



Computational Analysis of a Drag reducing Cone Grid

*A finite volume simulation of the gecko's
aerodynamic skin*

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As I finish my education, I find there are no shortage of people to thank. So in order of abstract proximity, I wish to thank...

... my supervisor, Mikael Mortensen, for guidance and patience both during this thesis and in many of the related subjects I have studied.

... my co-supervisor, Murat Tutkun, for the experimental work that this thesis is based upon, and for lending me his experience and insight.

... the rest of the professors at the university, for responding to stupidity with wisdom.

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...my family. For their always loyal support.

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Abstract

A recent study at the University of Illinois [1], inspired by the skin of geckos, explored the benefits of introducing a grid of cones to a airfoil and if this could possibly have effects that reduce the drag forces over a surface. The implications of this are enormous, as energy loss due to drag forces are a major issue for all movement on earth, becoming more and more problematic as the velocity increase. Any method to conclusively reduce this drag, even if only by a small amount, would be able to save untold amounts of fuel with all the environmental and economic benefits that would entail.

This thesis aims to explore is whether or not the introduction of a grid of cones like the one used in the aforementioned study can create an beneficial drag reducing phenomena for a surface. To accomplish this we perform a comparison of a surface with and without a cone grid using Computational Fluid Dynamics techniques. The problem is constrained into a simplified situation more suited for study, in this case a recycled channel flow, and the volume within is then discretized into a mesh of finite cells. Then the Navier-Stokes equations are solved for the entire domain, using Large Eddy Simulation and the Spalart-Allmaras turbulence model.

The results are negative, as we see that the cone grid suffers a higher drag coefficient than a corresponding flat plate, both for a slow laminar flow and for a high velocity turbulent flow. While there is a negligible difference between the two in the laminar case, the turbulent case see an increase in the average drag coefficient by 286% by adding the cones. The vortexes formed are discussed in detail, and possible error sources are discussed in detail.

A script for easily generating a cone grid mesh has also been developed and is added to the attachments, to make it easier for any later reproduction studies, if applicable.

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Introduction

This is a one-semester thesis, finishing a Masters Degree in Applied Mathematics and Fluid dynamics at the University of Oslo autumn 2017.

Researchers with the University of Illinois [1] has recently done a experimental study linking a grid system of cones covering an airfoil to a total decrease in drag force over the airfoil as a result of a change in flow separation. This was inspired by biological textures found on the surface on the skin of geckos, a field of study that may have untapped potential.

One of the many implications of that study are that a flat plate covered with this texture may have a lower total aerodynamic drag than a perfectly plain flat plate. If this is true, it could potentially have enormous ramifications for all objects in the world moving fast enough that drag force becomes a non-negligible issue.

To explore this I have constrained the problem into a testable and quantifiable experiment that I analyze using Computational Fluid Dynamic techniques. I first define a open channel covered with walls only on the top and bottom, then let the inlet, outlet and sides be infinitely recycled until we approach a steady or semi-steady state. To avoid the loss of energy, I add a source term to the momentum equation designed to keep the mean velocity of the entire volume constant.

I then run 4 separate experiments where I first solve the case for a low velocity laminar flow in a plain channel; then the same flow velocity but with the bottom of the channel covered with the cone grid; then a high velocity, turbulent flow in a empty channel; and a high velocity flow with a cone covered channel. These 4 cases are then directly compared, to get a understanding of the benefits from covering or not covering the bottom plate with the texture.

I then discuss how the results can be evaluated, what potential weaknesses may be inherent in my approach, and how to mitigate them. Finally I summarize the results in a conclusion, and looks at how they compare with my expectations.

As a attachment I have provided a script I designed to generate the mesh I ended up using.

Method

Basic problem definition

We are here focusing on one essential question:

Is it possible that by adding a cone grid to a flat plate we could decrease the total amount of drag force on the plate as a fluid flows over it?

To answer this it is essential to run two kinds of simulations: One with a perfectly flat plane, and one with a coned surface. These two cases can then be compared directly. In a perfect world we would research this for a infinite plane, with a infinite fluid flowing over it. Further more, we would like to achieve perfect knowledge of the drag development for all fluids and for all velocities. This is obviously problematic, as my resources are generally not described as “infinite” by anyone with a basic understanding of both mathematics and my wallet.

So in order to better solve this problem we constrict our approach to a few useful approximations. First of all, we only investigate the flow for a single fluid with a constant viscosity, similar to the one in the experimental study.

Secondly, we only investigate two velocities: A laminar flow with a Reynolds number of 10^3 ; and a high velocity turbulent flow with a Reynolds number of 10^5 . This gives us 4 discrete cases that can be directly compared with each other. The Reynolds number is a dimensionless number that gives a comparison between the inertia and viscous forces in a system, and a high number (above ~ 3000) is traditionally an indicator of possible turbulence.

Third, we only investigate a finite section of the infinite plate, and only a finite volume above it. To keep our simulation accurate, we impose a recycling condition on the boundary of this finite space as we move over the plate, effectively letting us follow the flow of fluid further and further downstream as it develops into what we hope to be a semi-steady state. To keep the flow controlled, we introduce a upper wall and effectively create a open channel flow. Introducing a coned grid will place $85\ \mu\text{m}$ high obstacles on the bottom, which we expect to constrict the inlet. My co-supervisor Tutkun advised me to keep this constriction below 3%, prompting us to set the total height of the channel to $3000\ \mu\text{m}$.

Fourth, we discretize the volume into a mesh of finite volume cells, and apply Computational Fluid Dynamic techniques to numerically solve the Navier-Stokes equations for the mesh.

The end result is a solution that is achievable, testable, and evaluable.

Description of the numerical method

Computational Fluid Dynamics involves numerically approximating the Navier-Stokes equations on a discretized domain. In this case, we are using the finite volume method, built into the open-source program OpenFoam.

The full Navier-Stokes equations are incredibly computationally expensive to solve due to the incredible amount of small turbulent vortexes, so we make use of a system called Large Eddy Simulation. With this system only the large vortexes are fully computed, and the effects of the smaller vortexes are simply modeled. The equations are further simplified by assuming that the fluid will behave as incompressible. Equation 1 shows us the LES momentum equations, with reference to the thesis by E. Villiers [2], where \bar{u} is the filtered velocity field vector; \bar{p} is the filtered pressure field; ν is the viscosity; ρ is the density; and τ is the sub grid-scale stress tensor.

$$1) \frac{\partial \bar{u}}{\partial t} + \nabla \cdot (\bar{u} \bar{u}) = \frac{-\nabla \bar{p}}{\rho} + \nabla \cdot \nu (\nabla \bar{u} + \nabla \bar{u}^T) + \nabla \cdot \tau, \quad \nabla \cdot \bar{u} = 0$$

To calculate the turbulence I make use of the Spalart-Allmaras DDES model, a model originally designed to be used for high turbulence aerodynamics. Since this model has grown steadily in popularity it became my first choice. I also made some attempts at using a Smagorinsky-Lilly model, but I found the Spalart-Allmaras model converged much more reliably. Equation set 2 shows how the eddy viscosity (ν_t) is connected to a Spalart-Allmaras variable ($\tilde{\nu}$). The constants are: $c_{b1} = 0.1355$, $c_\sigma = 2/3$, $c_{b2} = 0.622$, $\kappa = 0.41$, $c_{w1} = c_{b1}/\kappa^2 + (1 + c_{b2})/c_\sigma$, $c_{w2} = 0.3$, $c_{w3} = 2$, $c_{v1} = 7.1$; and ω is the vorticity magnitude.

$$2) \frac{D\tilde{\nu}}{Dt} = c_{b1} \tilde{S} \tilde{\nu} + \frac{1}{c_\sigma} [\nabla \cdot ((\nu + \tilde{\nu}) \nabla \tilde{\nu}) + c_{b2} (\nabla \tilde{\nu})^2] - c_{w1} f_w \left(\frac{\tilde{\nu}}{y_w}\right)^2, \quad \tau = \nu_t (\nabla \bar{u} + \nabla \bar{u}^T),$$

$$\nu_t = \tilde{\nu} f_{v1}, \quad f_{v1} = \frac{X^3}{X^3 + c_{v1}^3}, \quad X \equiv \frac{\tilde{\nu}}{\nu}, \quad \tilde{S} \equiv \omega + \frac{\tilde{\nu}}{\kappa^2 y_w^2} f_{v2}, \quad f_{v2} = 1 - \frac{X}{1 + X f_{v1}},$$

$$f_w = g \left(\frac{1 + c_{w3}^6}{g^6 + c_{w3}^6}\right)^{\frac{1}{6}}, \quad g = r + c_{w2} (r^6 - r), \quad r = \frac{\tilde{\nu}}{\tilde{S} \kappa^2 y_w^2}.$$

The numerical differential schemes used in the simulations:

Reference for the schemes are the OpenFoam User Guide [3] and an analysis by Hrvoje Jasak [4].

Time differential terms: *Backwards* difference. This is a second order implicit scheme.

Gradient terms: *Cell limited Gauss Linear 1* for velocity and turbulent viscosity, and *Gauss Linear* for everything else. *Cell limited <SCHEME> 1* means that some accuracy is sacrificed for stability. *Gauss <SCHEME>* means that the scheme makes use of Gaussian integration and *linear* means that a central difference interpolation is used.

Divergence terms: *Gauss LUST unlimitedGrad(U)* for velocity and *Gauss limitedLinear 1* for the Spalart-Allmaras variable. LUST refers to a mixed 75% linear scheme and 25% linear upwind scheme. *limitedLinear 1* refers to the TVD scheme and the Sweby limiter function.

Gradients normal to the Surface: *limited corrected 0.33*. Since this is a unstructured mesh, orthogonality is a issue and we use a non-orthogonal correction term. This term is then modified with a relaxation factor of 33%.

Laplacian terms: *Gauss linear limited corrected 0.33*. This takes the form of *Gauss <interpolation scheme> <surface gradient scheme>*, both of which are mentioned above.

Point to point Interpolation: *Linear*. This refers to what is commonly known as central difference.

The equation set is then solved using the PISO algorithm.

Detailed description of the cones used

The cones are placed in a 3D Cartesian system with exactly 120 μm between each cone in both x and y directions. The cones have a diameter of 40 μm at the bottom, are 85 μm tall, and starts expanding at $z=65$ μm to a diameter of 85 μm at the top. This is visualized by Figure 1.

