second order for the instantaneous predictions
 394 of surface velocities.

395 The results from the instantaneous predictions contrast with the dynamical evolution
 396 started from guesses of past temperature fields. The models started at 10 Ma and 30 Ma
 397 display discrepancies in slab evolution that quickly arise within the first 10 My. The trench east
 398 of Australia retreats faster than expected. Considering the presence of continental Zealandia
 399 instead of pure oceanic floor (Mortimer et al. 2017) would certainly impede the retreat. The
 400 subduction under North America breaks off whereas it is expected to persist to the present-day
 401 on Earth. It is certainly artificially generated by the errors in the reconstructed temperature
 402 field because of the recurrent chopping off of slabs by imposing plate velocities at the surface.
 403 The break-off of the Farallon slab, and the low angle of the sinking slab counteract the forces
 404 that drag North America westwards. Therefore, the North Atlantic Ridge starts to localise
 405 incipient convergence. This change of force balance in the East Pacific, combined with the
 406 strong subduction in the west are responsible for the westward motion of the Pacific Plate
 407 instead of being north-westward.

408 The fast growth of errors comes from feedbacks between errors in the initial temperature
 409 field, which are stronger in the lower mantle than the upper mantle, and errors of parameter-
 410 isation **of the physics**. Unfortunately, the initial temperature field contains errors coming
 411 from (1) errors in the initial condition at 200 Ma (Step 1 of the chart flow in Fig. 1), (2) errors
 412 in **physical** parameters used for Step 2 (Fig. 1) since, for instance, slab sinking rate depends
 413 on the radial viscosity structure, and (3) uncertainties in plate reconstructions. As yet, we do
 414 not have a way in which to correct all these issues, which all point the deep mantle as the
 415 major source of errors.

416 The lower mantle is also the region where our parameterisation of convection fails the
 417 most. Indeed, we neglect compressibility, i.e. the decrease of thermal expansivity with pres-
 418 sure (Chopelas and Boehler 1992). When taken into account, it slows down slabs, which are
 419 consequentially more stagnant (Tosi et al. 2013). Another limitation of our models is that
 420 deep chemical heterogeneity is not incorporated. Furthermore, the top of the lower mantle is
 421 also the location of phase transitions. Depending on the density change and Clapeyron slope
 422 of the transitions, **mostly at 660 km depth**, sinking slabs can stagnate and lie for some
 423 time at a phase boundary (Christensen and Yuen 1984; Tackley et al. 1993).

424 **Compared to the instantaneous models, dynamic calculations demonstrate**
 425 **stronger discriminating power for sources of errors in kinematic predictions.**
 426 **Therefore, they have rich potential for inversions of rheology and guessed tem-**
 427 **perature fields, even over short timescales. Indeed, the initial conditions and**
 428 **the rheological parameters can be good enough for an accurate prediction of in-**
 429 **stantaneous flow, but not for a prediction after 10 My of evolution. We suggest**
 430 **here that using inversions of dynamical evolution using surface velocities as data**
 431 **constraints rather than inputs should lead to improved rheologies and resulting**
 432 **mantle flow. Methods like sequential data assimilation (Bocher et al. 2016, 2017)**
 433 **and adjoint-based inversions (Li et al. 2017) are under development for that very**
 434 **purpose.**

435 Nonetheless, the dynamical framework we used has strong limitations. The physics is
 436 approximated since compressibility is not taken into account, and the rheology is empirical
 437 instead of being defined by properties at the mineralogical scale. The vigour of convection
 438 is lower than that of Earth, therefore convective structures are probably about twice larger
 439 than expected for our planet. Increasing the convective vigour could also increase the time-
 440 dependence and the chaotic nature of the flow. Most of these limitations are caused by the
 441 computational cost of the time-dependent calculations. Parallelisation in time could be a
 442 solution (Samuel 2012), however, it is then difficult to simultaneously test a variety of initial
 443 conditions at 200 Ma and parameterisations **of the physics**. With all these simplifications,
 444 the models presented here already generate tectonics consistent at first order with what is
 445 expected, even for the dynamic evolution.

446 5 CONCLUSIONS

447 We compare the tectonic predictions (kinematics and plate boundary locations) of 3D spher-
 448 ical convection models with plate-like behaviour with tectonic reconstructions for the Earth.

449 We show that calculation of instantaneous flows generate plate boundaries and kinematics
450 consistent with what is expected for present-day and in the past, except for small plates close
451 to subduction zones. Perturbing the rheological parameters does not significantly modify the
452 results although a weaker coupling between subducting plates and continents improves the pre-
453 dictions. Lithosphere structure and upper mantle slabs overcome rheological approximations
454 and errors in the temperature field of the lower mantle. Plumes and small scale convection
455 have imperceptible effects on the plate layout and kinematics. The models evolving freely over
456 several tens of million years show a rapid growth of errors. In the models presented here, errors
457 in the guessed past states interact with errors on rheological parameters. These calculations
458 show that short term (10-30 My) dynamical evolution models are more suitable experiments
459 than instantaneous flow calculations for the inversion of the temperature field and rheological
460 parameters. Such methods based on adjoint codes (Li et al. 2017) and bayesian approaches
461 (Bocher et al. 2016, 2017) are under development.

