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C. Zimmermann, J. Bonkerud, F. Herklotz, T. N. Sky, A. Hupfer, E. Monakhov, B. G. Svensson, and L. Vines







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# Influence of annealing atmosphere on formation of electrically-active defects in rutile TiO<sub>2</sub>

C. Zimmermann, <sup>1</sup> J. Bonkerud, <sup>1</sup> F. Herklotz, <sup>2</sup> T. N. Sky, <sup>1</sup> A. Hupfer, <sup>1</sup> E. Monakhov, <sup>1</sup> B. G. Svensson, <sup>1</sup> and L. Vines <sup>1</sup>

<sup>1</sup>Physics Department/Centre for Materials Science and Nanotechnology, University of Oslo, P.O. Box 1048, Blindern, Oslo N-0316, Norway

<sup>2</sup>Department of Physics, Freie Universität Berlin, 14195 Berlin, Germany

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Electronic states in the upper part of the bandgap of reduced and/or hydrogenated *n*-type rutile TiO<sub>2</sub> single crystals have been studied by means of thermal admittance and deep-level transient spectroscopy measurements. The studies were performed at sample temperatures between 28 and 300 K. The results reveal limited charge carrier freeze-out even at 28 K and evidence the existence of dominant shallow donors with ionization energies below 25 meV. Interstitial atomic hydrogen is considered to be a major contributor to these shallow donors, substantiated by infrared absorption measurements. Three defect energy levels with positions of about 70 meV, 95 meV, and 120 meV below the conduction band edge occur in all the studied samples, irrespective of the sample production batch and the post-growth heat treatment used. The origin of these levels is discussed in terms of electron polarons, intrinsic point defects, and/or common residual impurities, where especially interstitial titanium atoms, oxygen vacancies, and complexes involving Al atoms appear as likely candidates. In contrast, no common deep-level defect, exhibiting a charge state transition in the 200–700 meV range below the conduction band edge, is found in different samples. This may possibly indicate a strong influence on deep-level defects by the post-growth heat treatments employed. *Published by AIP Publishing*. https://doi.org/10.1063/1.5011136

#### I. INTRODUCTION

Titanium dioxide (TiO<sub>2</sub>) in its rutile form has gained considerable attention for its photocatalytic properties <sup>1-3</sup> or as part of solar cells. <sup>4,5</sup> However, the bandgap of rutile TiO<sub>2</sub> is approximately 3.2 eV, <sup>6</sup> which is too wide for utilizing the solar spectrum efficiently. <sup>6</sup> Recently, reduced and/or hydrogenated TiO<sub>2</sub> has received increasing interest because it exhibits stronger absorption in the visible/infrared wavelength regime than virgin rutile TiO<sub>2</sub>. <sup>7,8</sup> However, the understanding of intrinsic and impurity-related defects in this material is not fully developed to date, but it is of key importance in virtually all of its applications.

Reduced and/or hydrogenated rutile  ${\rm TiO_2}$  exhibits n-type conductivity,  ${}^{9-13}$  but the nature of the main donor(s) is still under debate even after decades of research. The oxygen vacancy ( ${\rm V_O}$ ), titanium interstitial ( ${\rm Ti_i}$ ), and hydrogen on an interstitial site ( ${\rm H_i}$ ) are considered to be potential sources of n-type doping.  ${}^{10,11,14-19}$  However, the properties of these donors remain elusive and controversial. The question which of these defects are dominant might furthermore strongly depend on the actual sample treatment.  ${}^{19}$  Importantly, hydrogen could be present in significant concentrations also in samples which were not intentionally hydrogenated.  ${}^{18}$ 

The identification of defects in rutile TiO<sub>2</sub> is particularly challenging as the energy scheme of the defect levels may be influenced by polaronic effects. <sup>19–29</sup> First, this makes the theoretical description of defects in rutile TiO<sub>2</sub> exceptionally challenging. <sup>19,24</sup> Second, polaronic effects can also lead to different defects having similar experimental signatures as electrons are trapped at similar Ti sites no matter which

defect they actually originate from. <sup>19</sup> Another consequence of the polaronic effects is that techniques which probe thermal or optical transition energies will yield significantly different values for the same defect. Hence, they cannot directly be used complementarily in identifying defects. <sup>19,20,23,24</sup>

This can, for example, be observed in the case of  $H_i$ : Conductivity, transport, electron paramagnetic resonance, and infrared absorption measurements report on a shallow donor level with thermal transition energies of several meV,  $^{10,11,25,30-32}$  while absorption data indicate optical transition energies of around 1-2 eV.  $^{8,28,32,33}$ 

Another prominent example is  $V_O$ . Some experiments indicate that  $V_O$  is a shallow donor in rutile  $TiO_2$ , responsible for the *n*-type conductivity observed in samples annealed at low oxygen partial pressure, <sup>13,14,34</sup> while other studies report  $V_O$ -related deep states. <sup>35,36</sup> This controversy concerning  $V_O$  is further complicated by the results of *ab-initio* calculations, as different studies strongly disagree on whether  $V_O$  induces shallow effective mass-like states or deep donor levels. <sup>23,37–40</sup>

Space-charge spectroscopic techniques such as thermal admittance spectroscopy (TAS), 41,42 deep-level transient spectroscopy (DLTS), 43 and thermally stimulated current spectroscopy (TSC) 44 probe thermal transition energies of electrically active defects. So far, only very few studies have been reported in the literature, where TAS, 36 DLTS, 35 and TSC 45,46 are applied to gain insights into defect properties of rutile TiO<sub>2</sub>. Various defect levels between 130 meV and 870 meV below the conduction band edge have been reported; however, the identity of the associated defects remains unknown.