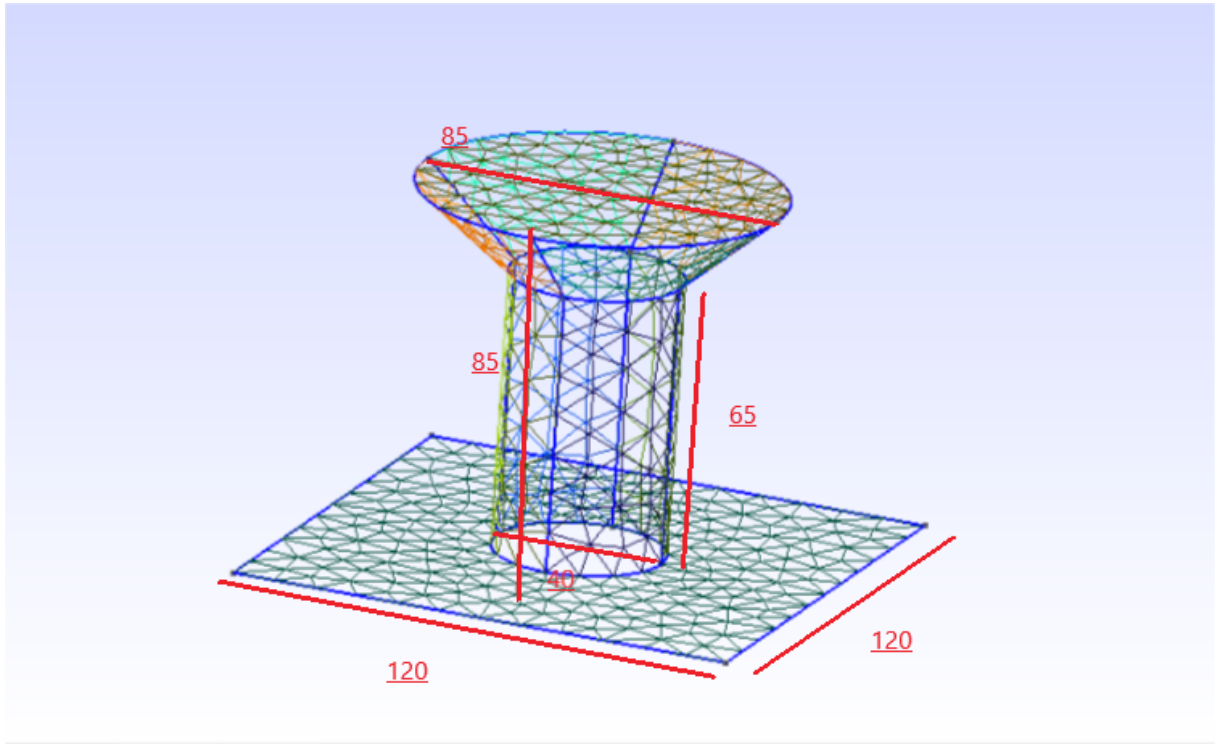


Figure 1: Sketch of a cone. All dimensions are in μm .

Description of the boundary conditions used

The numerical model we have chosen to use requires us to define boundary conditions for 4 variables at all boundaries and for the internal condition: Velocity vector (\mathbf{U}), pressure (P), Turbulent viscosity (ν_t), and the Spalart-Allmaras variable ($\tilde{\nu}$).

Note that the viscosity of the fluid (ν) is chosen as $0.0000011 \text{ m}^2/\text{s}$, in accordance with the experimental study this thesis is based on.

Initial condition for the internal volume:

\mathbf{U} : 0.367 m/s in the x direction for the laminar case, and 36.7 m/s for the turbulent case. This is chosen in order to get a Reynolds number of 10^3 and 10^5 respectively, with a characteristic height of the channel as 0.003 m and a viscosity of $0.0000011 \text{ m}^2/\text{s}$.

P : 0 at all points. As the absolute pressure is irrelevant to an incompressible fluid, only the relative value as the simulation progresses is relevant.

ν_t : $0.00002 \text{ m}^2/\text{s}$ on each point. Irrelevant for the laminar solution, and for the turbulent solution it is chosen as twice the size of the fluid viscosity, to ensure that the simulation would

“start up” fully turbulent.

\tilde{v} : 0.00002 m²/s on each point, using the same argument as v_t .

In addition, the *fvOptions* function in *OpenFoam* is used to apply a source term to the momentum equation of the type *meanVelocityForce*. This is a function specifically designed to keep the average velocity constant, and is required to avoid the system from losing energy over time. The values here mimic the start condition, being 0.367 m/s in the x direction for the laminar case and 36.7 m/s for the turbulent case.

Inlet and outlet boundaries

I will refer to the boundary at $x=0$ as inlet, even through a cyclic simulation technically does not have a inlet. The boundary at $x=1440 \mu\text{m}$ is likewise refereed to as an outlet.

U: Cyclic, referring to the opposite side. The cyclic condition (often called “periodic”) refers each cell to a similar cell at the opposite boundary, and matches the values as if they where placed adjacent to each other. This allows us to reuse the same domain infinitely, as whatever flow pattern leaves at the outlet returns at the inlet.

P: Cyclic, referring to the opposite side.

v_t : Cyclic, referring to the opposite side.

\tilde{v} : Cyclic, referring to the opposite side.

Side boundaries

The sides at $y=0$ and $y=720 \mu\text{m}$ are refereed to the left and right sides, and like the inlet and outlet they are both cyclic and referring to each other.

U: Cyclic, referring to the opposite side. The cyclic condition refers each cell to a similar cell at the opposite boundary, and matches the values as if they where placed adjacent to each other. This allows us to reuse the same domain infinitely, as the inlet flow corresponds to whatever form the outlet currently have.

P: Cyclic, referring to the opposite side.

v_t : Cyclic, referring to the opposite side.

\tilde{u} : Cyclic, referring to the opposite side.

Walls

These boundary conditions refer to both the top wall, the bottom wall, and the surface of the cones.

U: No-slip condition. Due to the friction at the wall, we assume that the velocity of the fluid relative to the wall approach zero at the boundary.

P: Zero-gradient. We are assuming that the wall press back towards the fluid with the same force the fluid press into the wall.

ν_t : `nutUSpaldingWallFunction`. This is a wall function that estimates what the turbulent viscosity should be, based on Spalding's work on creating a enchanted version of the “law of the wall” [5].

\tilde{u} : 0. Similar to the no-slip condition, this value should always be zero at the wall.

Description of the mesh

A detailed script used for generating the mesh in the program *GMSH* is attached at the end of this thesis.

The mesh is defined by 4 parts. First of all, we have the cones themselves. In order to control the relative location of the cones and the volume surrounding them, each cone is placed inside a cube of $120\mu\text{m} \times 120\mu\text{m} \times 120\mu\text{m}$. The cell size in this cube can then be assigned at all points individually, and after a long series of experiments and readjustments I ended up using $5\mu\text{m}$ cells on the top of the cones, $20\mu\text{m}$ cells on the top of the cube surrounding the cone, and $10\mu\text{m}$ everywhere else inside the cube. This cube is then copied in x and y direction into a 12×6 grid. The end result is visualized by Figure 2.

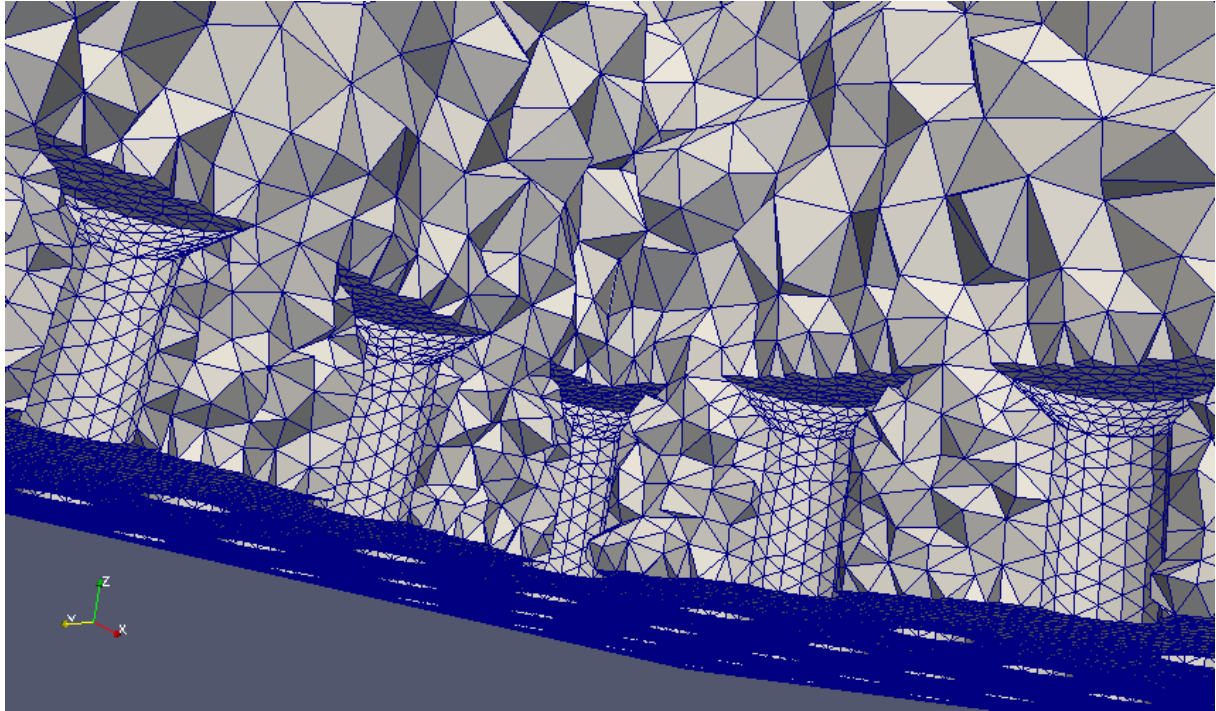


Figure 2: A visualization of the grid density surrounding the cones. The slicing is done using a "crinkle clip" function in the program ParaView, meaning that the cut follows the cell faces and thus gives a great representation of the actual mesh density.

To fill the rest of the channel, it is now a matter of attaching a large empty volume on top of the grid surface. But because we want to control the cell size in different parts of the channel, we divide this into 3 parts. The second part is a 700 μm high cuboid placed on the top of the grid. The mesh size is here 20 μm at the bottom and 40 μm at the top. This represents a boundary layer where the velocity increases as we move farther away from the wall. The final decision of using a 700 μm distance was made based on a series of early iterations of the simulation. Figure 3 visualizes the setup.