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Table 1. Non dimensional and dimensional parameters of the reference convection model, also used to generate the Rayleigh number.

Parameter	Non dimensional value	Dimensional value
Rayleigh number	10^6	
Heat production rate	20	$4.6 \cdot 10^{-12} \text{ W kg}^{-1}$
Surface temperature	0.12	255 K
Basal temperature	1.12	2390 K
Reference density	1	4400 kg m^{-3}
Thermal expansivity	1	$4.5 \cdot 10^{-5} \text{ K}^{-1}$
Thermal diffusivity	1	$10^{-6} \text{ m}^2 \text{ s}^{-1}$
Thermal conductivity	1	$4 \text{ W m}^{-1} \text{ K}^{-1}$
Reference viscosity	1	10^{23} Pa s
Viscosity jump factor at 660 km	30	
Activation energy	8	142 kJ mol^{-1}
Yield stress at the surface	$2 \cdot 10^4$	230 MPa
Yield stress depth derivative	$2.5 \cdot 10^5$	1030 Pa m^{-1}
Continent nuclei viscosity factor	100	
Continent nuclei yield stress	$2 \cdot 10^5$	2300 MPa
Buoyancy number for continent nuclei	-0.4	
Continent belts viscosity factor	50	
Continent belts yield stress	$2 \cdot 10^5$	2300 MPa
Buoyancy for continent belt	-0.3	
Tibet viscosity factor	50	
Tibet yield stress	$5 \cdot 10^4$	590 MPa
Buoyancy number for Tibet	-0.3	
Weak crust viscosity factor	0.1	
Weak crust yield stress	$2 \cdot 10^3$	23 MPa
Buoyancy number for weak crust	0.	
Maximum viscosity cutoff	10^4	10^{27} Pa s

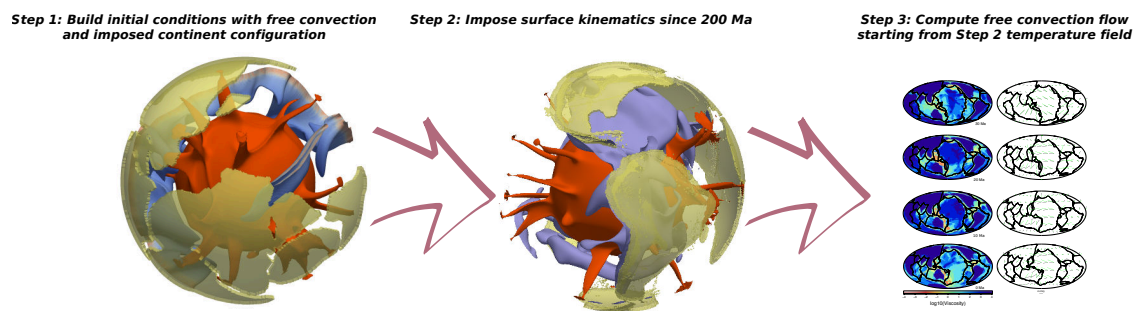


Figure 1. Flow chart of the methodology used to generate the fully dynamic convection flows leading to the tectonic predictions.

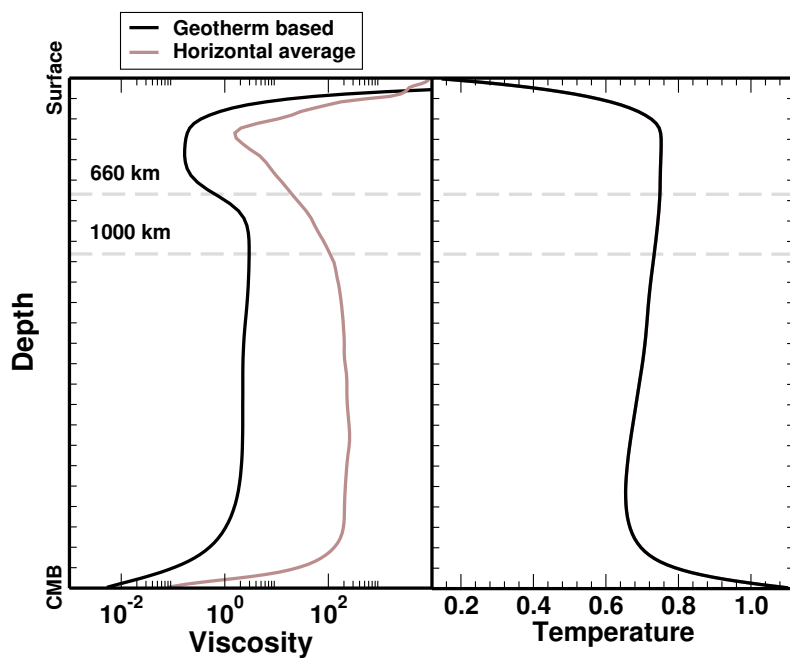


Figure 2. Viscosity (left) and temperature (right) profiles within the final snapshot of the convection model, in non-dimensional units. The viscosity profiles corresponds to that generated by the geotherm on the right, and to the horizontally averaged viscosity of the last snapshot of the convection reconstruction (stiff slabs dominate the average).

