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# Thermoelectric Properties of $\text{Ca}_3\text{Co}_{2-x}\text{Mn}_x\text{O}_6$ ( $x = 0.05, 0.2, 0.5, 0.75,$ and $1$ )

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**Abstract:** High-temperature instability of the  $\text{Ca}_3\text{Co}_{4-y}\text{O}_{9+\delta}$  and  $\text{CaMnO}_{3-\delta}$  direct p-n junction causing the formation of  $\text{Ca}_3\text{Co}_{2-x}\text{Mn}_x\text{O}_6$  has motivated the investigation of the thermoelectric performance of this intermediate phase. Here, the thermoelectric properties comprising Seebeck coefficient, electrical conductivity, and thermal conductivity of  $\text{Ca}_3\text{Co}_{2-x}\text{Mn}_x\text{O}_6$  with  $x = 0.05, 0.2, 0.5, 0.75,$  and  $1$  are reported. Powders of the materials were synthesized by the solid-state method, followed by conventional sintering. The material  $\text{Ca}_3\text{CoMnO}_6$  ( $x = 1$ ) demonstrated a large positive Seebeck coefficient of  $668 \mu\text{V}/\text{K}$  at  $900 \text{ }^\circ\text{C}$ , but very low electrical conductivity. Materials with compositions with  $x < 1$  had lower Seebeck coefficients and higher electrical conductivity, consistent with small polaron hopping with an activation energy for mobility of  $44 \pm 6 \text{ kJ/mol}$  and where both the concentration and mobility of hole charge carriers were proportional to  $1-x$ . The conductivity reached about  $11 \text{ S}\cdot\text{cm}^{-1}$  at  $900 \text{ }^\circ\text{C}$  for  $x = 0.05$ . The material  $\text{Ca}_3\text{Co}_{1.8}\text{Mn}_{0.2}\text{O}_6$  ( $x = 0.2$ ) yielded a maximum  $zT$  of  $0.021$  at  $900 \text{ }^\circ\text{C}$ . While this value in itself is not high, the thermodynamic stability and self-assembly of  $\text{Ca}_3\text{Co}_{2-x}\text{Mn}_x\text{O}_6$  layers between  $\text{Ca}_3\text{Co}_{4-y}\text{O}_{9+\delta}$  and  $\text{CaMnO}_{3-\delta}$  open for new geometries and designs of oxide-based thermoelectric generators.

**Keywords:**  $\text{Ca}_3\text{Co}_{2-x}\text{Mn}_x\text{O}_6$ ; thermoelectric properties; thermal conductivity; electrical conductivity; Seebeck coefficient

## 1. Introduction

Ceramics based on cobalt oxides are attractive for many applications [1] because the wide variation in crystal structure, oxygen non-stoichiometry, and valence of Co give rise to a wide range of useful properties [2].  $\text{Ca}_3\text{Co}_4\text{O}_{9+\delta}$  (CCO) is among the best p-type thermoelectric (TE) materials and also a potential cathode material for solid oxide fuel cells [3].  $\text{Ca}_3\text{Co}_2\text{O}_6$  (C326) has a lower TE performance compared to CCO, but is stable up to  $1026 \text{ }^\circ\text{C}$  in ambient air, which is  $\sim 100 \text{ }^\circ\text{C}$  higher than the stability limit for CCO [4,5]. Due to the higher stability, C326 has been studied in order to understand and improve its ferroelectric, magnetic, and thermoelectric properties [6–10]. C326 has the  $\text{A}_3\text{BB}'\text{O}_6$  structure ( $\text{A} =$  alkaline earth and  $\text{B} =$  transition metal or alkaline earth) [8] consisting of chains of alternating face-sharing  $\text{CoO}_6$  octahedra ( $\text{Co}^{1^\circ}$  positions) and trigonal bipyramids ( $\text{Co}^{2^\circ}$  positions) with Ca ions between the chains [11]. The special arrangement of  $\text{Co-O-Co}$  makes C326 a narrow-band semiconductor with strong anisotropy where the charge transport is more dominant in the  $a$ - $b$  plane than along the  $c$  direction [9]. Pure C326 has a positive Seebeck coefficient of about  $170 \mu\text{V}/\text{K}$  reported by Mikami et al. [12] and about  $180 \mu\text{V}/\text{K}$  reported by Iwasaki et al. [13] at  $700 \text{ }^\circ\text{C}$ . C326 has electrical