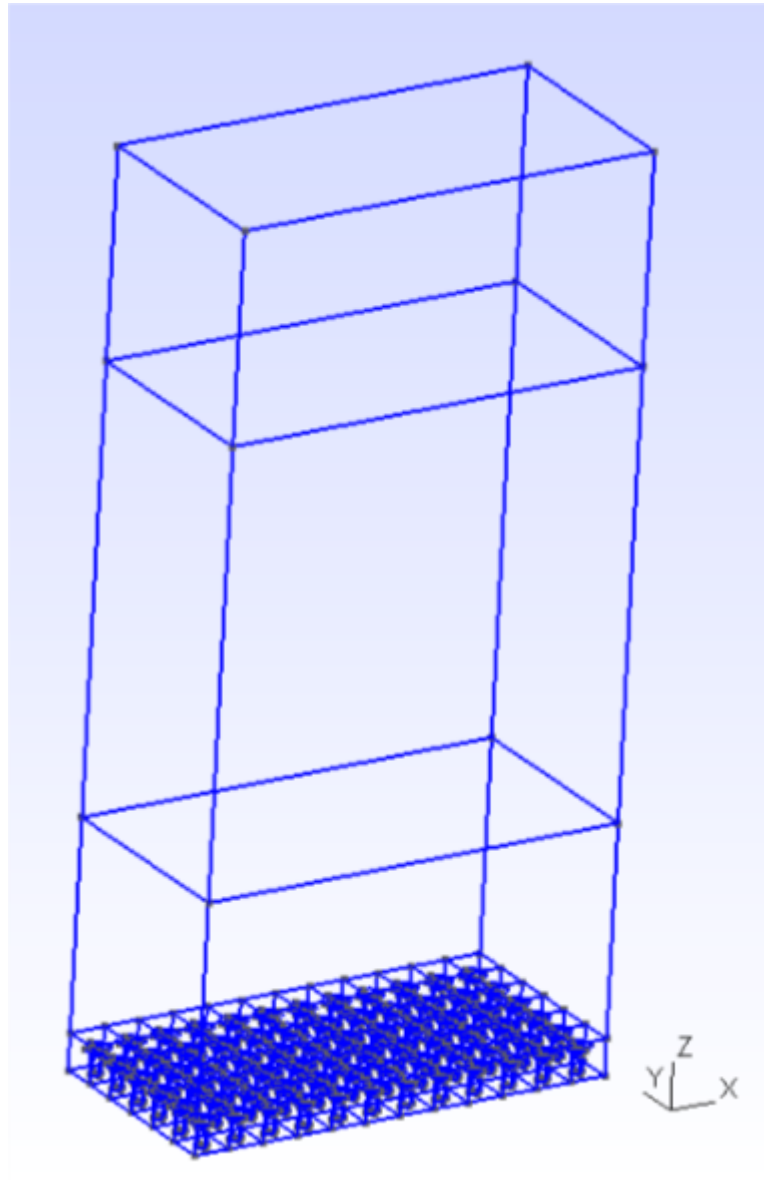


Figure 3: A conceptual sketch visualizing the different parts the mesh is built up from.

The third part of the mesh represents the main section of the flow and have a cell size of $40\ \mu\text{m}$ everywhere. It is placed on top of the lower boundary layer section and is bounded by a symmetric boundary layer section on the top wall.

The fourth and final part is a boundary layer towards the top wall, placed on top of the main flow section. It is defined symmetrically to the lower boundary layer, and thus is $700\ \mu\text{m}$ high with a cell size starting at $40\ \mu\text{m}$ and ending in $20\ \mu\text{m}$. The final distribution of cell size is visualized in Figure 4.

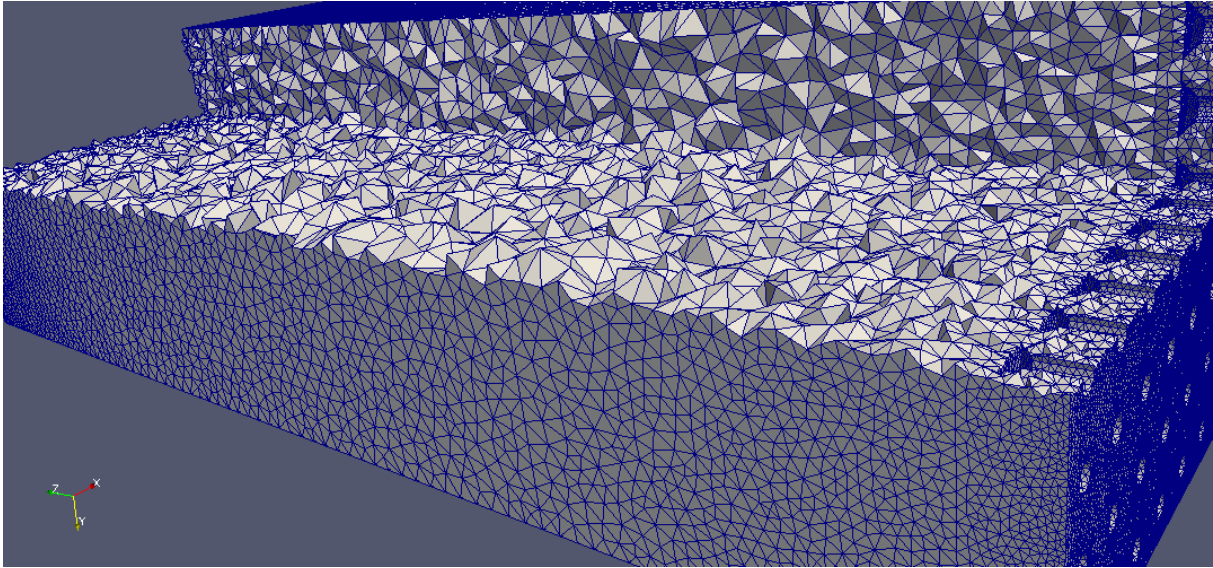


Figure 4: A visualization of the cell density in the mesh. The slicing is done using a "crinkle clip" function in the program ParaView, meaning that the cut follows the cell faces.

Calculation of Drag Coefficient

We can imagine the drag force as the wall's resistance to the movement of the fluid. The drag force also generates vortices, and results in a large loss of energy over time. It is a huge issue in fluidmechanics, as reducing it could save unimaginative amounts of energy on a global scale.

For our purposes we shall investigate this by evaluating the Drag Coefficient, defined in Equation 3 as the drag force (F_D) relative to the area the drag is applied to (A), the density (ρ), and the velocity of the fluid (U). It is important at this point to note that when the cone grid is applied to the flat surface, the area of contact increase with the size of the cones. I want to make clear that I will be using the same reference area for calculation of the drag coefficient for both the flat plate and the cone grid, in order to compare the two correctly, even as the cones technically has a much larger area of contact with the fluid.

$$3) C_D = \frac{2 F_D}{U^2 A \rho}$$

Openfoam has a built in function called *forceCoeffs* that handles the detailed calculation for a selected boundary, that I made use of to generate the results in the next chapter.

Lastly, I have been overly cautious regarding the appearance of numerical artifacts at the

boundaries. While I in retrospect believe these effects were less of an issue now than I did in the start of the project, I have consistently been avoiding using the outermost layer of cones for the calculation of the drag coefficient. While this does in no way introduce any errors, I doubt this actually removed any either, and it may have made the final result slightly more sensitive to stochastic fluctuations since the reference area is smaller.

Evaluation and eventual rejection of other approaches

The generation of the mesh and proper density of it was a large issue especially in the start of the project. My original approach was to use a program called *FreeCAD* to generate *stl* files of the boundaries, then use the program *snappyHexMesh* built into *OpenFoam* to generate a mesh. While this approach had a lot of benefits it had a major weakness: It would generate approximations on the corners of the mesh, giving rounded corners with non-plane cyclic boundaries. This generated inherent errors that made the approach non-feasible.

For the mesh itself I originally made attempts at generating a long channel with a traditional inlet and outlet, but this approach proved unfeasible for a number of reasons, most prominently the enormous computational cost it would require.

Attempts were also made at making a high density mesh of only a few cones and a lower channel roof, solved using the Smagorinsky–Lilly turbulence model, and compare this with the other results. It was unfortunately prone to severe convergence problems, and I ultimately ended up not having the resources (time) to spare.

Results

The results are presented in 2 sections: A laminar model with a Reynolds number of 10^3 ; and a LES simulation using the Spalart-Allmaras turbulence model of Reynolds number of 10^5 .

For each section we analyze the measured drag coefficient, the velocity profile, and visualize the solution.

For the turbulent case we also take a more detailed look into the behavior of the vortexes.

Laminar model

A mean velocity of 0.367 m/s in the x direction was used to give a Reynolds number of 10^3 for the channel flow. then two simulations was run: One with a 12x6 cone grid pattern, and one with a empty channel. Both where run with a PISO algorithm with a time step difference of $10 \mu\text{s}$, starting from a channel with uniform velocity.

Figure 5 shows the evolution of the measured drag coefficient as a function of time. This is a laminar solution, so we expect to tend towards a steady state as time tends towards infinity. Due to the lack of infinite time, however, we stop the simulation after 1 full second, where the simulation has asymptotically approached it's steady state. While it is possible to continue, we already clearly see that the flat plate has a lower drag coefficient than the coned grid for this Reynolds number.

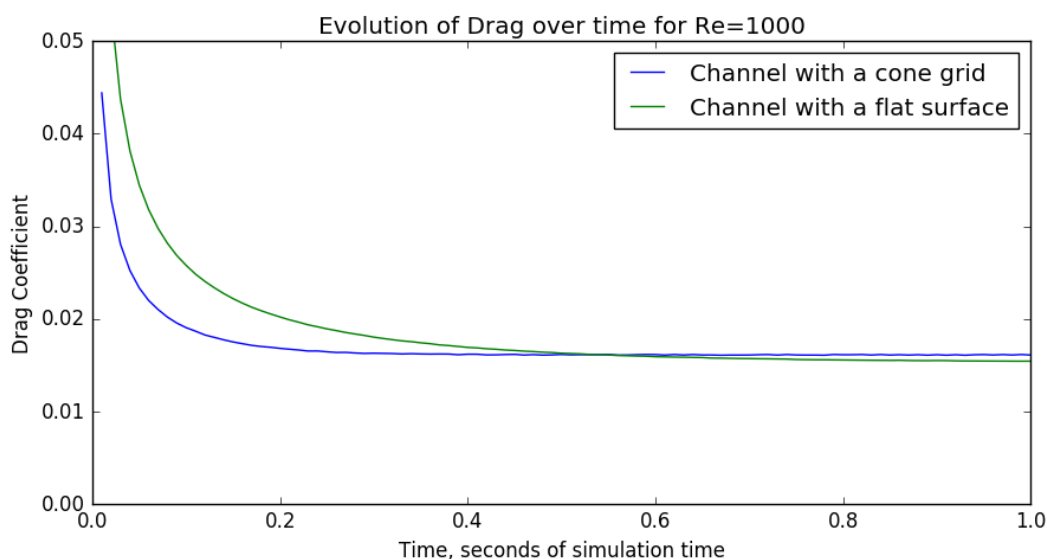


Figure 5: A plot of how the drag coefficient, and thus the force upon the bottom surface of the channel, develops as time progresses

Figure 6 displays the velocity profile for this solution at the steady state, and the empty channel's profile is typical for laminar channel flow. We note that the 85 μm cones effectively limit the velocity around them, and that the typical velocity profile for a laminar channel develop after they have been passed.