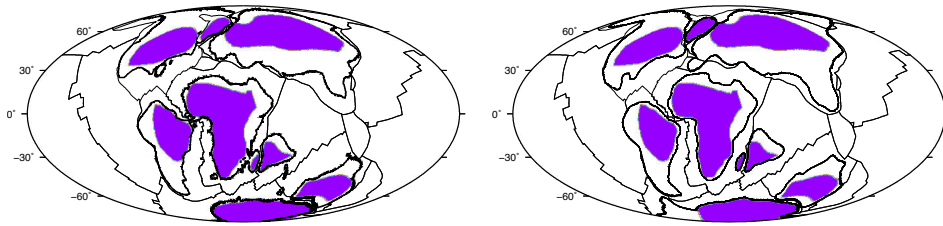


Figure 3. Update of the shape of continents at 80 Ma. Shape of the continent boundaries and continent nuclei (in purple) at 80 Ma before (left) and after (right) the update of their shape.

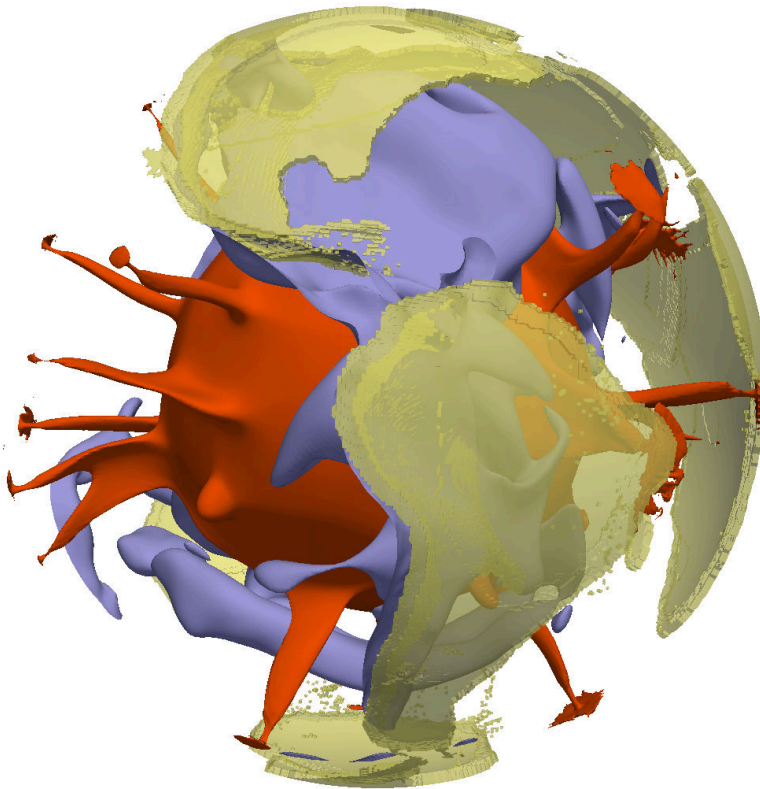


Figure 4. Selected 3D view state of the model corresponding to present-day after Step 2 in the flow chart. Continental material is highlighted in yellow. South America is visible on the front side. The cold isotherm surface in blue (non-dimensional temperature 0.6) allows to visualize downwelling currents. The hot isotherm surface in red (non-dimensional temperature 0.9) shows plumes coming from the base of the model.