conductivity of about  $5 \text{ S}\cdot\text{cm}^{-1}$  at  $500 \text{ }^\circ\text{C}$  [14], and at ambient temperature a thermal conductivity of about  $1.7 \text{ W}\cdot\text{m}^{-1}\cdot\text{K}^{-1}$  [8] is reported. Improvements of the properties have been reported by substitution on A(Ca)- and B(Co)-sites and a significant enhancement of the electrical conductivity was observed when 50 at.% of Co was substituted with Ir [8]. A 10 at.% Cu substitution on the Co-site gave a significant improvement in the power factor [13]. Hervoche et al. [11] investigated the effect of Mn substitution on the Co-site in terms of structural and magnetic properties, and found that the crystal structure belongs to the R3c space group with unit cell dimensions of  $9.084 \text{ \AA} < a < 9.134 \text{ \AA}$  and  $10.448 \text{ \AA} < c < 10.583 \text{ \AA}$  for  $\text{Ca}_3\text{CoMnO}_6$  [11]. They also confirmed a solid solution in the entire composition interval ( $0 < x < 1$ ) [11] by using sol-gel synthesis, in contrast to results obtained by solid-state synthesis by Bazuev et al. [15], where an inhomogeneity region at about  $x = 0.5$  was observed [15,16]. For  $\text{Ca}_3\text{CoMnO}_6$ , there is complete filling of  $\text{Co}^{1+}$  by Mn [11]. Hervoche et al. showed presence of cation ordering for the composition with  $x = 1$ , while for those with  $x < 1$  cation disordering [11]. They also state that the Mn has the oxidation state  $4+$ , hence converting the  $\text{Co}^{2+}$  occupancies to  $\text{Co}^{2+}$  [11]. Mikami et al. demonstrated that 10 at.% Mn substitution on the Co-site caused an increase in electrical conductivity in the low-temperature region, but a decrease in the power factor due to a significant reduction of the Seebeck coefficient [12]. High stability of  $\text{Ca}_3\text{Co}_{2-x}\text{Mn}_x\text{O}_6$  for  $0 \leq x \leq 0.25$  has been reported by Golovkin and Bazuev [4].

In our previous work on the CCO- $\text{CaMnO}_3$ -based oxide p-n junction,  $\text{Ca}_3\text{Co}_{2-x}\text{Mn}_x\text{O}_6$  with different contents of Mn were formed at the CCO- $\text{CaMnO}_3$  interface after heat treatment at  $900 \text{ }^\circ\text{C}$  [17]. Furthermore, the CCO- $\text{CaMnO}_3$  oxide p-n junction was also utilized in the recently developed all-oxide TE module, where  $\text{Ca}_3\text{Co}_{2-x}\text{Mn}_x\text{O}_6$  was formed as a reaction product at the CCO- $\text{CaMnO}_3$  p-n junction affecting the electrical conductivity across the junction, as well as boosting the generated voltage across the hot side of the TE module [17].

To the best of our knowledge there are no reports describing the TE properties of  $\text{Ca}_3\text{Co}_{2-x}\text{Mn}_x\text{O}_6$  in the whole composition range ( $0 < x \leq 1$ ) within the temperature range of  $200\text{--}900 \text{ }^\circ\text{C}$ , and we here report a detailed study of the electrical conductivity, thermal conductivity and Seebeck coefficient of  $\text{Ca}_3\text{Co}_{2-x}\text{Mn}_x\text{O}_6$  ( $x = 0.05, 0.2, 0.5, 0.75, \text{ and } 1$ ) materials. The TE properties of this phase may help to understand and optimize performance of all-oxide thermoelectric devices based on CCO and  $\text{CaMnO}_3$  [17].

## 2. Materials and Methods

### 2.1. Materials Synthesis

$\text{Ca}_3\text{Co}_{2-x}\text{Mn}_x\text{O}_6$  powders ( $x = 0.05, 0.2, 0.5, 0.75, \text{ and } 1$ ) were synthesized by the solid-state method using submicron  $\text{CaCO}_3$ ,  $\text{Mn}_2\text{O}_3$  and  $\text{Co}_3\text{O}_4$  precursors from Inframat Advanced Materials, (Manchester, CT, USA, >99% purity). The precursors were first dried at  $120 \text{ }^\circ\text{C}$  for 5 h to remove adsorbed moisture and perform accurate weighing for five different compositions, and then each batch was ball-milled in isopropanol for 8 h using zirconia balls in order to obtain homogeneous mixtures. After drying in a rotavapor (R-210, Büchi, Bern, Switzerland), the powder mixtures were uniaxially pressed into pellets (one for each batch) at 5 MPa and heated at  $1000 \text{ }^\circ\text{C}$  for 10 h in ambient air. After grinding and reheating the pellets using the same procedure, the final powders were prepared by grinding the reheated pellets in a mortar followed by sieving. The final powders were then pressed into bars ( $15 \times 5 \times 2 \text{ mm}^3$ ) and pellets (diameter 12.7 mm, thickness 2.2 mm) by cold isostatic pressing at 200 MPa, and conventionally sintered in ambient air at  $1010 \text{ }^\circ\text{C}$  for 30 h, using heating and cooling rates of  $200 \text{ }^\circ\text{C}/\text{h}$ .