The scarcity of reports on space-charge spectroscopy performed on rutile  ${\rm TiO_2}$  is partially related to the difficulty in forming rectifying junctions. However, recent progress, see e.g., Ref. 48, shows promising results for Schottky contacts of sufficient quality to pursue TAS and DLTS studies on rutile  ${\rm TiO_2}$ .

In this work, we report on electrically active defects observed by TAS and DLTS measurements on rutile  $TiO_2$  single crystals subjected to different reducing and/or hydrogenating heat-treatments. Our results show that techniques such as TAS and DLTS are highly applicable for systematic studies of electrically active defects in non-stoichiometric rutile  $TiO_2$ .

#### II. EXPERIMENTAL

The samples used in the present study were (001)-oriented rutile  ${\rm TiO_2}$  single crystals grown by the float zone method and were purchased from MTI Corporation. The samples were acquired at different occasions and represent several different production batches. The as-received single crystals were colorless and semi-insulating, reflected by a resistivity of  $>10^7~\Omega$  cm. After cutting into  $5\times 5~{\rm mm^2}$ -sized samples, the crystals were cleaned in an ultrasonic bath with acetone, isopropanol, and deionized water for  $5~{\rm min}$  each. Afterwards, the samples were subjected to one of the three following heat treatments (annealings) using a tube furnace:

- 1. Annealing in forming gas flow  $(N_2 + H_2 \text{ with } [H_2]/[N_2] \approx 1/9$ , where the square brackets denote the concentration) at temperatures between 500 °C and 600 °C for 35–75 min. (forming gas annealing)
- 2. Annealing in closed ampules filled with H<sub>2</sub> gas (0.5 bar at room temperature) for 20 min or 40 min. The ampules were evacuated with a roughing pump before filling with H<sub>2</sub>. (H<sub>2</sub> gas annealing)
- 3. Annealing in  $N_2$  flow at temperatures between 980 °C and 1250 °C for 1.25–25 h. ( $N_2$  gas annealing)

The samples were always put into the furnace when the desired annealing temperature  $T_{\rm anneal}$  was reached. After the heat treatment, the samples were cooled-down without force in the cold furnace zone while maintaining the gas flow. Subsequently, the annealed crystals were cleaned again using the afore-mentioned procedure and further boiled in  $H_2O_2$  (40%) for 1–3 min. This treatment is commonly used for the preparation of Schottky diodes on ZnO and has proven to lead to highly rectifying diodes.

Between 10 and 15 Pd contacts with a thickness in the range of  $\sim$ 150–200 nm were deposited onto the samples via electron beam evaporation, using a Si shadow mask with pad areas of  $0.7 \times 10^{-3}$  to  $4.2 \times 10^{-3}$  cm<sup>2</sup>. Eutectic InGa was used as Ohmic back contact.

Secondary ion mass spectrometry (SIMS) measurements were performed using a Cameca IMS 7f instrument with a primary beam of  $10\,\mathrm{keV}$   $\mathrm{O}_2^+$  ions. Rutile  $\mathrm{TiO}_2$  samples implanted with Cr, Al, or Si were used as references to obtain absolute concentration values. For other residual elements, relative concentrations were determined. A constant erosion rate was assumed for depth-calibration, where the

crater depths were measured using a surface Stylus Profilometer.

Fourier transform infrared (FTIR) absorbance spectra were recorded with a Bruker IFS125 HR spectrometer equipped with a globar or tungsten light source, a KBr or  $CaF_2$  beam splitter, and an InSb detector. Measurements were performed with a spectral resolution of  $0.5 \, \mathrm{cm}^{-1}$  and at a sample temperature of 27 K. Unpolarized light was used with the wave vector,  $\vec{k}$ , directed perpendicular to the  $\vec{c}$ -axis of the samples.

The current-voltage (IV) and capacitance-voltage (CV) measurements were carried out under dark conditions at room temperature using a Keithley 6487 unit and an Agilent 4284A LCR meter, respectively.

DLTS was conducted using a refined version of the setup described elsewhere. In short, the setup utilizes a Boonton 7200 capacitance meter and a closed-cycle He cryostat. During measurements, reverse bias voltages between –4 V and –3 V were applied. Filling pulses with an amplitude of 2 V to 4 V and a duration of 50 ms were employed. The DLTS signal was extracted from the acquired capacitance-versus-time transients using a lock-in weighting function with six different rate windows in the range of (20 ms)<sup>-1</sup> to (640 ms)<sup>-1</sup>. A delay time of 5 ms and a temperature resolution of 1 K were used. Measurements were performed both during heat-up and cool-down.

TAS measurements were conducted with a temperature resolution of 1 K during heat-up and cool-down using an Agilent 4284A LCR meter at probe frequencies  $f_{\rm meas}$  between 10 kHz and 1 MHz. Further details about the setup used can be found in Ref. 52.