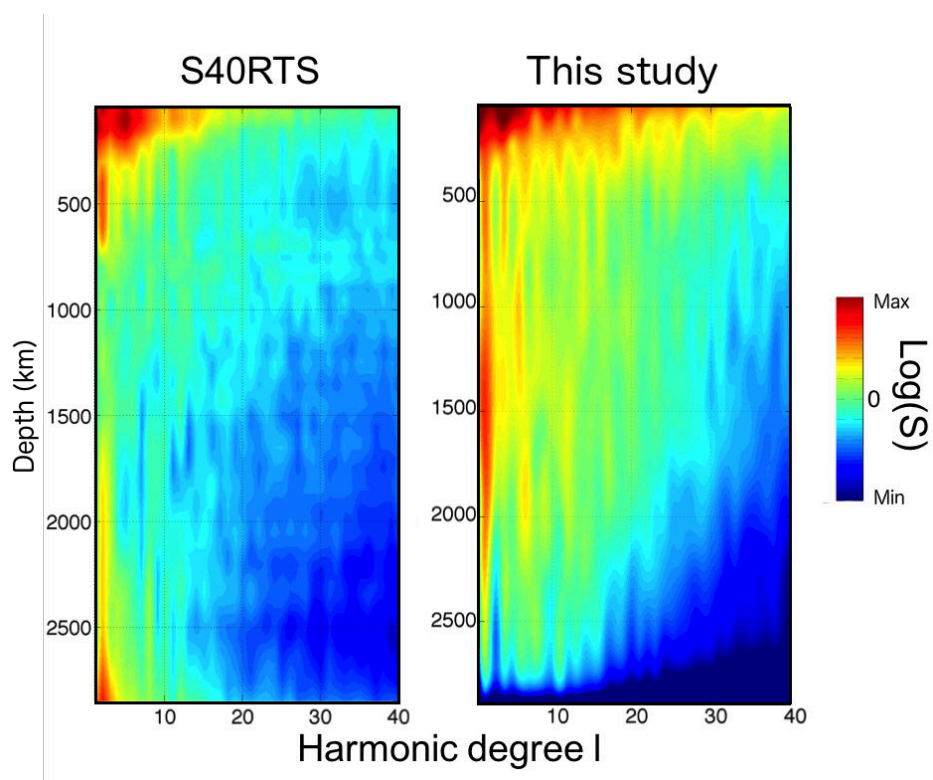


Figure 5. Power spectra of the seismic anomalies for the tomographic model S40RTS and the non-dimensional temperature field after imposing plate velocities until present-day. The amplitude of the power spectra is in log-scaled.

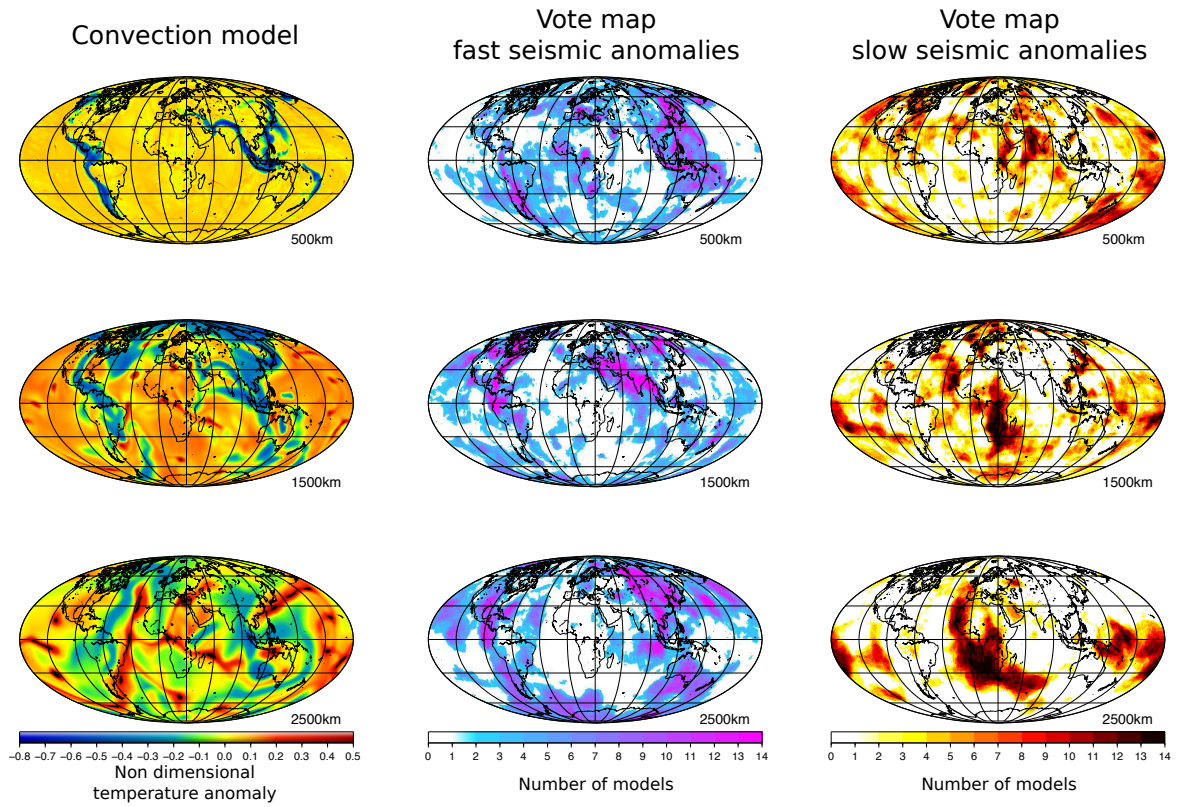


Figure 6. Comparison between slices in the convection model and vote maps computed from 14 tomographic models. Left column: maps at 500, 1500 and 2500 km depth of the non-dimensional temperature anomalies in the convection models. Central column: vote maps at the same depth for fast seismic anomalies in seven tomographic models of V_s and seven tomographic models of V_p . Right column: vote maps at the same depth for slow seismic anomalies in seven tomographic models of V_s and seven tomographic models of V_p .