### 2.2. Characterization

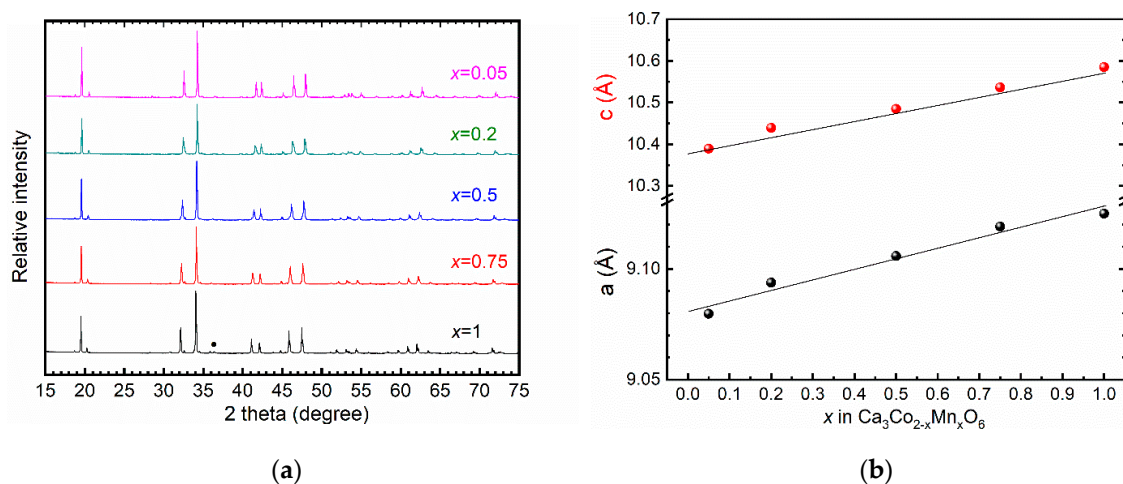
X-ray diffraction (XRD, Bruker, Billerica, MA, USA) of sintered and ground pellets was performed to validate the phase purity of the materials. The data were recorded on a Bruker D8 Advance equipped with a Lynxeye XE detector using a step size of  $0.013^\circ$  and counting 16.9 s/step. Unit cell

parameters of  $\text{Ca}_3\text{Co}_{2-x}\text{Mn}_x\text{O}_6$  were refined using Topas 5 software (Bruker, MA, USA) by Pawley fitting. Morphology and particle size were determined by SEM (S-3400N, Hitachi, Tokyo, Japan). The thermal expansion coefficients (TECs) during heating and cooling were recorded in the range 100–800 °C in ambient air using a dilatometer (DIL 402, Netzsch, Cologne, Germany). The densities of the ceramic samples were measured by the Archimedes method in isopropanol. Thermal conductivity was acquired by the laser flash method (LFA 457 MicroFlash, Netzsch, Cologne, Germany) on pellet-shaped samples [18], while Seebeck coefficient and electrical conductivity were measured on bar-shaped samples using a four-point method [19,20]. All TE data were collected in the temperature range 200–900 °C with steps of 100 °C.

### 3. Results and Discussion

#### 3.1. Materials Characteristics

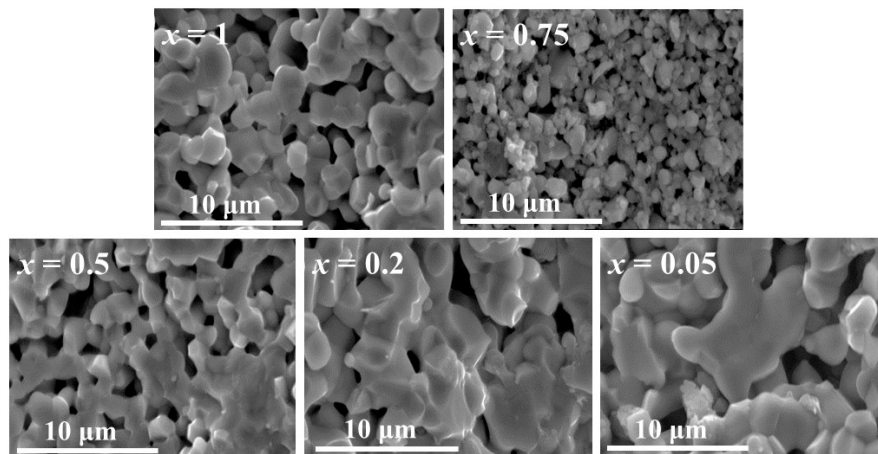
XRD patterns of sintered samples of  $\text{Ca}_3\text{Co}_{2-x}\text{Mn}_x\text{O}_6$  with  $x = 0.05, 0.2, 0.5, 0.75$  and 1 are shown in Figure 1a.



**Figure 1.** (a) XRD patterns of  $\text{Ca}_3\text{Co}_{2-x}\text{Mn}_x\text{O}_6$  ( $x = 0.05, 0.2, 0.5, 0.75$ , and 1) with marked  $\text{Mn}_2\text{O}_3$  peak (●); and (b) cell parameters as a function of  $x$  in  $\text{Ca}_3\text{Co}_{2-x}\text{Mn}_x\text{O}_6$ . Lines represent corresponding data reported by Hervoches et al. for materials prepared by the sol-gel method [11].

Diffraction lines for the target phase  $\text{Ca}_3\text{Co}_{2-x}\text{Mn}_x\text{O}_6$  were indexed according to the reference patterns for the compositions  $\text{Ca}_3\text{CoMnO}_6$  [6],  $\text{Ca}_3\text{Co}_{1.25}\text{Mn}_{0.75}\text{O}_6$  [11],  $\text{Ca}_3\text{Co}_{1.5}\text{Mn}_{0.5}\text{O}_6$  [11],  $\text{Ca}_3\text{Co}_{1.8}\text{Mn}_{0.2}\text{O}_6$  [12] and  $\text{Ca}_3\text{Co}_{1.95}\text{Mn}_{0.05}\text{O}_6$  [14]. Phase-pure materials were obtained showing that by careful synthesis the formation of secondary phases can be avoided, as opposed to the previously published difficulties in obtaining phase pure materials in this system using solid-state synthesis [6,15]. An additional low-intensity diffraction line in the  $\text{Co}_3\text{CoMnO}_6$  ( $x = 1$ ) pattern was observed at  $2\theta \approx 36.5^\circ$ , which corresponds to  $\text{Mn}_2\text{O}_3$ . The variation in cell parameters of  $\text{Ca}_3\text{Co}_{2-x}\text{Mn}_x\text{O}_6$  with increasing  $x$  is in good agreement with the data previously reported by Hervoches et al. [11] according to Figure 1b. The lattice parameters are summarized in Table 1.