### III. RESULTS

SIMS measurements were performed in order to monitor selected relevant impurities in the heat-treated samples. Cr and Li, Al, and Si are present in significant concentrations, where the relative concentrations vary by at least an order of magnitude between different samples for Cr  $(10^{16}-10^{17}\,\mathrm{cm}^{-3})$ , Al  $(10^{16}-10^{17}\,\mathrm{cm}^{-3})$ , and Li  $(\leq 10^{16}\,\mathrm{cm}^{-3})$ , whilst lower variations are found for Si  $(10^{17}\,\mathrm{cm}^{-3})$ .

FTIR measurements were undertaken to determine the concentration of interstitial hydrogen (H<sub>i</sub>) from its O–H vibrational mode at  $\sim\!\!3290\,\mathrm{cm}^{-1}.^{30,53}$  The as-received TiO $_2$  samples reveal a H<sub>i</sub> concentration in the range of  $1\text{--}3\times10^{16}\,\mathrm{cm}^{-3}.$  The heat treatments result in an increase of [H<sub>i</sub>]. For the N $_2$  gas annealed samples, [H<sub>i</sub>] increases to about  $5\times10^{17}\,\mathrm{cm}^{-3}.$  Substantially, more H<sub>i</sub> is observed in the case of annealing in H $_2$  gas or forming gas. In both cases, precise quantitative measurements are prevented because of the high [H<sub>i</sub>], leading to saturation of the O–H vibrational mode in the FTIR absorbance spectra.

Generally, different Pd/TiO<sub>2</sub>/InGa junctions on the same TiO<sub>2</sub> sample display different IV characteristics, especially in terms of rectification. This indicates an inhomogeneity of the as-received samples unveiled by the applied annealing procedure. For some diodes, rectifications of up to six orders of magnitude in current can be found when the applied voltage *V* is varied between –4 V and 4 V. In Fig. 1, examples of

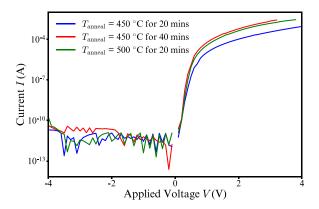


FIG. 1. IV curves of Pd Schottky contacts on  $\mathrm{H}_2$  gas annealed  $\mathrm{TiO}_2$  single crystals.

such IV curves are shown for H<sub>2</sub> gas annealed samples. In general, similar results are obtained independently of the specific annealing procedure used.

In Fig. 2, the results of CV measurements using different probe frequencies (4 kHz–1 MHz) are shown for two Pd/TiO<sub>2</sub>/InGa junctions by depicting  $1/C^2$  versus V. Two equivalent circuits consisting of only one resistance and capacitance were assumed to deduce the capacitance of the junctions (see also the inset of Fig. 2): (i) Capacitance  $C_P$  parallel to a resistance  $R_P$  (solid lines and left inset) and (ii) Capacitance  $C_S$  and a resistance  $R_S$  in series (dashed lines and right inset).

According to the depletion approximation, the depletion layer capacitance  $C_d$  of a Schottky junction on an n-type semiconductor is given by  $^{54}$ 

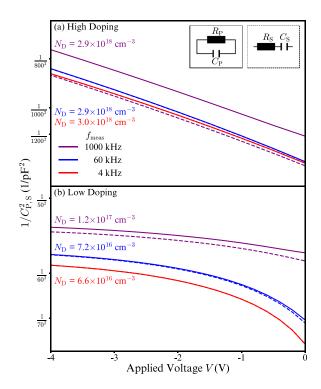


FIG. 2. Frequency-dependent  $1/C_{\rm P,S}^2$  - V plots for Pd Schottky contacts on forming gas annealed TiO<sub>2</sub> crystals. An equivalent circuit with the depletion layer capacitance  $C_{\rm d}$  either in parallel (solid lines and left inset) or in series (dashed lines and right inset) with a resistance has been assumed.

$$C_{\rm d} = \sqrt{\frac{A^2 \epsilon_0 \epsilon_{\rm r} e N_{\rm D}}{2(V_{\rm bi} + V_{\rm bias})}}.$$
 (1)

Here, A denotes the junction area,  $\epsilon_0$  the vacuum permittivity,  $\epsilon_r$  the static dielectric constant, e the elementary charge,  $N_D$  the donor concentration,  $V_{bi}$  the built-in voltage, and  $V_{bias}$  the applied bias voltage. A static dielectric constant  $\epsilon_r$  of 100 was assumed.  $^{10-12,55,56}$  For a uniform donor concentration, one expects a straight line for  $1/C_d^2$  versus  $V_s^{54}$  which holds reasonably well for the highly doped sample in Fig. 2(a). From the slope of the curves, we obtain a donor concentration  $N_D$  of about  $3 \times 10^{18}$  cm<sup>-3</sup>. For high reverse bias voltages and the highest probe frequency employed (1 MHz), a linear behavior is also observed for the low-doped sample [see Fig. 2(b)]. From the corresponding slope, a donor concentration  $N_D$  of about  $1 \times 10^{17}$  cm<sup>-3</sup> is obtained. For low reverse bias voltages and especially low probe frequencies, pronounced deviations from a linear dependence occur as will be commented on in the discussion Sec. IV A.