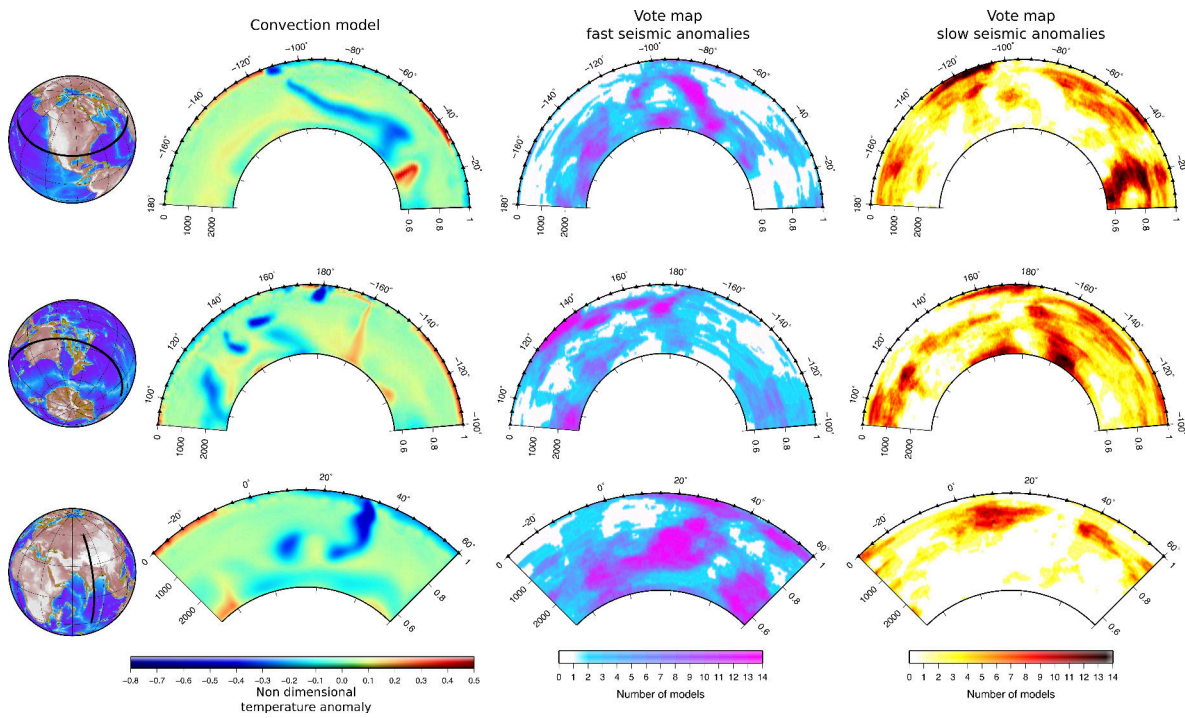


Figure 7. Comparison between cross sections through the convection model and the votes computed from 14 tomographic models. Left column: non-dimensional temperature anomalies in the convection model. Central column: votes for fast seismic anomalies in 14 tomographic models. Right column: votes for slow seismic anomalies in 14 tomographic models. Top: cross-sections of the Farallon slab below South California. Middle: cross-sections of the Tonga slab. Bottom: cross-sections of the slab below the Himalayan collision.

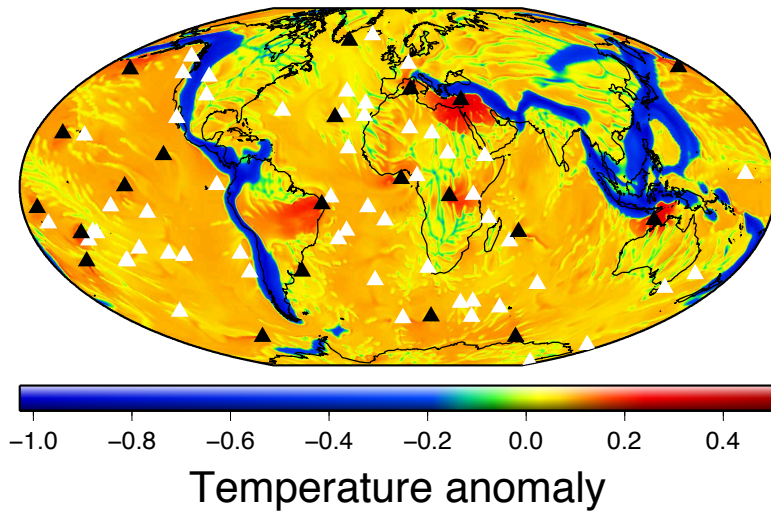


Figure 8. Temperature anomalies at 370 km depth and plume locations in the model at present-day after Step 2 in the flow chart. Non-dimensional temperature anomalies respective to the laterally averaged temperature. The black triangles represent the location of plumes reaching the top boundary layer in the model. The white triangles represent hotspot locations from the GPlates 2.0 database (Whittaker et al. 2015). The model was not designed to produce plumes at the same location as on Earth. The elongate negative anomalies represent the location of subducted slabs. Small scale convection below continents and ocean forms networks of alternating positive and negative anomalies (green and yellow-orange colours).