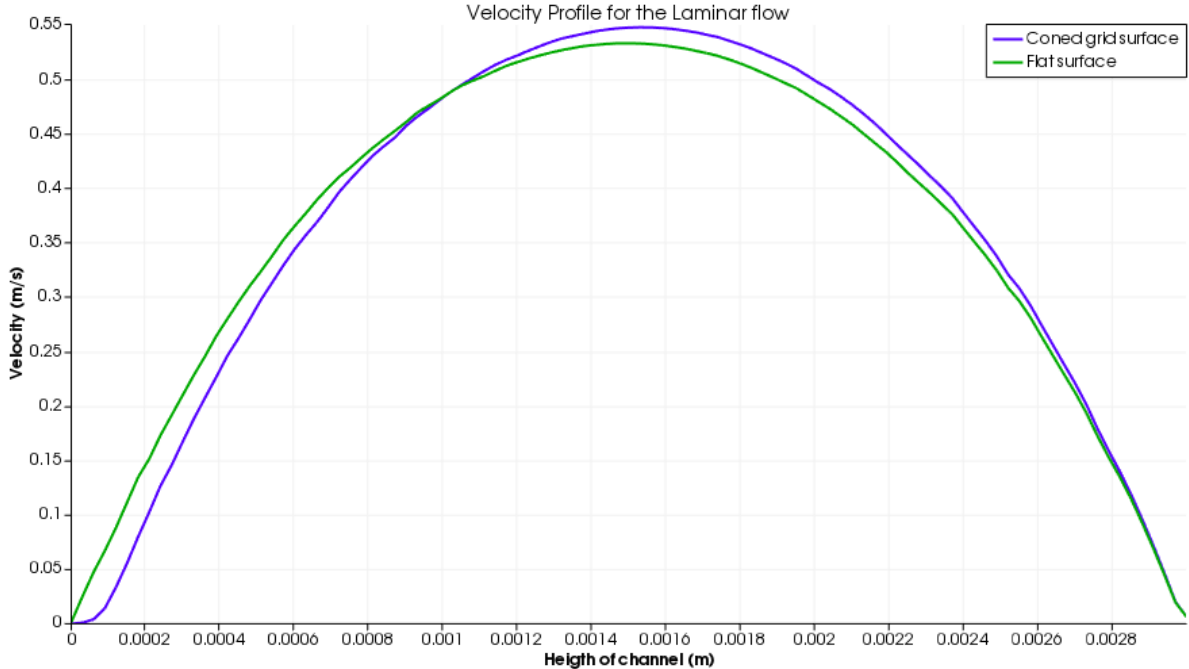


Figure 6: The velocity profile of the fully developed laminar flow, read at time = 1s

Figure 7 visualize the solution of the coned grid, so that we can better understand it when compared to the higher Reynolds number solution.

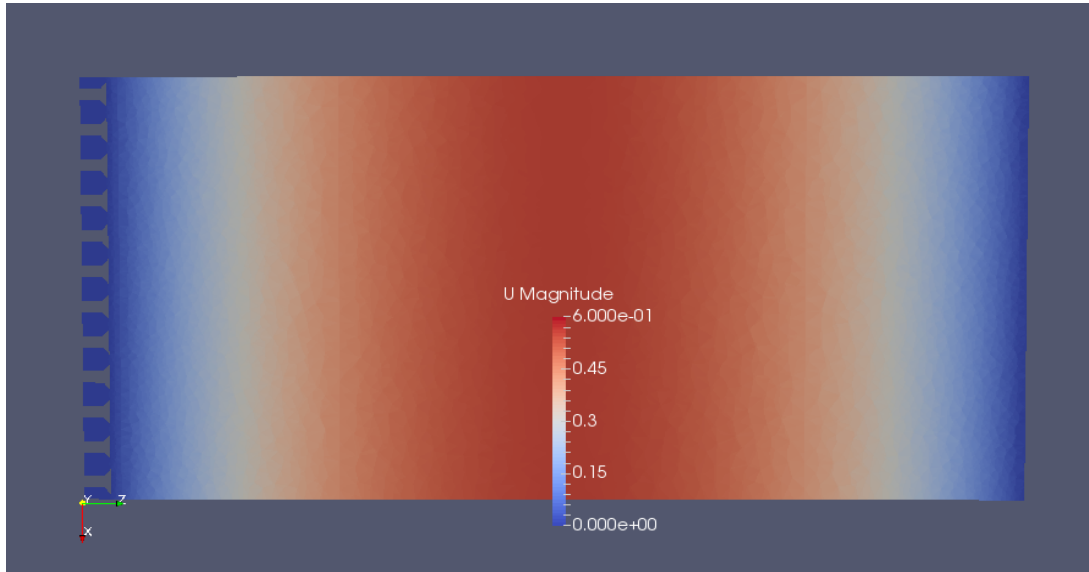


Figure 7: A visualization of laminar flow in a channel with cones. Note that it is turned sideways to save some space.

Turbulent Case

Similar to the previous situation, a mean velocity of 36.7 m/s was used to give a Reynolds number of 10^5 for the turbulent channel flow, but this time using a the Spalart-Allmaras turbulence model. Again two simulations where run: One with the identical 12x6 grid pattern and one with the empty channel. The mesh was kept identical to the previous set of cases. Both where run with a PISO algorithm, and for the coned simulation the time-step difference was $0.1 \mu\text{s}$, starting from a channel with uniform velocity. The time step in the empty channel was increased to $0.5 \mu\text{s}$ to preserve computational resources.

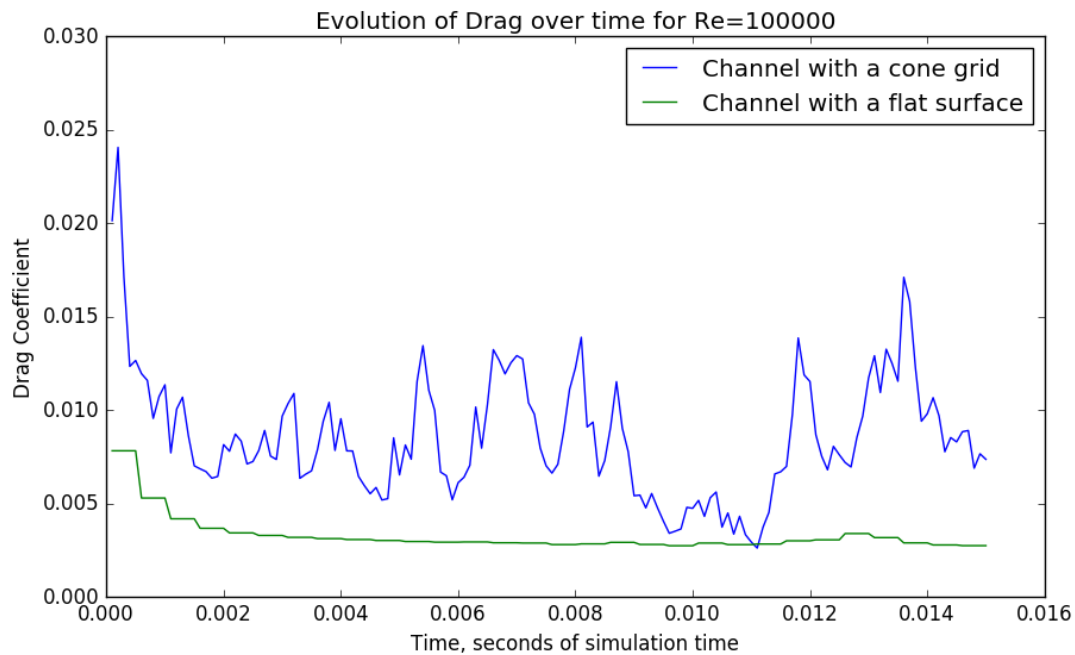


Figure 8: A plot of how the drag coefficient, and thus the force upon the bottom surface of the channel, develops as time progresses. Note the large fluctuations characteristic of turbulent flow.

Figure 8 shows the evolution of the measured drag coefficient as a function of time. This is a turbulent solution, so we do not expect to a steady state but a slightly varying one as vortexes continue to form, move, and dissolve. The simulation is stopped after 0.015 seconds, where the simulation seems to have reached a semi-steady state. We note that while the empty channel has comparatively negligible vortexes, the coned grid is dominated by large fluctuations.

In order to better examine the results we present a temporally averaged velocity profile, Figure 9, from 0.005s to 0.015s. The reason for selecting this particular time is a visual judgment call that the simulation seems to have approached as close to a “solved” state as we can expect by 0.005s. Note that in a perfect simulation we should expect the averaged flat channel velocity profile to be perfectly symmetrical. I have calculated that the averaged Drag coefficients for the two solutions are 0.0083 for the cone grid and 0.0029 for the empty channel.

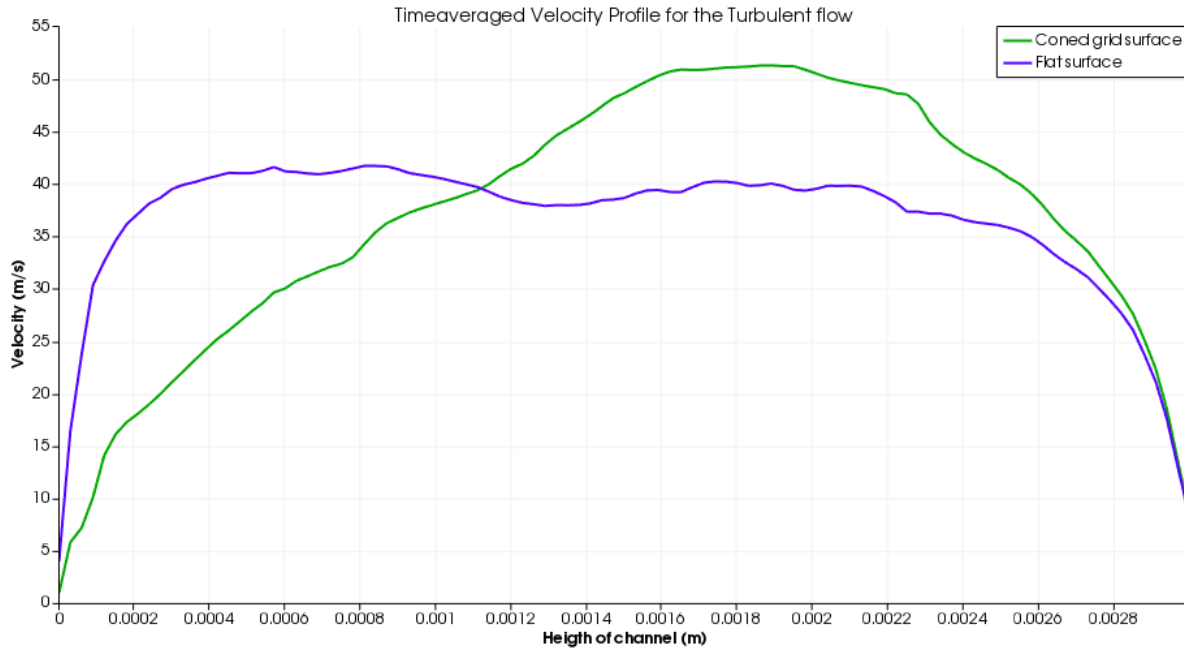


Figure 9: The time averaged velocity profile of the fully developed turbulent flow. The period from $t=0.005s$ to $t=0.015s$ is used for sampling time.