Microstructures of the ceramic materials with different  $x$  are presented in Figure 2. An increase in grain coarsening with decreasing Mn-content ( $x$ ) is observed, where the smallest  $x$  resulted in microstructure with the largest grains.  $\text{Ca}_3\text{Co}_2\text{O}_6$  naturally forms non-spherical (polyhedral) grains [14] which predominantly intend to grow more in a-b than in c-direction due to its crystal structure [6]. Hence, the increasing grain size of  $\text{Ca}_3\text{Co}_{2-x}\text{Mn}_x\text{O}_6$  when decreasing  $x$  towards 0 ( $\text{Ca}_3\text{Co}_2\text{O}_6$ ) might result in modifications in grain size and morphology. Furthermore, the microstructures show more inter-connected grains with decreasing  $x$ . Moreover, the microstructure of the material with  $x = 1$  contains larger and more inter-connected grains than the material with  $x = 0.75$ .



**Figure 2.** SEM micrographs of  $\text{Ca}_3\text{Co}_{2-x}\text{Mn}_x\text{O}_6$  fracture surfaces,  $x = 1, 0.75, 0.5, 0.2,$  and  $0.05$ .

**Table 1.** Cell parameters, cell volume, bulk density, thermal expansion coefficient, activation energy and pre-exponential factor of electric conductivity, and figure of merit of sintered  $\text{Ca}_3\text{Co}_{2-x}\text{Mn}_x\text{O}_6$  materials with different Mn content ( $x$ ).

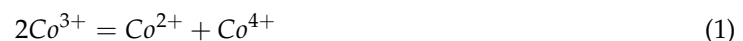
$\text{Ca}_3\text{Co}_{2-x}\text{Mn}_x\text{O}_6$	$x = 1$	$x = 0.75$	$x = 0.5$	$x = 0.2$	$x = 0.05$	$x = 0$
a parameter (Å)	9.1312	9.1192	9.1058	9.0938	9.0797	9.0850 *
c parameter (Å)	10.5793	10.5362	10.4845	10.4391	10.3893	10.3888 *
Cell volume (Å <sup>3</sup> )	763.9	758.8	752.9	747.6	741.8	737.6 *
Bulk density (g/cm <sup>3</sup> )	3.15	3.21	3.26	3.42	3.43	-
Crystallographic density (g/cm <sup>3</sup> )	4.31 *	4.34 *	4.40 *	4.48 **	4.51 **	4.52 *
Relative density (%)	73	73	74	76	76	-
TEC 400–800 °C, ( $10^{-6} \text{ K}^{-1}$ )	19.8	18	19.2	20	20	-
TEC 800–400 °C, ( $10^{-6} \text{ K}^{-1}$ )	19.7	18.2	19.2	19.7	20.7	-
TEC 100–400 °C, ( $10^{-6} \text{ K}^{-1}$ )	14.4	14.8	15.6	16.2	15.9	-
TEC 400–100 °C, ( $10^{-6} \text{ K}^{-1}$ )	15.0	14.5	15.6	15.9	15.8	-
Activation energy $E_a$ (kJ/mol)	-	45.9	38.4	39.0	42.9	50.1 #
$\sigma_0 / 1000$ (S·K/cm)	-	33	73	220	490	1800 #
Figure of merit $zT$ at 900 °C	0.0004	0.006	0.008	0.021	0.020	-

\* Calculated from data by Hervoches et al. [11] and # by Mikami et al. [12]. \*\* Interpolated data.

The bulk densities of the sintered materials were in the range 3.15–3.43 g/cm<sup>3</sup> giving 73 to 76% relative density, using crystallographic densities calculated from Hervoches et al. [11], as summarized in Table 1. TECs of the materials recorded in the temperature intervals 100–400 °C and 400–800 °C during heating and cooling were in the range  $14.4\text{--}16.2 \times 10^{-6} \text{ K}^{-1}$  and  $18\text{--}20 \times 10^{-6} \text{ K}^{-1}$ , respectively (Table 1).