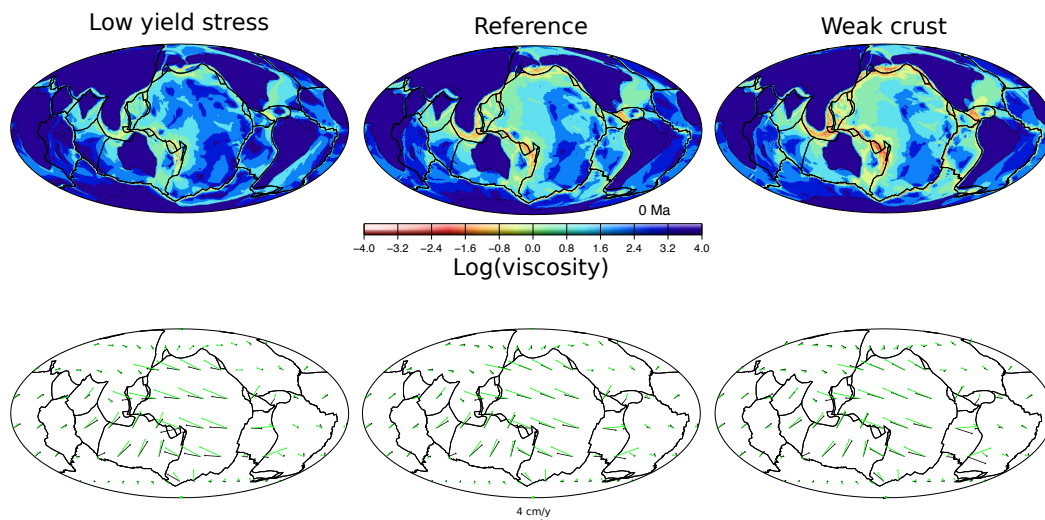


Figure 9. Viscosity field and kinematics of instantaneous flow models vs. plate boundaries and kinematics on Earth, at present-day. Top row: Viscosity field at 10 km depth emerging from the instantaneous flow calculation, and the expected plate layout of the Earth, as indicated by plate boundaries in black and based on the reconstruction of Seton et al. (2012). The reference model is in the middle column. The model with a factor of two lower yield stress is on the left, and the model with a weak crust is on the right. Bottom row: For the same models, black arrows represent model velocities and green arrows represent the expected velocities, as derived from the plate reconstruction of Seton et al. (2012).

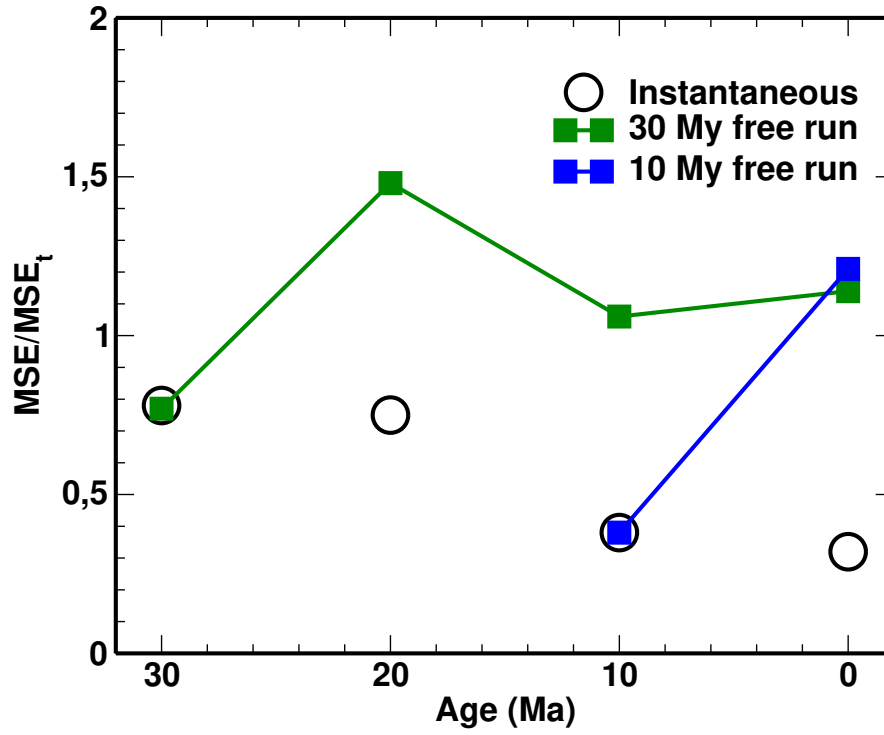


Figure 10. Ratio of the Mean Squared Error MSE of the computed velocity field (relative to the expected values for the Earth at 0, 10, 20 and 30 Ma) to the Mean Squared Error of the velocity of the tectonic reconstruction MSE_t (i.e. mean squared surface velocity in the no net rotation reference frame). Open circles represent the instantaneous flow calculations, while filled squares represent the fully dynamic evolution.