Lastly, we can examine the vortices visually, in Figure 10. Here we see a snapshot of the turbulent cone grid solution, with the scale chosen specifically to highlight typical large vortices. The largest vortex in the figure is $\sim 400 \mu\text{m}$ high, and while this fluctuates I wish to note that I consider it typical, this gives us a characteristic value for the integral length scale, the scale of the largest vortices in the system. We will revisit this topic in the next chapter. Further more we can rescale Figure 10 into Figure 11 to get a better idea about how vortices look between the cones. To further examine this, Figure 12 is identical to Figure 11 but simply moved $60 \mu\text{m}$ (“half a cone”) in the y direction to see the free flow between the cones. We see here that the smallest visual vortices are the ones only a few cells wide. This is to be expected, as any vortices smaller than the cells would be impossible to detect. It would also look like the cones appear to effectively give us two separate systems of vortices, but we need to be careful about how much we read into this as the scaling has been selected specifically to highlight the minor vortices to the detriment of the largest. As we shall soon see, this may not be the case.

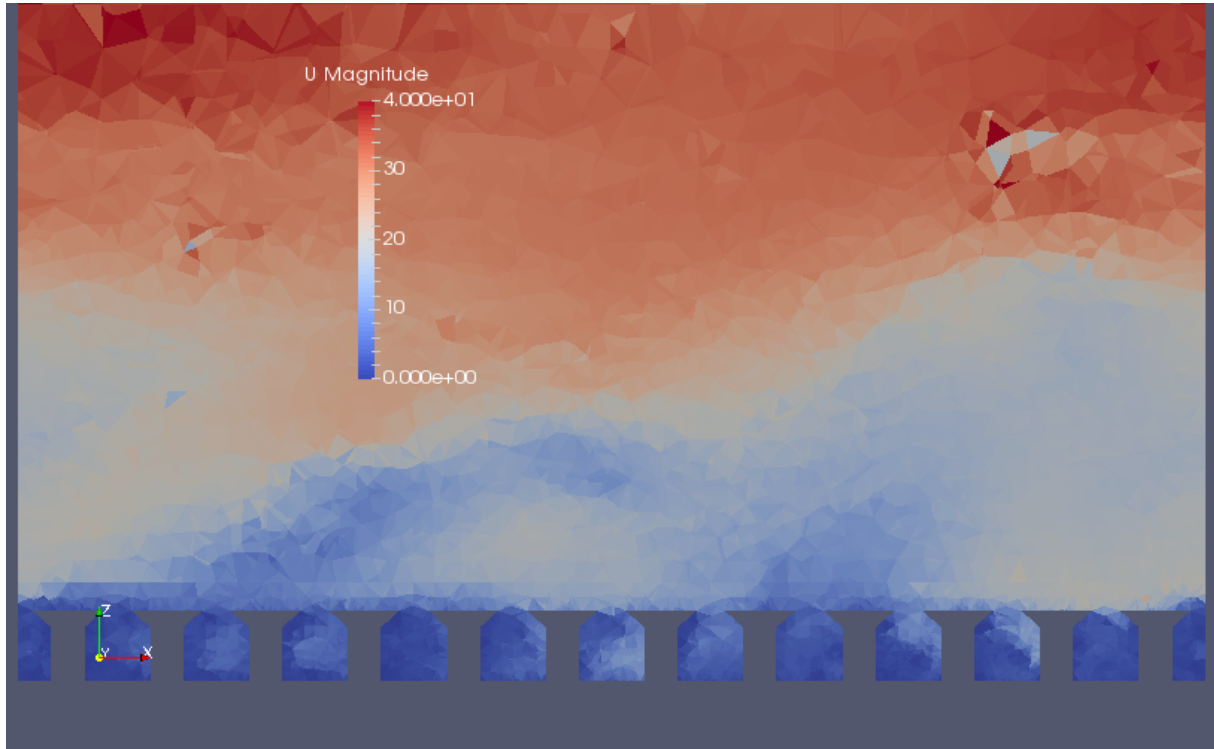


Figure 10: A visualization of the vortices in the turbulent cone grid. Note that the scale and time ($t=0.012$) has been chosen in order to amplify the visual effect. The upper part of the figure has been cut at $z=820\mu\text{m}$, and the cones are $85\mu\text{m}$ tall. The largest vortex is $\sim 400\mu\text{m}$ high.

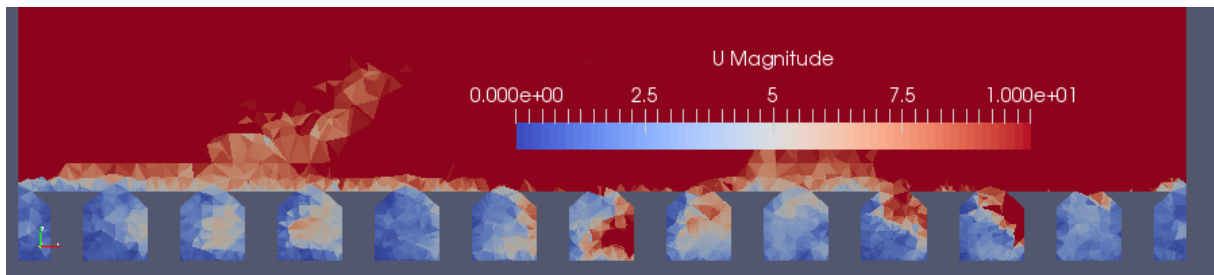


Figure 11: A rescale of the previous figure to amplify the visual effect of the minor vortices between the cones. ($t=0.012\text{s}$)

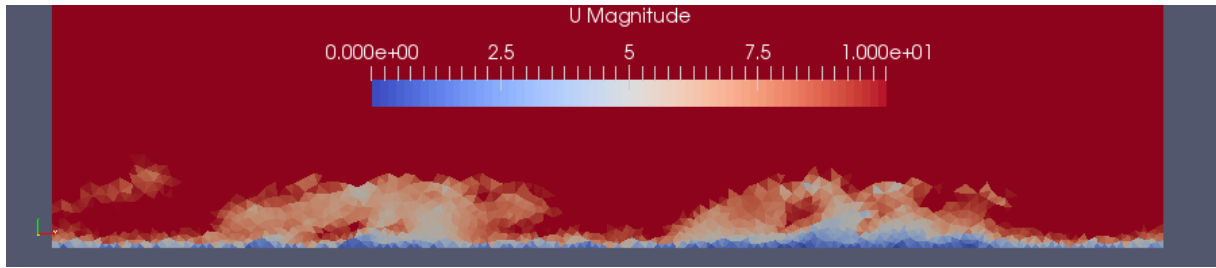


Figure 12: A $60\mu\text{m}$ displacement in y direction of the previous figure to display the more unhindered vortices moving between the cones. ($t=0.012\text{s}$)

In addition to these figures we can also examine the grid from above, and Figure 13 presents a slice at $z=50\mu\text{m}$. Comparing this to a slice at $z=100\mu\text{m}$ presented in Figure 14, we can see that the large scale vortices above the grid appear as a matter of fact to have great influence upon the system of smaller vortices below.

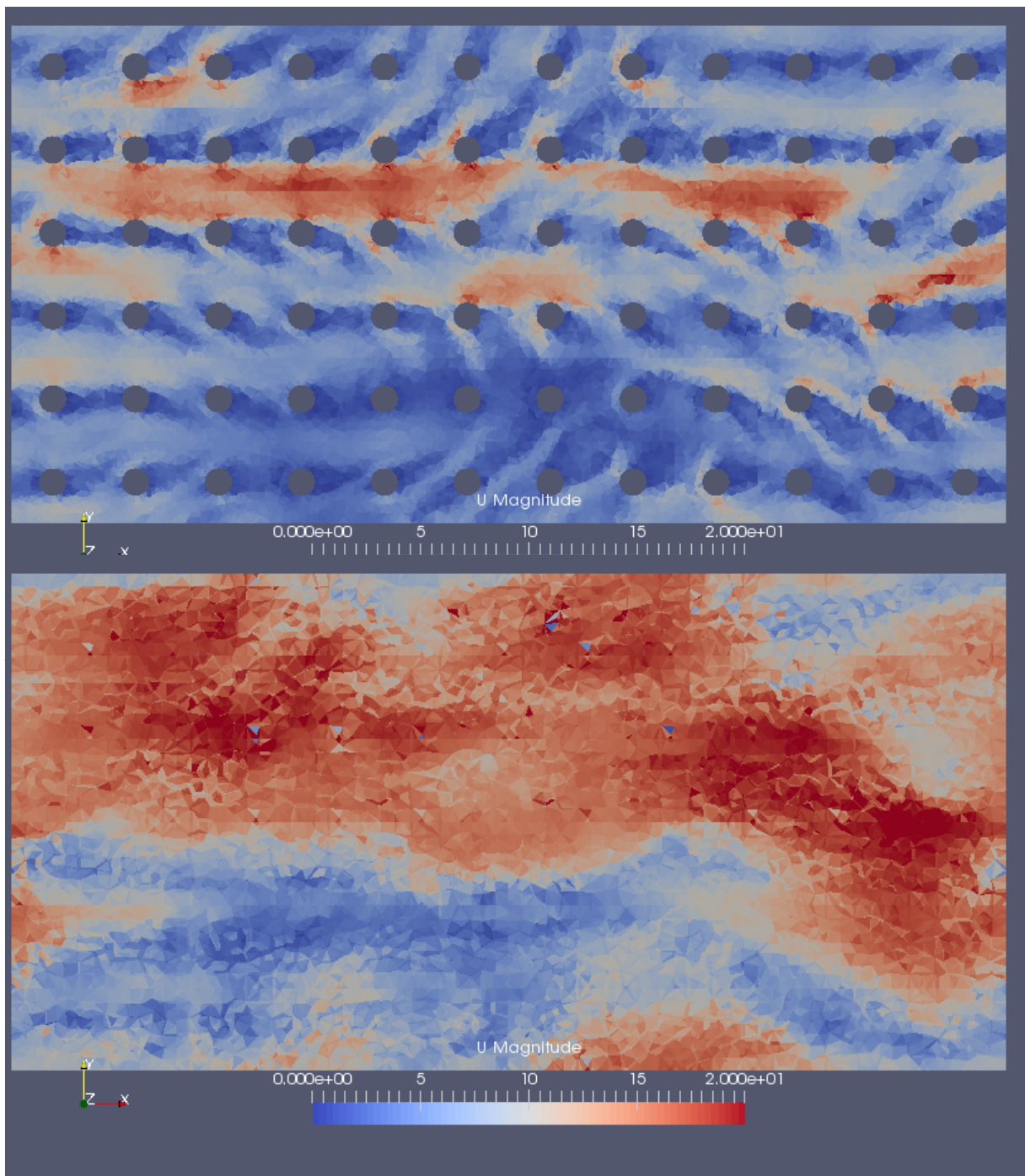


Figure 14: A slice at $z=100\mu\text{m}$, showing the large scale vortices above the grid. ($t=0.012\text{s}$)

Lastly, I want to display the averaged results in the same manner, to have a good basis for comparison. Figure 16 visualize the velocity over the cones, and Figure 15 show us the average velocity field between them. There is a noteworthy numerical artifact in the upper right corner of Figure 16 that can be compared to Figure 10, and I urge you to keep this in mind when we discuss numerical artefacts in next chapter.