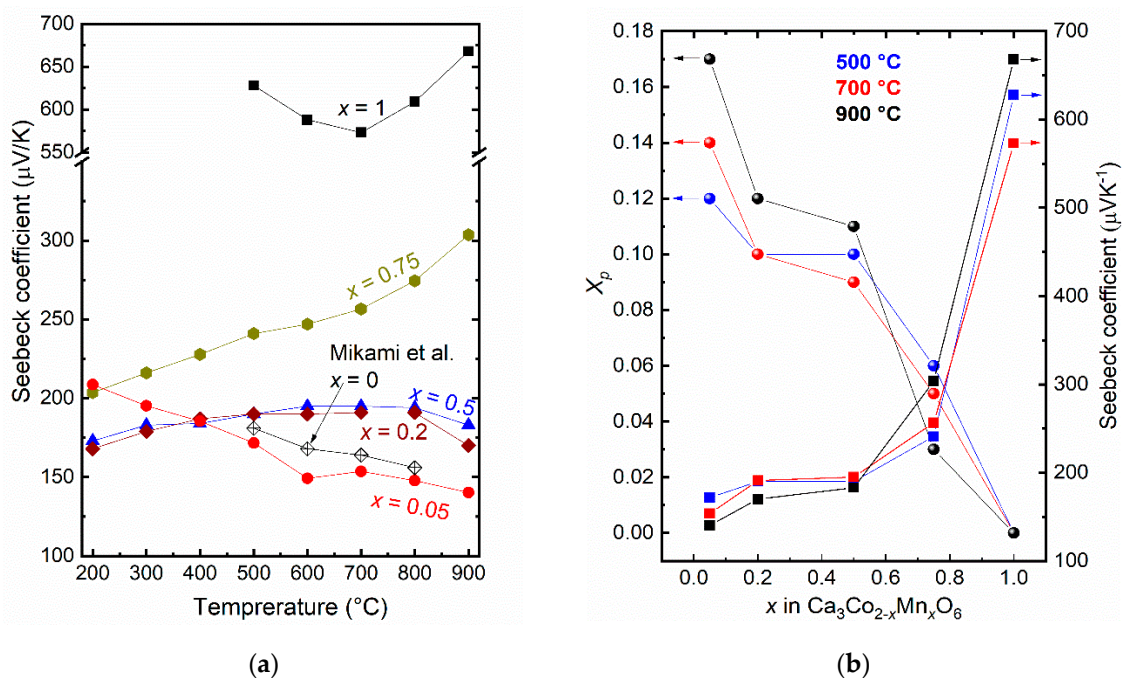
### 3.2. Thermoelectric Properties

The Seebeck coefficients of  $\text{Ca}_3\text{Co}_{2-x}\text{Mn}_x\text{O}_6$  are presented as a function of temperature and  $x$  in Figure 3a,b, respectively. They are all positive, showing predominantly p-type conductivity for all conditions and compositions. The Seebeck coefficient increases with increasing  $x$  while it is to a first approximation not very affected by temperature, at least for the  $x \leq 0.5$  samples. This suggests that charge carriers are not generated by a thermally activated process, but present in the form of partially filled states connected to cobalt, or by a reaction such as



(disproportionation) being driven to complete disorder by having a negligible enthalpy. This will give a fraction of  $\text{Co}^{4+}$ , representing electron holes, not higher than 1/3 ( $\text{Co}^{4+}$  over all  $\text{Co}^{3+} + \text{Co}^{4+}$ ),

and more reasonably somewhat lower by e.g., only one of the two Co sites disproportionated or degeneracy by spin or coupling to Co–O bonds.



**Figure 3.** Seebeck coefficient of  $\text{Ca}_3\text{Co}_{2-x}\text{Mn}_x\text{O}_6$  as a function of (a) temperature and (b)  $x$  at selected temperatures. Data for  $\text{Ca}_3\text{Co}_{2-x}\text{Mn}_x\text{O}_6$  ( $x = 0$ ), from Mikami et al. [12], are included for comparison. Figure 3b includes a plot of  $X_p$  (left hand axis) based on Equation (2), which is calculated from Seebeck coefficients at 500, 700, and 900 °C.

We shall see that the electrical conductivity indicates a hopping mobility of charge carriers, and we may therefore apply Heikes' formula [21] to get a first approximation of the fraction of Co from  $\text{Co}1^\circ$  site contributing to the p-type conductivity based on the Seebeck coefficients:

$$S = \frac{k_B}{e} \ln\left(\frac{1 - X_p}{X_p}\right) \quad (2)$$

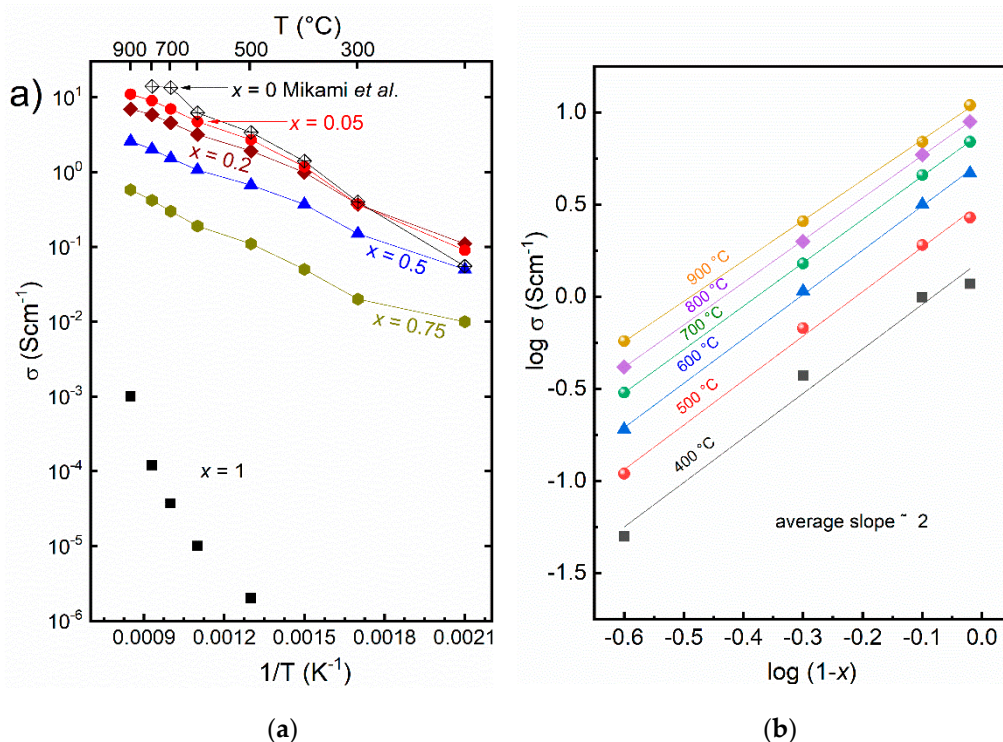
Here, the Seebeck coefficient  $S$  is a function of Boltzmann's constant  $k_B$ , the (elementary) charge of the charge carrier (holes)  $e$ , and the fraction of Co from  $\text{Co}1^\circ$  site contributing to the p-type conductivity  $X_p$ . Figure 3b (left hand axis) shows the apparent fraction of holes  $X_p$  based on data at 500, 700, and 900 °C, starting with reasonable values in the range  $1/8$ – $1/6$  for the Co-rich compositions ( $x = 0.05$ ) and decreasing quite linearly with  $x$  and approaching zero for  $x = 1$ . From this we may state quite unambiguously that the charge carrier (hole) concentration is directly proportional to  $1 - x$ , i.e., the concentration of Co on the  $\text{Co}1^\circ$  site. Ideally, the  $x = 1$  composition must then generate its charge carriers by a different, e.g., thermally activated mechanism.

Figure 4 shows an Arrhenius plot of the electrical conductivity of  $\text{Ca}_3\text{Co}_{2-x}\text{Mn}_x\text{O}_6$  which increases in a simple activated manner with increasing temperature for all compositions  $x < 1$ . In combination with the high, un-activated concentrations of charge carriers deduced from the Seebeck coefficients, it is reasonable to interpret the activated conductivity in terms of a small polaron hopping model [22]:

$$\sigma = \frac{\sigma_0}{T} \exp\left(-\frac{E_a}{RT}\right) \quad (3)$$

Accordingly, fitting  $\ln(\sigma T)$  vs.  $1/T$  (not shown) yields pre-exponentials  $\sigma_0$  and activation energies  $E_a$ , and these are included in Table 1. The activation energies fall in the range  $44 \pm 6$  kJ/mol, fairly

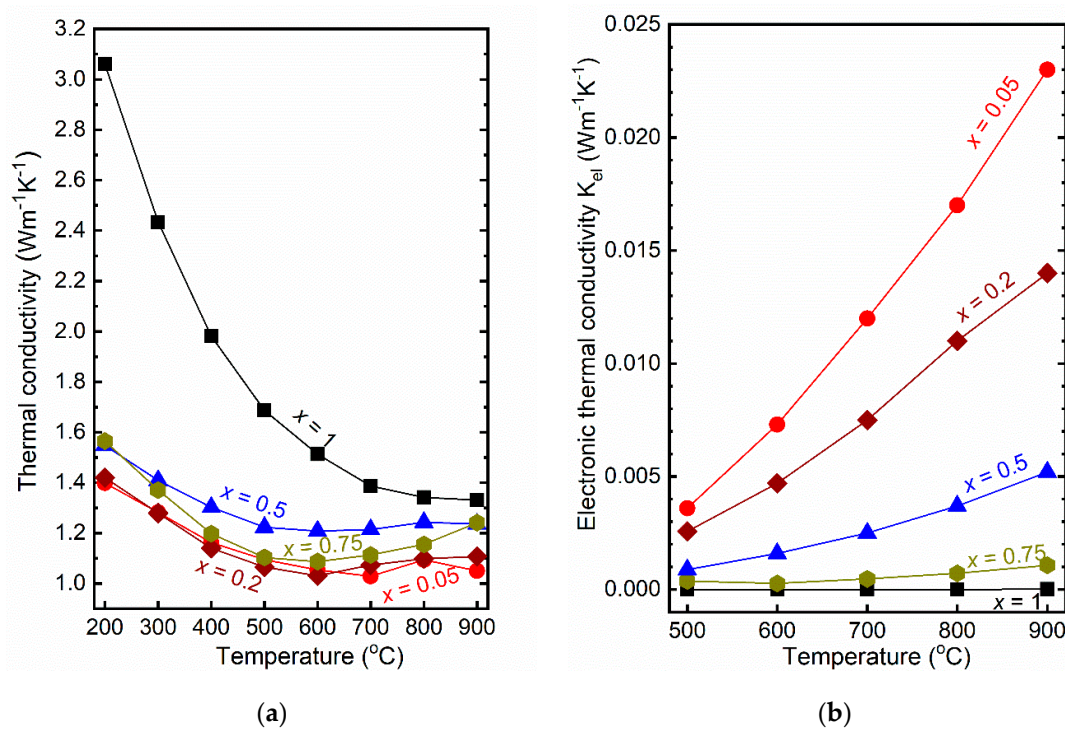
independent of composition for  $x < 1$ , and we suggest that this may be attributed to the barrier of electron hole hopping between Co sites.