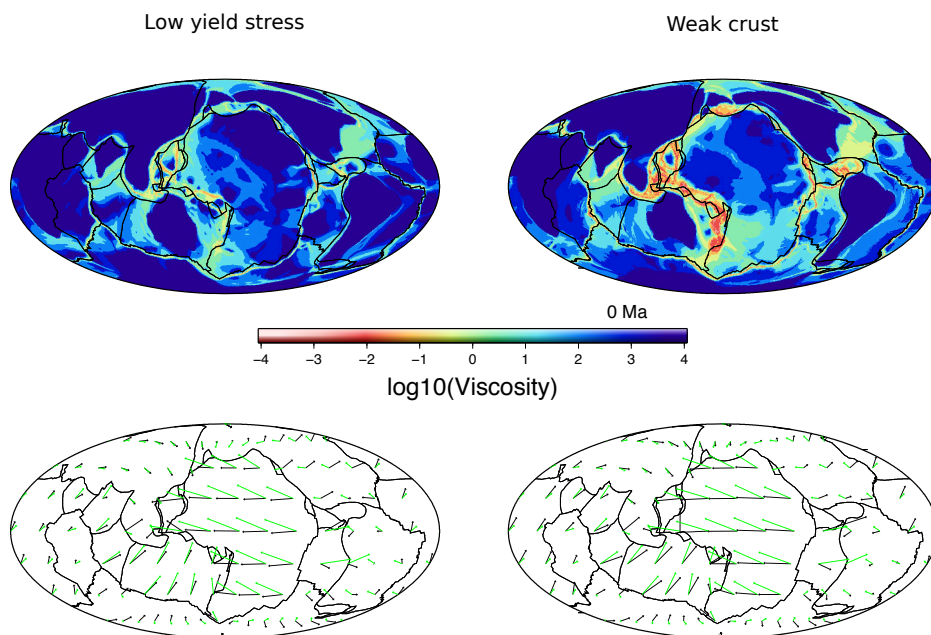


Figure 11. Viscosity field and kinematics of dynamic models started at 10 Ma vs. plate boundaries and kinematics on Earth. Top row: Viscosity field at 10 km depth emerging from the calculation after 10 My of evolution, and the expected plate layout of the Earth. The model having a factor of two lower yield stress is on the left, and the model with a weak crust is on the right. Bottom row: For the same models, black arrows represent model velocities and green arrows represent the expected velocities at present-day.