#### A. Thermal admittance spectroscopy

In TAS, the capacitance C and conductance G of a rectifying junction are determined as a function of sample temperature T and probe frequency  $f_{\rm meas}^{41,42}$  by assuming an appropriate equivalent circuit for the junction. Here, a series circuit was assumed and the measured capacitance is denoted as  $C_{\rm S}$  for series capacitance [see also the right inset of Fig. 2(a)].

When crossed by the Fermi level, shallow defect levels being present in the junction give rise to inflection points  $T_{\rm inf}$  in the C-T spectra<sup>41,42,58</sup> and can be used to determine the activation energy (enthalpy)  $E_{\rm A}=E_{\rm C}-E_{\rm D}$  ( $E_{\rm C}=$  conduction band edge and  $E_{\rm D}=$  defect level position) of shallow states using  $^{42,54}$ 

$$\frac{2\pi f_{\text{meas}}}{T_{\text{inf}}^2} \sim \exp\left(-\frac{E_{\text{A}}}{k_{\text{b}}T_{\text{inf}}}\right),$$
 (2)

where  $k_{\rm b}$  denotes the Boltzmann constant.

Figure 3 shows representative TAS spectra obtained on four different Pd/TiO<sub>2</sub>/InGa junctions. The corresponding TiO<sub>2</sub> samples were forming gas annealed (a) and (b), H<sub>2</sub> gas annealed (c), and N<sub>2</sub> gas annealed (d). Several inflection points in the  $C_S$ -T plots are revealed, which correspond to electron states being present in TiO<sub>2</sub>. The values of  $T_{\rm inf}$  to be used in Eq. (2) were extracted from the local maxima positions in the derivative spectra  ${\rm d}C_S/{\rm d}T^{58}$  [see the example in the inset of Fig. 3(b)].

All the investigated forming gas annealed samples [see Figs. 3(a) and 3(b)] show the electron levels labeled  $D_{2,\mathrm{FG}}$  and  $D_{3,\mathrm{FG}}$ .  $D_{4,\mathrm{FG}}$  is only present in some samples in sufficient concentrations to be detected by TAS. The levels labeled  $D_{1,\mathrm{H}}$ ,  $D_{2,\mathrm{H}}$ , and  $D_{3,\mathrm{H}}$  are seen for all the investigated samples annealed in  $H_2$  gas [see Fig. 3(c)]. For all the investigated samples annealed in  $N_2$  gas, the levels  $D_{2,\mathrm{N}}$  and  $D_{3,\mathrm{N}}$  are observed, while  $D_{4,\mathrm{N}}$  is only detected in a few samples.  $D_{1,\mathrm{FG}}$ ,  $D_{1,\mathrm{H}}$ , and  $D_{1,\mathrm{N}}$  can only be resolved at very low temperatures.

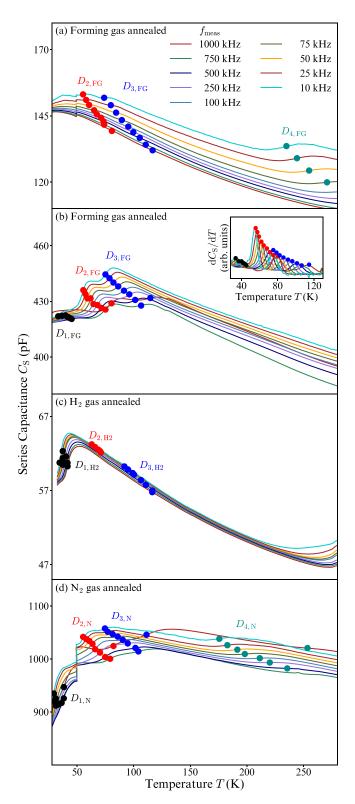


FIG. 3.  $C_S - T$  plots for four different Pd/TiO<sub>2</sub>/InGa junctions. The inset in (b) shows  $dC_S/dT$  over T, which was used to determine  $T_{\inf}$  [see Eq. (2)].

By comparing the value pairs ( $T_{\rm inf}$ ,  $f_{\rm meas}$ ) for the electron levels observed in samples subjected to different heat-treatments, it is found that  $D_{\rm 2,FG}$  and  $D_{\rm 2,N}$ , as well as  $D_{\rm 3,FG}$  and  $D_{\rm 3,N}$ , respectively, can arise from the same electron levels.

Figure 4 displays Arrhenius plots obtained from the TAS spectra shown in Fig. 3 according to Eq. (2). Linear least-

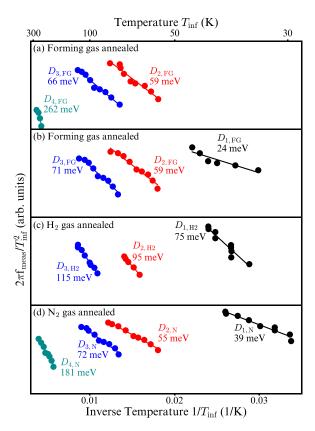


FIG. 4. Arrhenius plots derived from the  $C_S$ -T curves shown in Fig. 3 using Eq. (2).

squares fits, represented by solid lines in Fig. 4, have been used to determine  $E_{\rm A}$ . In Table I, the obtained activation energy values of the observed electron levels are summarized.