**Figure 4.** (a) Arrhenius plot of electrical conductivity of  $\text{Ca}_3\text{Co}_{2-x}\text{Mn}_x\text{O}_6$  versus  $1/T$ . The data for  $\text{Ca}_3\text{Co}_{2-x}\text{Mn}_x\text{O}_6$  ( $x = 0$ ) are from Mikami et al. [12]. (b) Double-logarithmic plot of isothermal conductivities from 400 to 900 °C versus  $(1 - x)$  suggesting a slope of 2 at the higher temperatures.

The pre-exponential  $\sigma_0$  increases with decreasing  $x$ , as expected from the behavior of the concentration of charge carriers deduced from the Seebeck coefficient. However, plots of the pre-exponential, or more sensibly, isothermal conductivities, versus  $1 - x$  do not yield simple linear relationships. Figure 4b is a double-logarithmic plot suggesting a slope of 2, i.e., the conductivity is proportional to  $(1 - x)^2$ . Since we have already concluded that the concentration of charge carriers is proportional to  $1 - x$ , the square dependency suggests further that also the charge mobility is proportional to  $1 - x$ . This is quite reasonable; the electron holes can jump on  $\text{Co}^{1^\circ}$  but not  $\text{Mn}^{1^\circ}$  occupants. Alternatively, one may take the broader approach that the  $\text{Mn}^{4+1^\circ}\text{-Co}^{2+2^\circ}$  combination—unlike the  $\text{Co}^{3+1^\circ}\text{-Co}^{3+2^\circ}$  combination—cannot host hole jumps. The  $x = 1$  composition is left with a low and in the ideal case activated concentration of charge carriers—giving the high Seebeck coefficient of around  $600 \mu\text{V}/\text{K}$ —while the mobility becomes low and the resulting conductivity very low.

The thermal conductivity of  $\text{Ca}_3\text{Co}_{2-x}\text{Mn}_x\text{O}_6$  given in Figure 5a decreases with increasing temperature for all materials. The material with  $x = 1$  reveals the highest thermal conductivity of about  $3 \text{ W}\cdot\text{m}^{-1}\cdot\text{K}^{-1}$  at 200 °C, while  $1 \text{ W}\cdot\text{m}^{-1}\cdot\text{K}^{-1}$  at 600 °C represents the lowest value, obtained for  $x = 0.2$ . In spite of similar relative porosities, the composition with  $x = 1$  demonstrated significantly higher thermal conductivity than the other materials. This may be attributed to the ordered cation arrangement at  $\text{Co}^{1^\circ}$  for  $\text{Ca}_3\text{CoMnO}_6$  ( $x = 1$ ) [11] as opposed to the Co-Mn disorder in the solid solutions of  $0 < x < 1$ .



**Figure 5.** (a) Thermal conductivity of  $\text{Ca}_3\text{Co}_{2-x}\text{Mn}_x\text{O}_6$ ,  $x = 0.05, 0.2, 0.5, 0.75$ , and  $1$  as a function of temperature; and (b) calculated electronic thermal conductivity as a function of temperature.

In general, thermal conductivity is the sum of electronic,  $\kappa_{el}$ , and phonon,  $\kappa_p$ , (lattice) thermal conductivities, where the electronic part can be calculated by Equation (4)

$$\kappa_{el} = \sigma TL \quad (4)$$

where  $\sigma$  is the total electrical conductivity ( $\text{S}\cdot\text{cm}^{-1}$ ),  $T$  absolute temperature (K) and  $L$  is the Lorenz number ( $\text{W}\cdot\Omega\cdot\text{K}^{-2}$ ) [23] which can be calculated by Equation (5)

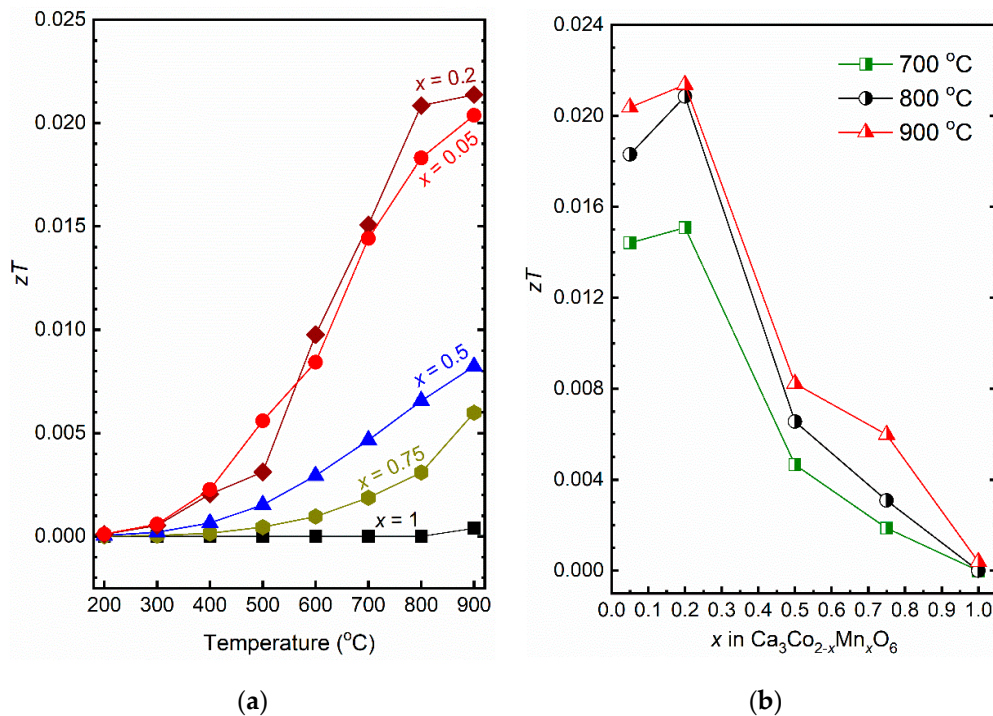
$$L = 1.5 + \exp\left(-\frac{|S|}{116}\right) \quad (5)$$