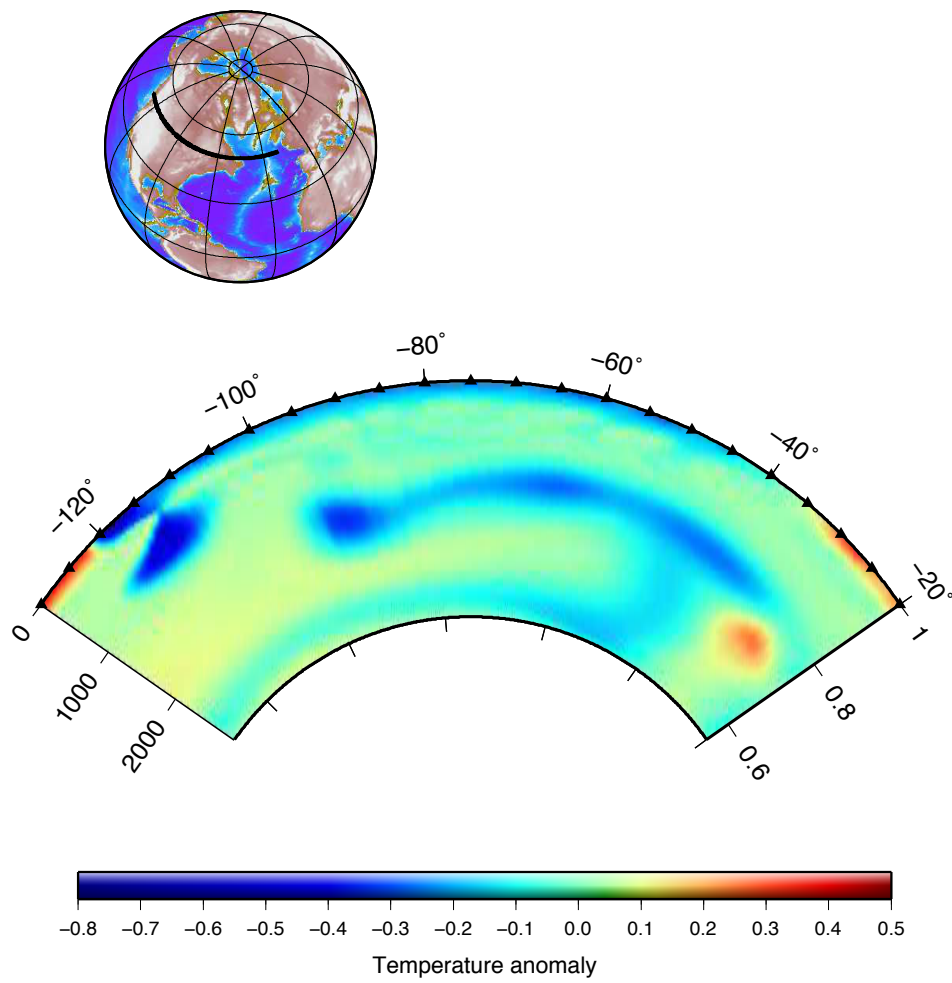


Figure 12. Erroneous prediction of slab break-off under Cascadia. The residual non-dimensional temperature field at 0 Ma for the dynamic evolution started at 10 Ma. The slab is broken off while it is not expected on Earth.

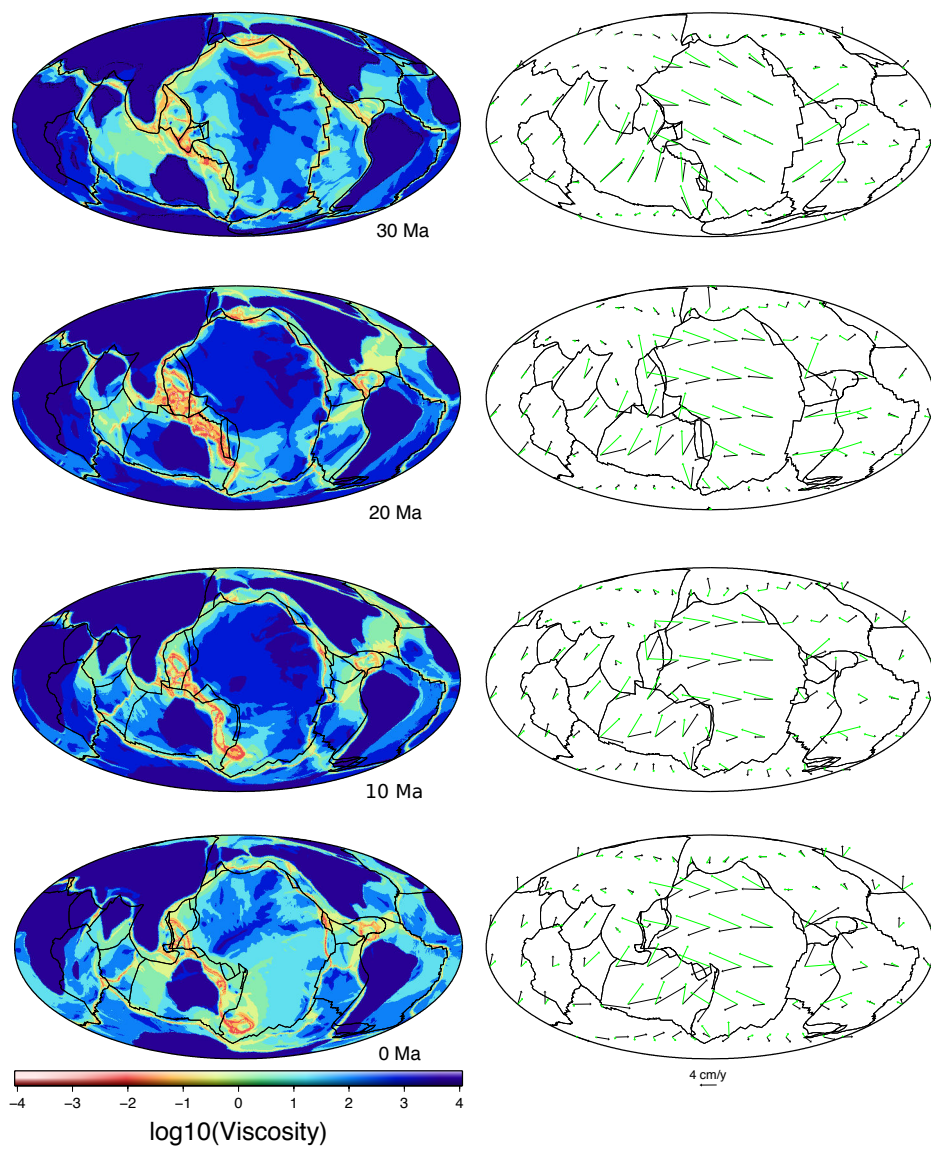


Figure 13. Viscosity field and kinematics of the dynamic models started at 30 Ma vs. plate boundaries and kinematics on Earth at the corresponding time-steps. Left column: Viscosity field at 10 km depth emerging from dynamic evolution of the model with weak crust, and the expected plate layout of the Earth over the time evolution based on plate boundaries from the model of Seton et al. (2012), black lines. Right column: black arrows represent model velocities and green arrows represent the expected velocities over the time evolution.