#### B. Deep-level transient spectroscopy

DLTS was used to probe deep electron traps in heat-treated TiO<sub>2</sub> samples. The trap concentration  $N_{\rm T}$  was deduced assuming a uniform and sufficiently low ( $\leq 0.1 N_{\rm D}$ ) defect distribution, where<sup>43,54</sup>

$$N_{\rm T} = 2 \frac{\Delta C}{C_{\rm rh}} N_{\rm D}. \tag{3}$$

Here,  $\Delta C$  is determined from the measured capacitance transients, <sup>43,51,54</sup> while  $C_{\rm rb}$  is the capacitance measured at the

TABLE I. Overview of thermal activation energies  $E_{\rm A}$  determined by TAS on Pd/TiO<sub>2</sub>/InGa junctions. Subscript FG: forming gas annealing, N: N<sub>2</sub> gas annealing, and H2: H<sub>2</sub> gas annealing. The intervals stated take into account the fitting errors and the spread across the surface of the samples measured.

Forming gas annealed		H <sub>2</sub> gas	annealed	N <sub>2</sub> gas annealed		
Defect level	E <sub>A</sub> (meV)	Defect level	E <sub>A</sub> (meV)	Defect level	E <sub>A</sub> (meV)	
$D_{1,FG}$	[19, 29]	$D_{1,{ m H2}}$	[67, 84]	$D_{1,\mathrm{N}}$	[35, 42]	
$D_{2,\mathrm{FG}}$	[54, 65]	$D_{2,\mathrm{H2}}$	[92, 98]	$D_{2,\mathrm{N}}$	[53, 57]	
$D_{3,FG}$	[62, 75]			$D_{4,\mathrm{N}}$	[169, 192]	
$D_{4,\mathrm{FG}}$	[206, 318]					

quiescent reverse bias voltage.  $N_{\rm D}$  is derived from CV measurements.<sup>54</sup>

For each DLTS rate window, the peak in  $\Delta C$  occurs at a different  $T_{\text{max}}$ . Using the following relation for the electron emission rate  $e_{\text{n}}$  at the DLTS peak maximum<sup>54</sup>

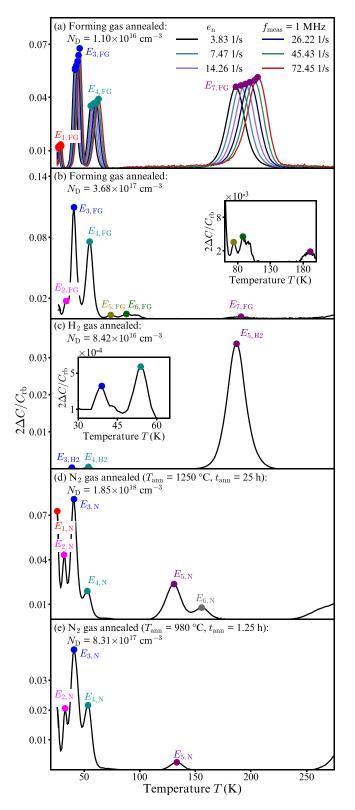


FIG. 5. DLTS results for five different Pd/TiO<sub>2</sub>/InGa junctions. In (a), results for the six rate windows used for obtaining Arrhenius plots are shown. In (b)–(e), only the results for the longest rate window are displayed  $(e_n = 3.83 \, \text{s}^{-1}$  at the peak maximum).

$$\frac{e_{\rm n}}{T_{\rm max}^2} = \beta \sigma_{\rm a} \exp\left(-\frac{E_{\rm A}}{k_{\rm b} T_{\rm max}}\right),\tag{4}$$

the apparent capture cross-section  $\sigma_a$  and the thermal activation energy  $E_A$  for the deep-level defect can be determined.  $\beta$  is a material-specific constant and is given by  $^{43,54}$ 

$$\beta = 2\sqrt{3} \left(\frac{2\pi}{h^2}\right)^{3/2} k_b^2 m_e^*. \tag{5}$$

Here,  $m_{\rm e}^*$  denotes the effective electron mass in TiO<sub>2</sub>, while h is the Planck constant. There is quite a spread in values reported for  $m_{\rm e}^*$ . <sup>11,34,59–64</sup> In this study, a value of ten-times the free electron mass  $m_{\rm e}$  is assumed.

Figure 5 displays exemplary DLTS spectra measured on Pd/TiO<sub>2</sub>/InGa junctions. Figures 5(a) and 5(b) show the results for forming gas annealed samples, where seven different defect levels are observed. The levels labeled  $E_{3,FG}$  and  $E_{4,FG}$  are present in all samples irrespective of the annealing conditions used (duration or temperature) and the specific production batch from which the TiO<sub>2</sub> single crystals originated.  $E_{1,FG}$  appears at very low temperatures and was not resolved for all the measurements shown here. The levels  $E_{2,FG}$ ,  $E_{5,FG}$ ,  $E_{6,FG}$ , and  $E_{7,FG}$  occur occasionally and were not observed in all the investigated samples.

In Fig. 5(c), a DLTS spectrum of a  $H_2$  gas annealed sample is shown. Different annealing durations and/or temperatures lead to qualitatively similar DLTS spectra with similar levels being present and  $E_{5,\rm H2}$  as the dominant one. All the investigated samples originated from the same production batch.

Figures 5(d) and 5(e) show DLTS results for the  $N_2$  gas annealed samples. The samples originated from the same production batch but were subjected to different annealing durations and temperatures. The levels  $E_{2,N}$ ,  $E_{3,N}$ ,  $E_{4,N}$ , and  $E_{5,N}$  are observed in all the samples, whereas  $E_{6,N}$  is only present in samples annealed at high temperatures and for long durations. The level  $E_{1,N}$  is very shallow and can only be resolved fully at low temperatures using short rate windows.