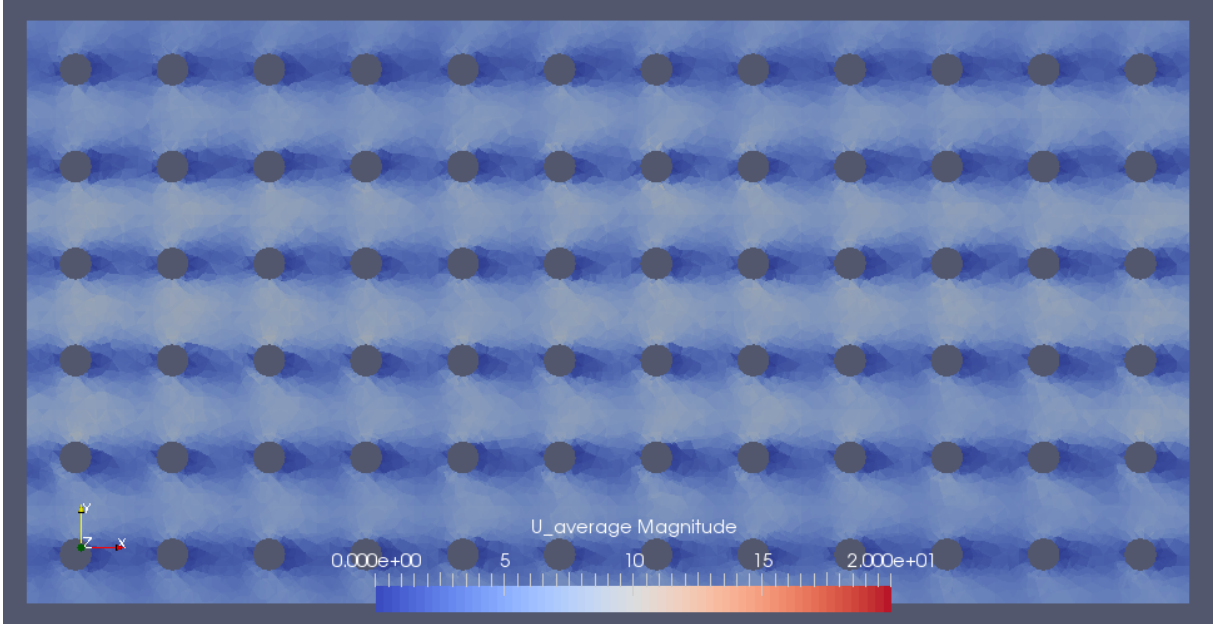


Figure 15: A slice of the temporally averaged velocity at $z=50 \mu\text{m}$.

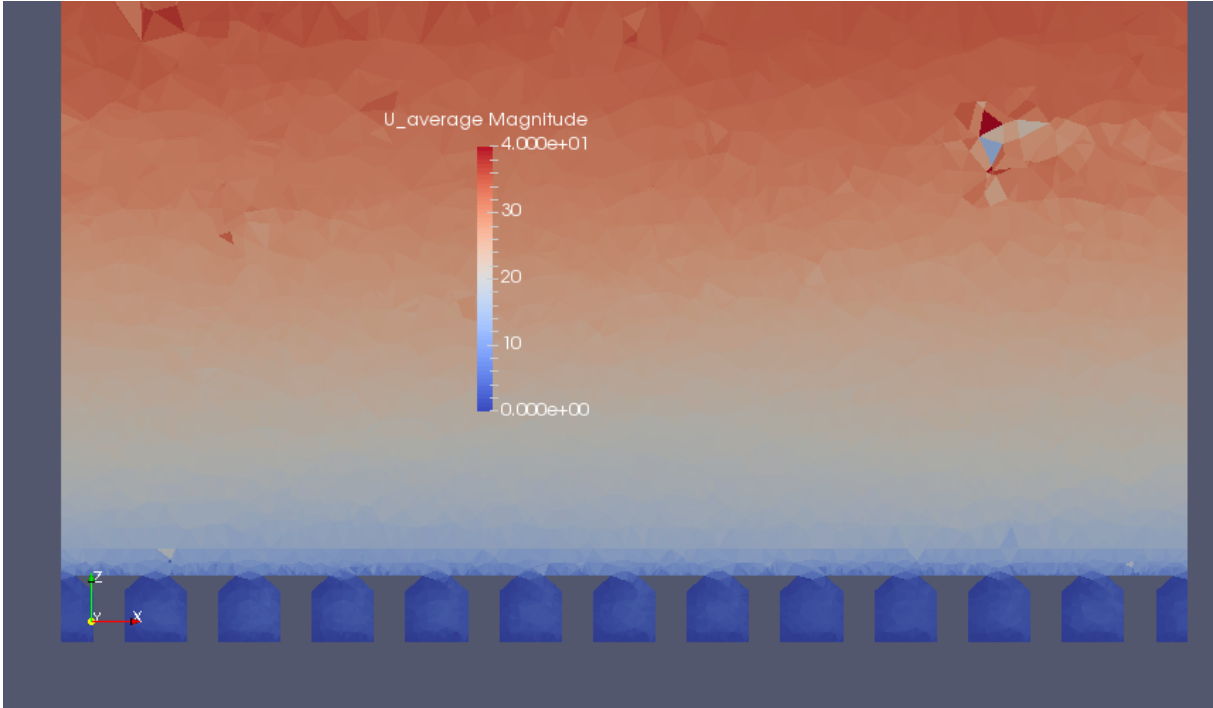


Figure 16: A temporal average of a vertical slice of the velocity over the cones, showing a height up to $z=820 \mu\text{m}$.

Discussion

“Thanks to the development in computer technology it's now possible to get wrong results in CFD quicker and cheaper than ever before” -Unknown

After having looked at the results in the last section, we will now consider possible error sources, discuss them, and if possible verify the results with regards to them. The ability to solve Computational Fluid Dynamic problems is worth little without the ability to also critically analyze the results.

I've done my very best to minimize all of the effects I describe here, and even if they were to change the exact answer by some degree, I do not believe they could possibly accumulate, even together, in large enough quanta to change the final conclusion of this report.

Which is why I remind myself that science cares little for the belief of humans.

Inherent errors from numerical solutions

I assume the reader is knowledgeable about the basic concepts involved in numerical solutions of equations, and these apply here. Openfoam uses the finite volume method to approximate the solution to the governing equations, and even without introducing a turbulence model this would give us errors in the form of computational round-off errors and errors from the numerical schemes used to approximate the differential terms. This is especially important when we have a development from a specific initial condition and want to examine what the end result looks like, as the errors can accumulate over time. In our situation, however, we have a correcting source term in the momentum equation that will continually correct the main flow velocity as it approaches a steady state. This correcting term allow us to neglect any accumulation of computational errors as we steadily approach a steady-state solution.

Possible errors from basic problem constraints

As we introduce obstacles into a empty channel we do of coarse constrict the flow, increasing the flow in the center by a unknown amount. In a perfect world we would use a channel of infinite height, reducing errors from this problem towards zero. However, since that is unrealistic I was advised by my supervisor Tutkun to keep the possible restriction of the inlet below 3%. His long experience with simulation suggest that this would keep the error

introduced from the obstacle at a negligible level. A secondary issue is the size of the cone grid, as this possibly restricts the size of the vortices that can form. I have had to restrain myself to a 6 x 12 grid, and this is far below the recommendations I have received. A common practice is to have a channel length ~ 10 times the height of the channel, and a width equal to half the length. While the requirement of having a width of half the length is easily achievable, the length would require me to use a 250 cone long grid. I estimate this would take me around 22 years of computation time if I solved for the same amount of time steps. Since I am using a cyclic boundary condition on the inlet, outlet, and both sides I hope this does not become a problem, but it is an issue I would have wanted to avoid if I could.

The existence of turbulence in the high Reynolds number case

A possible problem with the LES approach on an unperturbed surface is that under some initial conditions vortices might not form at all, giving us a solution comparable to the laminar result. For our high velocity case with the flat channel this can be a possible issue. We noted the relative low amount of fluctuations in the drag coefficients development over time in Figure 8, and while the velocity profile in Figure 9 points to a turbulent flow we should still verify this further. Figure 17 displays an overhead rendition of the empty channel solution where the scale is chosen to highlight that vortices are, indeed, present.

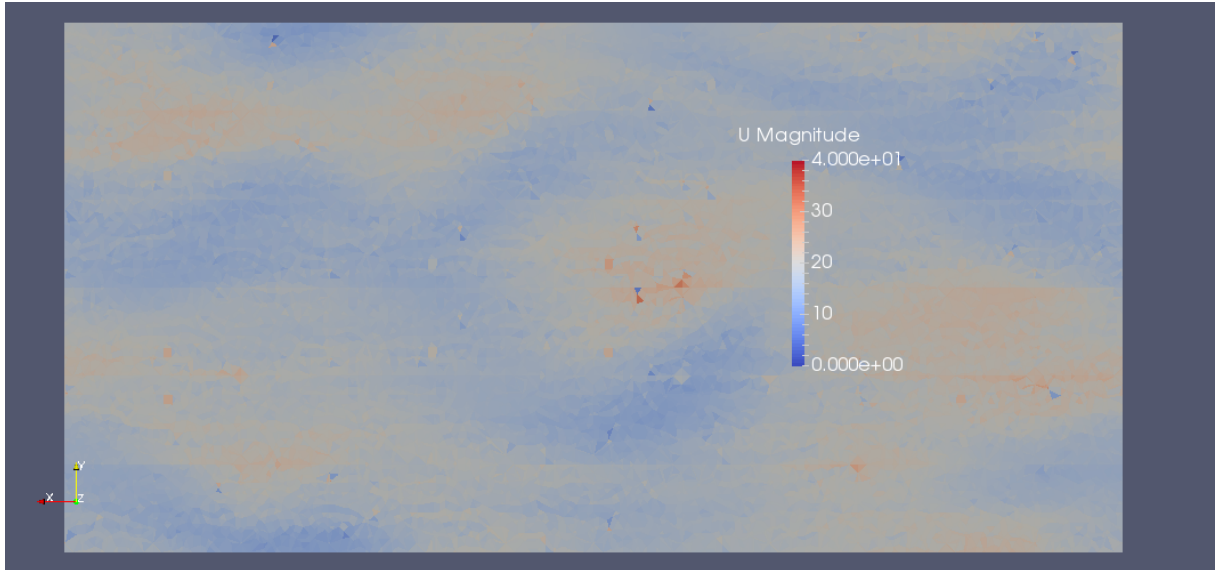


Figure 17: A overhead rendition of the turbulent flat plate solution. This is taken $50 \mu\text{m}$ above the flat plate, and clearly visualizes the existence of vortexes in this region.