where  $S$  represents the Seebeck coefficient [24]. The calculated electronic part of the thermal conductivity of  $\text{Ca}_3\text{Co}_{2-x}\text{Mn}_x\text{O}_6$  as a function of temperature presented in Figure 5b is increasing with decreasing  $x$  and temperature in accordance with the relative variation in electronic conductivity. The highest electronic thermal conductivity is observed at  $900\text{ }^\circ\text{C}$  for  $x = 0.05$ , which represents only 2% of the total thermal conductivity, the rest being dominated by the phonon contribution.

The figures of merit ( $zT$ ), calculated from Equation (6)

$$zT = \frac{\sigma S^2 T}{\kappa} \quad (6)$$

are presented in Figure 6a. The  $zT$  values increased with increasing temperature and the highest value of 0.021 was obtained for  $x = 0.2$  at  $900\text{ }^\circ\text{C}$ , due to a combination of relatively low thermal conductivity and high electrical conductivity as well as a moderate Seebeck coefficient.



**Figure 6.** (a) Figure of merit  $zT$  of  $\text{Ca}_3\text{Co}_{2-x}\text{Mn}_x\text{O}_6$ ,  $x = 0.05, 0.2, 0.5, 0.75$ , and  $1$  as a function of temperature and (b) as a function of  $x$  in  $\text{Ca}_3\text{Co}_{2-x}\text{Mn}_x\text{O}_6$  at  $700, 800$  and  $900$   $^{\circ}\text{C}$ .

The  $zT$  values as a function of  $x$  presented in Figure 6b decrease with increasing  $x$  in the temperature range of  $700$ – $900$   $^{\circ}\text{C}$ . The material with  $x = 0.2$  demonstrated a promising  $zT$  value which probably can be further improved by using alternative synthesis methods (such as sol-gel or spray pyrolysis) followed by e.g. spark plasma sintering to obtain smaller grains and a further reduction in thermal conductivity due to enhanced phonon scattering at grain boundaries. The porosity of the materials will also influence the thermal and electrical conductivity. Pore size and distribution as well as type of pores could be tailored in such a way to reduce thermal conductivity more than the power factor, to enhance  $zT$  [25]. Designing a continuous mesoporous nanocrystalline framework seems to be a promising solution [25].

#### 4. Conclusions

Phase pure  $\text{Ca}_3\text{Co}_{2-x}\text{Mn}_x\text{O}_6$  materials with  $x = 0.05, 0.2, 0.5, 0.75$ , and  $1$  were prepared by a solid-state synthesis method. Cold isostatic pressing followed by conventional sintering resulted in relative bulk densities in the range of  $73$ – $76\%$  of theoretical. The Seebeck coefficient shows that the materials are p-type conductors, seemingly by holes from fully disordered Co oxidation states. This concentration hence decreases with  $x$  and the Seebeck coefficient correspondingly increases and reaches values well above  $600$   $\mu\text{V}/\text{K}^{-1}$  for  $\text{Ca}_3\text{CoMnO}_6$  at high temperatures. For  $x < 1$ , the electrical conductivity is consistent with small polaron hopping with an activation energy of mobility of  $44 \pm 6$   $\text{kJ}/\text{mol}$ . The conductivity increases with decreasing  $x$ , reaching above  $10$   $\text{S}\cdot\text{cm}^{-1}$  at  $900$   $^{\circ}\text{C}$  for  $x \leq 0.05$ . It appears that the conductivity is proportional to  $(1 - x)^2$ , which suggests that both the concentration and mobility of charge carriers are proportional to the Co content on the  $\text{Co}1^{\circ}$  site  $(1 - x)$ , where the electron holes can jump on  $\text{Co}1^{\circ}$  sites but not  $\text{Mn}1^{\circ}$  sites. Thermal conductivity is dominated by phonon transport, with only minor electronic contribution. The figure-of-merit increased with decreasing Mn-content ( $x$ ) till a maximum at  $x = 0.2$  of  $zT = 0.021$ . While this is in itself modest, the thermodynamic stability and in situ formation of  $\text{Ca}_3\text{Co}_{2-x}\text{Mn}_x\text{O}_6$  between  $\text{Ca}_3\text{Co}_{4-y}\text{O}_{9+\delta}$  and  $\text{CaMnO}_{3-\delta}$  open for new geometries and designs of oxide-based thermoelectric generators.



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