When comparing the  $(T_{\rm max}, e_{\rm n})$  pairs for the observed defect levels across samples subjected to different heat-treatments, it can be found that the following defect levels may have the same origin:  $E_{\rm 2,N}$  and  $E_{\rm 2,FG}$ ,  $E_{\rm 3,N}$ ,  $E_{\rm 3,FG}$ , and  $E_{\rm 3,H2}$ , and  $E_{\rm 4,FG}$ ,  $E_{\rm 4,N}$ , and  $E_{\rm 4,H2}$ .

In Table II, an overview of the observed defect levels and their activation energy values, as well as apparent capture cross sections, is given. Due to the ambiguity concerning the value of the effective electron mass  $m_{\rm e}^*$ , only orders of magnitude values are stated for  $\sigma_{\rm a}$ .

# IV. DISCUSSION

#### A. Experimental remarks

Generally, the Pd/TiO<sub>2</sub>/InGa junctions display high rectification (see Fig. 1) as required for accurate space-charge spectroscopy measurements. In the case of highly doped samples, the CV characteristics resemble those expected for a depletion layer capacitance under uniform doping [see the linear  $1/C^2$  - V dependency in Fig. 2(a)]. However,

TABLE II. Overview of thermal activation energies  $E_A$  and apparent capture cross sections  $\sigma_a$  determined using DLTS on Pd/TiO<sub>2</sub>/InGa junctions. Subscript FG: forming gas annealing, N: N<sub>2</sub> gas annealing, and H2: H<sub>2</sub> gas annealing. The intervals stated for  $E_A$  take into account fitting errors and the scatter between the measured samples. The values stated for  $\sigma_a$  take only into account the scatter across the surface of the samples because of the large uncertainty.

Forming gas annealed			H <sub>2</sub> gas annealed			N <sub>2</sub> gas annealed		
Defect level	E <sub>A</sub> (meV)	$\sigma_{\rm a}({\rm cm}^2)$	Defect level	E <sub>A</sub> (meV)	$\sigma_{\rm a}~({\rm cm}^2)$	Defect level	E <sub>A</sub> (meV)	$\sigma_{\rm a}~({\rm cm}^2)$
$E_{1,FG}$	[57, 76]	$10^{-13}$	$E_{1,\mathrm{H2}}$	[49, 96]	$10^{-11}$	$E_{2,\mathrm{N}}$	[63, 93]	$[10^{-15}, 10^{-12}]$
$E_{2,\mathrm{FG}}$	[69, 96]	$[10^{-14}, 10^{-12}]$	$E_{3,\mathrm{H2}}$	[81, 104]	$10^{-14}$	$E_{1,\mathrm{N}}$	[82, 99]	$10^{-12}$
$E_{3,FG}$	[87, 111]	$[10^{-15}, 10^{-13}]$	$E_{4,\mathrm{H2}}$	[92, 144]	$[10^{-16}, 10^{-14}]$	$E_{3,\mathrm{N}}$	[86, 109]	$[10^{-15}, 10^{-13}]$
$E_{6,\mathrm{FG}}$	[104, 114]	$10^{-20}$	$E_{5,\mathrm{H2}}$	[446, 471]	$[10^{-15}, 10^{-14}]$	$E_{4,\mathrm{N}}$	[110, 123]	$10^{-15}$
$E_{4,\mathrm{FG}}$	[111, 132]	$[10^{-15}, 10^{-14}]$				$E_{5,\mathrm{N}}$	[273, 313]	$[10^{-16}, 10^{-15}]$
$E_{5,\mathrm{FG}}$	[204, 218]	$10^{-12}$				$E_{6,\mathrm{N}}$	[365, 395]	$[10^{-15}, 10^{-14}]$
$E_{7,\mathrm{FG}}$	[424, 630]	$[10^{-14}, 10^{-13}]$						

deviations from this behavior are evident for low doped samples [see Fig. 2(b)]. These deviations can be caused by a non-uniform doping concentration, a highly compensated interfacial layer being present between the metal contact(s) and TiO<sub>2</sub>, <sup>47,65-67</sup> a high density of deep defect levels not responding fully to the probe frequency, <sup>68</sup> or high series resistance. <sup>69,70</sup>

Our set of data indicates that several of these causes contribute to the recorded CV characteristics, especially high series resistance and the presence of a highly compensated interfacial layer. We found that their relative contribution depends on the sample and its particular treatment. By using comparatively small contact areas, the effect of the high series resistance can be minimized, <sup>69,70</sup> and a detailed analysis of the CV characteristics and barrier heights of the Schottky junctions used in this work can be found in Ref. 48.

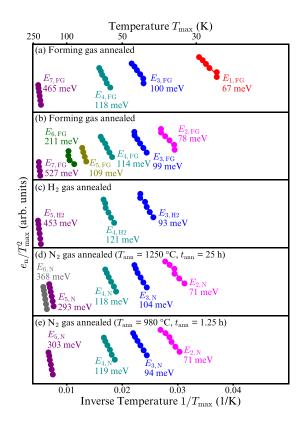


FIG. 6. Arrhenius plots according to Eq. (4) derived from the DLTS measurements shown in Fig. 5.