Mesh size, and possible impact

A common error source is inadequate refinement of the mesh, or suboptimal distribution of the cells. In a Large Eddy Simulation like this any vortexes smaller than the cell size in any point of the simulation will be modeled instead of simulated. Since the smallest cells in the simulation is placed at the top of the cone and are approximately $5 \mu\text{m}$ tall, any vortex smaller than this is modeled. Using the theory of the Kolmogorov Microscales, we can approximate the smallest vortexes as having a characteristic length of $\eta \sim 0.3 \mu\text{m}$, in accordance with Equation 4 from textbook [6]. η is the length microscale, ν is viscosity for the fluid, U is the integral velocity and L is the integral length scale. Of coarse refinement of all cells down to this level would increase the accuracy of the simulation, but unfortunately this would increase the computational cost, which is already at the “half-to-one-month-of-dedicated-computer-time” scale and thus can not reasonably be increased for this thesis. My conclusions is thus based on the assumption that this grid is sufficiently fine to approximate the drag on the cones, and that any minor vortexes are negligible for the final result.

$$4) \quad \eta = \left(\frac{\nu^3 \cdot L}{U^3} \right)^{(1/4)} = \left(\frac{0.0000011^3 \cdot 0.0004}{36.7^3} \right)^{(1/4)} = 3.2 \times 10^{-7}$$

Another way to confirm that the mesh is sufficient is is to simply refine the mesh by halving the length in each dimension and rerunning the simulation. If the new simulation then gives the same drag coefficient, the solution can be considered mesh independent for this value.

Unfortunately this would require use of ~8 months of computing time during the end of a 4 month thesis, which is unrealistic with our current understanding of spacetime.

Wallfunction for v_t , Spalding

While the instantaneous velocity, pressure, and the transported variable \tilde{v} are all without wall functions, one is used for the turbulent viscosity v_t at the boundary layer of the cones. As such, I need to evaluate the dimensionless parameter y^+ , defined by the distance (y), shear velocity (U_t) and viscosity (ν) of the fluid in Equation 5. Openfoam gives us a tool for calculating the height of the cell closest to a boundary in y^+ , and while this value is preferred as small as possible, it is generally advised to be below 1 by the CFD community for this kind of simulation. As I validated this value in the end phase of the project, I found that the average value on the cones at the end time ($t=0.015s$) was 2.4. The maximum recorded value was 8.8; and the minimum 0.081. For the flat plate the average value is 3.7; the maximum value is 6.8; and the minimum 0.86. I record this as a possible error source, but without further experiments I can not fully know if it is negligible or not.

$$5) \quad y^+ = y \frac{U_t}{\nu}$$

Turbulence semi-steady-state assumption

In the high velocity case I make the argument, based off the development of the drag coefficient, that the simulation is as close to a resolved state as I could expect. While I think this reasoning is sound, the only way to verify this is to apply orders of magnitude more computational time. If it turns out that the large fluctuations I observed eventually dissipates and the system reaches a state with less total drag, then my conclusion may need to be reevaluated. However, considering that the total drag needs to be cut with at least 65% in order to change my conclusion, I find this unrealistic.

Numerical Artifacts

A unfortunate side effect of using this turbulence model that I could not seem to remove to my satisfaction was a series of strange numerical artifacts in the middle of the channel, as shown in Figure 18. While these do not seem to affect any non-negligible vortices, they do seem to throw off the middle section slightly. Considering that these give off a noticeable impression in a large overview look on the channel but does not appear at all close to the area I'm actually

looking into (the bottom layer), I consider these more an embarrassment than a real problem. A majority of these appear to form at the outer boundary of the mesh, which is part of the reason why I kept discarding the outmost layer of cones from the final calculation of the drag coefficient. Of course, it is also possible that the extended area that I'm discarding this way would help diminish the fluctuations as the drag would be calculated over a larger area. If I were to redo the simulation I would probably ignore the possibility of removing these artifacts in favor of a less stochastic final product.

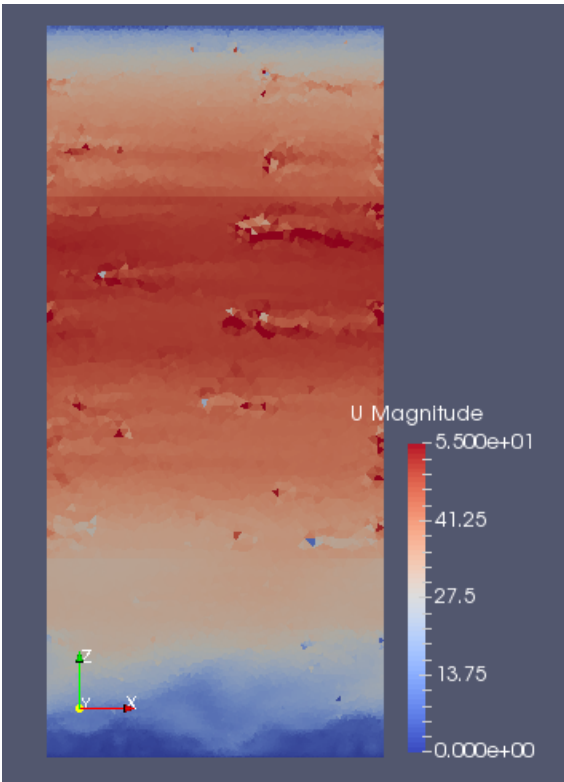


Figure 18: A overview of the solution at $t=0.015s$, scaled to visualize a series of numerical artifacts on the outer boundary of the mesh.

Conclusion

Our original hypothesis was that a grid of cones could be introduced to a flat plate and that we would see the total drag force over the area decrease. Unfortunately, the evidence we have produced showed that adding a cone grid gave an increase in the average drag coefficient by 286%, up from 0.0029 for the empty channel to 0.0083 for the grid. This is, indeed, somewhat problematic for this hypothesis. It should be noted that there may be a lot to gain from increasing the domain size, mesh density and simulation time, but this is usually the case for all CFD projects.

Our hypothesis was based on the work done by Tutkun and his colleges [1], where they had found positive results. I do therefore want to address this seeming inconsistency between my work and theirs, and point out that the conclusions are NOT mutually exclusive.

What I have explored is only the effects on a perfectly flat plate, and while I found that the effects were not beneficial, Tutkun [1] looked at the effect of introducing it at an airfoil, and how this would affect the boundary layer separation of the flow. I wish to compare this with the more famous concept of *Drag Crisis* [7], the phenomena where introducing a roughness unto a sphere or cylinder, while increasing the local turbulence, decrease the total loss of energy as the increased turbulence decrease the flow separation and thereby the total wake. If it was this effect that was observed, and not a effect of the cone grid being better suited than a flat plate for a plane surface, then both results are not only consistent but supportive of each other.

I also want to note this flow separation effect only becomes relevant at very specific Reynolds numbers, for a sphere usually around 10^5 . It is always possible there are beneficial effects that we did not find because we did not investigate the right flow velocity.

I believe this research has great potential, especially on the subject of wings and other objects whose wake has a flow separation issue. We may yet learn to re-evaluate what range of grid systems can be used in such a way and what effects they may have.

From a mechanical engineering point of view, I also want to consider a different issue: Suppose we DID cover a car with a cone grid like this, and suppose it DID reduce drag significantly enough to make this worthwhile, we also need to use a grid that is durable as the car experience common use. A cone only 40 μm wide might be quite fragile, therefore

prompting the need to develop more durable grid systems.

On a personal level I must admit that I did not expect these results. It was my hope when I started this study that I would be able to prove a great potential on flat plates for this biologically inspired grid, which I suppose remind us why it is always important to approach a hypothesis with an open mind, and to quantify the results in such a way that our own preconceptions are rendered mute.

I find it fitting to end the thesis with this quote:

Science is the great antidote to the poison of enthusiasm and superstition. -Adam Smith

List of references

- [1]: S. Dharmarathne, H. B. Evans, A. M. Hamed, B. Aksak, L. P. Chamorro, M. Tutkun, and L. Castillo (2017): "Large-scale Motions on a Wind Turbine Airfoil Section". Submitted to *Journal of Renewable Energy*, currently under review for publication.
- [2]: Eugene de Villiers (2006): "The Potential of Large Eddy Simulation for the Modeling of Wall Bounded Flows". *Thesis*. Imperial College of London, London, England.
- [3]: ESI-OpenCFD (retrieved 21.12.2017): "Numerical Schemes". Retrieved from <https://www.openfoam.com/documentation/user-guide/fvSchemes.php> .
- [4]: Hrvoje Jasak (1996): "Error Analysis and Estimation for the Finite Volume Method with Applications to Fluid Flows". *Thesis*. University of London, London, England.
- [5]: D. B. Spalding (1961): "A Single Formula for the "Law of the Wall"". *Journal of Applied Mechanics*.
- [6]: Frank M. White (2006): "Viscous Fluid Flow" (3rd edition), page 400, Singapore, McGraw-Hill Education.
- [7]: National Aeronautics and Space Administration (retrieved 21.12.2017): "Drag of a Sphere". Retrieved from <https://www.grc.nasa.gov/www/K-12/airplane/dragSphere.html> .