The interpretation of TAS and DLTS data is facilitated by uniform net carrier concentration versus depth profiles acquired at high measurement frequencies ( $\geq 10\,\mathrm{kHz}$ ). Indeed, this was confirmed for all the samples presented here prior to TAS and/or DLTS measurements. The validity of the TAS and DLTS analysis is furthermore corroborated by the applicability of Eqs. (2) and (4). For essentially all the observed defect levels, an Arrhenius dependence holds for the extracted electron emission rates. The exception is the shallow level  $D_{1,\mathrm{FG}}$ , which is affected by charge carrier freeze-out.

#### B. Origin of the observed defect levels

The data in Figs. 3–6 reveal the presence of some rather prominent shallow electron traps ( $E_A \leq 130 \,\mathrm{meV}$ ) and that charge carrier-freeze out is limited even at 28 K. Irrespective of the sample production batch and the post-growth heat treatment employed, three particular levels always occur. They exhibit similar electron emission rates as a function of temperature in each sample with  $E_{\rm A} \approx 70 \, {\rm meV} \, (D_{3,{\rm FG}}, E_{2,{\rm FG}},$  $D_{1,H2}$ ,  $D_{2,N}$ , and  $E_{2,N}$ ),  $E_A \approx 95 \text{ meV}$  ( $E_{3,FG}$ ,  $D_{2,H2}$ ,  $E_{3,H2}$ , and  $E_{2,N}$ ), and  $E_A \approx 120 \,\mathrm{meV}$  ( $E_{4,FG}$ ,  $D_{3,H2}$ , and  $E_{4,N}$ ), respectively. This implies that these levels arise from intrinsic defects or defects involving omnipresent residual impurities. Generally, the absolute concentrations of defect levels in TiO2 are difficult to determine with a high degree of accuracy because of the uncertainty in the dielectric constant (permittivity).  $^{10-12,55,56}$  However, by assuming  $\epsilon_r=100$  (as for the CV data), one arrives at values of  $10^{15}$ – $10^{17}$  cm<sup>-3</sup> for most of the levels in Fig. 5.

Polaronic effects are strong in rutile  $TiO_2$  and may be responsible for some of the observed levels via self-trapping of electrons on Ti sites. For instance, Frederikse<sup>61</sup> and Deák *et al.*,<sup>24</sup> as well as Janotti *et al.*,<sup>23</sup> have reported experimental and theoretical indications, respectively, of such electron states with  $E_A$  below 150 meV. Other prevalent intrinsic candidates anticipated in reduced rutile  $TiO_2$  are the donor-like  $Ti_i$  and  $V_O$  centers. <sup>6,16,17,19</sup> However, reports on the  $E_A$  values for these two centers are scarce in the literature. Brandão *et al.* <sup>14</sup> suggested  $E_A \approx 2.8$  meV for a  $V_O$  donor-state based on electron paramagnetic resonance measurements, which is considerably lower than the thermal activation energy of our three "general" levels. On the other hand, rather recent

density functional theory (DFT) calculations by Janotti et al.<sup>23</sup> predict single and double donor states of  $V_O$  with  $E_A$ equal to about 100 meV and 140 meV, respectively, for a configuration where the donor electrons are rather localized at neighboring Ti atoms  $(V_O^{+2} + 2Ti^{+3})$ . Hence,  $V_O$  cannot be excluded as the origin of our 95 meV and 120 meV levels. Furthermore, Deák et al. 24 computed  $E_A \approx 100 \,\mathrm{meV}$  and ≈1300 meV for the single and double donor states, respectively, of a Vo configuration where the electrons are localized at the V<sub>O</sub> site. Mattioli *et al.*<sup>37</sup> conducted similar calculations as in Ref. 24 but found a substantially lower  $E_A$  value of about 300 meV for the double donor state. For thermally induced charge state transitions of Ti<sub>i</sub> in rutile TiO<sub>2</sub>, Hubbard-U corrected DFT data by Mattioli et al.37 suggest that the single and double donor levels are resonant with the conduction band, whilst the triple and quadruple ones are located in the bandgap at  $\approx$ 70 meV and 400 meV below the conduction band edge. Thus, Ti<sub>i</sub> may be an intrinsic candidate for the common level observed at 70 meV in our samples.

Main residual impurities found in all the investigated samples are H, Li, Al, Si, and Cr according to FTIR and SIMS measurements. Li displays a concentration below 10<sup>16</sup> cm<sup>-3</sup>, and the three latter ones exhibit concentrations between  $10^{16}$  and  $10^{17}$  cm<sup>-3</sup>. The H content is estimated to increase from the  $10^{16} \, \mathrm{cm}^{-3}$  range in the as-received samples to above  $10^{18} \, \text{cm}^{-3}$  after the forming gas and H<sub>2</sub> gas anneals where the absorption signal saturates. Si substitutes for Ti in rutile TiO<sub>2</sub><sup>71,72</sup> and is not expected to introduce localized electronic states in the bandgap but rather to give rise to bandgap narrowing. 60,72 Li in an interstitial configuration is potentially a shallow donor,  $^{26,60}$  but the predicted  $E_{\rm A}$  value is only 30 meV and does not agree with those of our three common levels. Also, the anticipated electron trap positions associated with Cr in rutile TiO2 deviate substantially from those of our three common levels, exhibiting values of 190 meV and 410 meV below the conduction band edge. 46 Hence, both Li and Cr (as well as Si) are ruled out as likely candidates for the three common levels while Al in combination with  $V_0$  appears to be a more plausible suggestion. Al itself substitutes for Ti and gives rise to an acceptor level in the lower part of the bandgap, i.e., Al on the Ti site acts as a p-type dopant. 34,73 However, on the basis of generation noise recombination and temperature-dependent Hall effect measurements, it is argued by different authors 60,74 that Al-related shallow acceptor states also occur close to the conduction band. In particular, Acket and Volger<sup>60</sup> have ascribed a level at  $\sim$ 50 meV below the conduction band edge to a  $2Al_{Ti}$  - $V_{O}$ complex which may be associated with our most shallow "general" defect level ( $E_A \approx 70 \,\mathrm{meV}$ ) or alternatively with the prominent one at ≈60 meV detected after forming gas and  $N_2$  gas anneals only  $(D_{2,FG}, D_{2,N})$ .

Interstitial H is prevailing in all the studied samples, as manifested by its characteristic absorption line at  $\sim$ 3290 cm<sup>-1</sup> in the acquired IR spectra. This holds already for the as-received samples and becomes even more clear after the forming gas and H<sub>2</sub> gas heat treatments. H<sub>i</sub> is a shallow donor in TiO<sub>2</sub>, and the 3290 cm<sup>-1</sup> line originates from the local vibrational mode of an O-H bond oriented perpendicular to the c-axis of the crystal. Monitoring the free

carrier absorption as a function of temperature and concurrently the transformation between neutral and positively ionized H<sub>i</sub>, Herklotz et al.<sup>30</sup> determined  $E_A$  to be  $10 \pm 1 \,\mathrm{meV}$ for the H<sub>i</sub> donor. This value is also corroborated by a muon spectroscopy study conducted by Shimomura et al. 22 To the best of our knowledge, no corresponding theoretical estimates are available in the literature. Accordingly, H<sub>i</sub> can be excluded as the origin of any of the three "general" defect levels observed in the present samples. However, in addition to Ti, and possibly Vo, Hi is an obvious candidate for the strong shallow donor activity found in our samples, exhibiting limited carrier freeze-out even at 28 K. That is, the dominant donor(s) must have an ionization energy below  $\sim$ 25 meV. Such very shallow donor states in reduced rutile  $TiO_2$  have also been reported by other authors, <sup>9-13</sup> and they are, indeed, expected to be due to intrinsic defect defects (like Ti<sub>i</sub> and possibly V<sub>O</sub>) and/or common residual impurities (like H<sub>i</sub>). Here, it should also be noted that the abnormal decrease in the depletion capacitance observed at temperatures above 50-100 K in the TAS measurements (Fig. 3) is not caused by a decreasing concentration of ionized shallow donors but primarily attributed to the temperature variation of  $\epsilon_r$  in rutile TiO<sub>2</sub>.

Finally, as demonstrated in Fig. 5, no common deep-level defect ( $E_{\rm A} \geq 200\,{\rm meV}$ ) is found to be present in different samples. A rather prominent level with  $E_{\rm A} \approx 300\,{\rm meV}$  exists after N<sub>2</sub> gas annealing ( $E_{\rm 5,N}$ ) but not after forming gas and H<sub>2</sub> gas annealing. The opposite holds for the pronounced level with  $E_{\rm A} \approx 460\,{\rm meV}$  ( $E_{\rm 7,FG}$  and  $E_{\rm 5,H2}$ ), present after forming gas and H<sub>2</sub> gas annealing but not after N<sub>2</sub> gas annealing. This indicates that these levels arise from (i) defects involving residual impurities with varying concentrations in different samples and/or (ii) complexes involving intrinsic defects being strongly influenced by the annealing conditions used. Further work needs to be pursued in order to resolve this issue.

# **V. SUMMARY**

The DLTS and TAS techniques are demonstrated to be highly applicable for detailed investigations of electrically active defects in rutile TiO<sub>2</sub> single crystals. A comprehensive study of Pd/TiO<sub>2</sub>/InGa junctions has been performed using TiO<sub>2</sub> crystals post-growth heat-treated in FG, H<sub>2</sub>, or N<sub>2</sub> atmospheres. Irrespective of the sample production batch and the heat-treatment employed, three rather shallow levels occur in all the samples with  $E_A \approx 70 \,\mathrm{meV}, \approx 95 \,\mathrm{meV}$  and  $\approx$ 120 meV, respectively. The origins of these levels are discussed in some detail where electron polarons and intrinsic defects such as Ti<sub>i</sub> and V<sub>O</sub> appear as viable candidates and complexes involving common residual impurities, especially Al in combination with V<sub>O</sub>. Furthermore, TAS data display limited charge carrier freeze-out even at 28 K (minimum temperature reached) and evidence the presence of dominant and very shallow donors ( $E_A \le 25 \,\mathrm{meV}$ ). An obvious shallow donor is the omnipresent Hi, as revealed by infrared absorption measurements of the studied samples, having an ionization energy of only  $\sim 10 \,\mathrm{meV}$ . In contrast to the shallow defects, no common deep-level defect is found to be present in different samples, possibly indicating a stronger dependence on the annealing conditions used.

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