Attachments

Script for generating the 6x12 cone grid mesh

As follows I present the script I created for generating a grid mesh. The script can be used as it is, but note that while most variables in the “control room” segment can be changed at will, changing the number of cones in the grid will require you to manually update surface loops that must take these new cones into consideration. These are marked in the script.

```
//This script is designed to be used with the program GMSH as a .geo file
//The output will be a mesh of a channel with a grid of cones at the bottom.
//It generates a cuboid surrounding each cone, and then adds 3 cuboids on top where cells for the main channel is held.
//The idea is to differentiate cell density depending on the expected boundary thickness.
//Note that if the number of cones are changed, two sections will need to be manually updated, as the surfacefaces of the cones change.

//Anders Utnes, 2017

//*****
//*****CONTROL ROOM*****

//Unit of distance is one micrometer
um=0.000001;

//Grid size at different points in mesh
ot= 20*um; //Outer top edge of box surrounding each cone
ol= 10*um; //Outer low edge of box surrounding each cone
il= 10*um; //inner low edge of cone
im= 10*um; //inner middle of each cone, the point of the angle
it= 5*um; //inner top of each cone
bl= 40*um; //The middle part of the boundary layer.

//Dimensions
th= 3000*um; //Channel total height
os= 120*um; //Outer length of the box surrounding cones
oh= 120*um; //Outer height of the box surrounding cones
imh= 65*um; //Height of the cone at the point it starts expanding
ith= 85*um; //Height of the cone at its top
ilr= 20*um; //Radius of the cone at the bottom
imr= 20*um; //Radius of the cone at the point it starts expanding
itr= 42.5*um; //Radius of the cone at the top
```

```

blt=          700*um; //Expected boundary layer thickness

//Number of cones in x direction
x=12;

//Number of cones in y direction
y=6;

//*****REMEMBER TO MANUALLY UPDATE THE SURFACELOOPS*****
//*****

//Cone and cuboid generation:

//Note that all information relevant to a cone is numbered as such:
//XXYYZZ, where XX refers to the x rank of the cone, YY to the y rank, and ZZ to the point/line/surface variable.

//Initializing wall at x=0:
a=0;
b=0;
Point(10000*a+100*b+0)=      {a*os, b*os, 0*oh, ol};
Point(10000*a+100*b+1)=      {a*os, b*os, 1*oh, ol};
Line(10000*a+100*b+1)=        {10000*a+100*b+0, 10000*a+100*b+1}; //Pillar

For b In {1:y:1}
  Point(10000*a+100*b+0)=      {a*os, b*os, 0*oh, ol};
  Point(10000*a+100*b+1)=      {a*os, b*os, 1*oh, ol};
  Line(10000*a+100*b+1)=        {10000*a+100*b+0, 10000*a+100*b+1}; //Pillar
  Line(10000*a+100*b+2)=        {10000*a+100*(b-1)+0, 10000*a+100*b+0}; //bot y
  Line(10000*a+100*b+3)=        {10000*a+100*(b-1)+1, 10000*a+100*b+1}; //top y
  Line Loop(10000*a+100*b+1)=    {10000*a+100*(b-1)+1, 10000*a+100*b+3, -(10000*a+100*b+1), -
(10000*a+100*b+2)};
  Plane Surface(10000*a+100*b+1)= {10000*a+100*b+1}; //Side with
normal in x direction
EndFor

//Making cones:
For a In {1:x:1}
  //Starting on a new wall at y=0
  b=0;
  Point(10000*a+100*b+0)=      {a*os, b*os, 0*oh, ol};
  Point(10000*a+100*b+1)=      {a*os, b*os, 1*oh, ol};
  Line(10000*a+100*b+1)=        {10000*a+100*b+0, 10000*a+100*b+1}; //Pillar
  Line(10000*a+100*b+4)=        {10000*(a-1)+100*b+0, 10000*a+100*b+0}; //bot x

```

```

Line(10000*a+100*b+5)=          {10000*(a-1)+100*b+1, 10000*a+100*b+1};    //top x
Line Loop(10000*a+100*b+2)=     {10000*(a-1)+100*b+1, 10000*a+100*b+5, -(10000*a+100*b+1), -(10000*a+100*b+4)};
Plane Surface(10000*a+100*b+2)= {10000*a+100*b+2};          //Side with normal in y
direction

```

For b In {1:y:1}

//Defining a cone:

```

Point(10000*a+100*b+10)=        {(a-0.5)*os-iltr, (b-0.5)*os, 0, il};
Point(10000*a+100*b+11)=        {(a-0.5)*os, (b-0.5)*os+iltr, 0, il};
Point(10000*a+100*b+12)=        {(a-0.5)*os+iltr, (b-0.5)*os, 0, il};
Point(10000*a+100*b+13)=        {(a-0.5)*os, (b-0.5)*os-iltr, 0, il};
Point(10000*a+100*b+14)=        {(a-0.5)*os, (b-0.5)*os, 0, il};
Circle(10000*a+100*b+10)=        {10000*a+100*b+10, 10000*a+100*b+14, 10000*a+100*b+11};
Circle(10000*a+100*b+11)=        {10000*a+100*b+11, 10000*a+100*b+14, 10000*a+100*b+12};
Circle(10000*a+100*b+12)=        {10000*a+100*b+12, 10000*a+100*b+14, 10000*a+100*b+13};
Circle(10000*a+100*b+13)=        {10000*a+100*b+13, 10000*a+100*b+14, 10000*a+100*b+10};
Line Loop(10000*a+100*b+5)=      {10000*a+100*b+10, 10000*a+100*b+11, 10000*a+100*b+12, 10000*a+100*b+13};
Point(10000*a+100*b+20)=        {(a-0.5)*os-imr, (b-0.5)*os, imh, il};
Point(10000*a+100*b+21)=        {(a-0.5)*os, (b-0.5)*os+imr, imh, il};
Point(10000*a+100*b+22)=        {(a-0.5)*os+imr, (b-0.5)*os, imh, il};
Point(10000*a+100*b+23)=        {(a-0.5)*os, (b-0.5)*os-imr, imh, il};
Point(10000*a+100*b+24)=        {(a-0.5)*os, (b-0.5)*os, imh, il};
Line(10000*a+100*b+20)=          {10000*a+100*b+10, 10000*a+100*b+20};
Line(10000*a+100*b+21)=          {10000*a+100*b+11, 10000*a+100*b+21};
Line(10000*a+100*b+22)=          {10000*a+100*b+12, 10000*a+100*b+22};
Line(10000*a+100*b+23)=          {10000*a+100*b+13, 10000*a+100*b+23};
Circle(10000*a+100*b+30)=        {10000*a+100*b+20, 10000*a+100*b+24, 10000*a+100*b+21};
Circle(10000*a+100*b+31)=        {10000*a+100*b+21, 10000*a+100*b+24, 10000*a+100*b+22};
Circle(10000*a+100*b+32)=        {10000*a+100*b+22, 10000*a+100*b+24, 10000*a+100*b+23};
Circle(10000*a+100*b+33)=        {10000*a+100*b+23, 10000*a+100*b+24, 10000*a+100*b+20};
Line Loop(10000*a+100*b+10)=     {10000*a+100*b+10, 10000*a+100*b+21, -(10000*a+100*b+30), -
(10000*a+100*b+20)};
Line Loop(10000*a+100*b+11)=     {10000*a+100*b+11, 10000*a+100*b+22, -(10000*a+100*b+31), -
(10000*a+100*b+21)};
Line Loop(10000*a+100*b+12)=     {10000*a+100*b+12, 10000*a+100*b+23, -(10000*a+100*b+32), -
(10000*a+100*b+22)};
Line Loop(10000*a+100*b+13)=     {10000*a+100*b+13, 10000*a+100*b+20, -(10000*a+100*b+33), -
(10000*a+100*b+23)};
Point(10000*a+100*b+30)=        {(a-0.5)*os-itr, (b-0.5)*os, ith, il};
Point(10000*a+100*b+31)=        {(a-0.5)*os, (b-0.5)*os+itr, ith, il};
Point(10000*a+100*b+32)=        {(a-0.5)*os+itr, (b-0.5)*os, ith, il};
Point(10000*a+100*b+33)=        {(a-0.5)*os, (b-0.5)*os-itr, ith, il};
Point(10000*a+100*b+34)=        {(a-0.5)*os, (b-0.5)*os, ith, il};
Line(10000*a+100*b+40)=          {10000*a+100*b+20, 10000*a+100*b+30};
Line(10000*a+100*b+41)=          {10000*a+100*b+21, 10000*a+100*b+31};
Line(10000*a+100*b+42)=          {10000*a+100*b+22, 10000*a+100*b+32};
Line(10000*a+100*b+43)=          {10000*a+100*b+23, 10000*a+100*b+33};

```

```

Circle(10000*a+100*b+50)=          {10000*a+100*b+30, 10000*a+100*b+34, 10000*a+100*b+31};
Circle(10000*a+100*b+51)=          {10000*a+100*b+31, 10000*a+100*b+34, 10000*a+100*b+32};
Circle(10000*a+100*b+52)=          {10000*a+100*b+32, 10000*a+100*b+34, 10000*a+100*b+33};
Circle(10000*a+100*b+53)=          {10000*a+100*b+33, 10000*a+100*b+34, 10000*a+100*b+30};
Line Loop(10000*a+100*b+20)= {10000*a+100*b+30, 10000*a+100*b+41, -(10000*a+100*b+50), -
(10000*a+100*b+40)};
Line Loop(10000*a+100*b+21)= {10000*a+100*b+31, 10000*a+100*b+42, -(10000*a+100*b+51), -
(10000*a+100*b+41)};
Line Loop(10000*a+100*b+22)= {10000*a+100*b+32, 10000*a+100*b+43, -(10000*a+100*b+52), -
(10000*a+100*b+42)};
Line Loop(10000*a+100*b+23)= {10000*a+100*b+33, 10000*a+100*b+40, -(10000*a+100*b+53), -
(10000*a+100*b+43)};
Line Loop(10000*a+100*b+30)= {10000*a+100*b+50, 10000*a+100*b+51, 10000*a+100*b+52, 10000*a+100*b+53};
Ruled Surface(10000*a+100*b+10)=      {10000*a+100*b+10};
Ruled Surface(10000*a+100*b+11)=      {10000*a+100*b+11};
Ruled Surface(10000*a+100*b+12)=      {10000*a+100*b+12};
Ruled Surface(10000*a+100*b+13)=      {10000*a+100*b+13};
Ruled Surface(10000*a+100*b+20)=      {10000*a+100*b+20};
Ruled Surface(10000*a+100*b+21)=      {10000*a+100*b+21};
Ruled Surface(10000*a+100*b+22)=      {10000*a+100*b+22};
Ruled Surface(10000*a+100*b+23)=      {10000*a+100*b+23};
Plane Surface(10000*a+100*b+30)=      {10000*a+100*b+30};

//Surrounding the cone with a outer cuboid:
Point(10000*a+100*b+0)=      {a*os, b*os, 0*oh, ol};
Point(10000*a+100*b+1)=      {a*os, b*os, 1*oh, ol};
Line(10000*a+100*b+1)=      {10000*a+100*b+0, 10000*a+100*b+1};          //Pillar
Line(10000*a+100*b+2)=      {10000*a+100*(b-1)+0, 10000*a+100*b+0};          //bot y
Line(10000*a+100*b+3)=      {10000*a+100*(b-1)+1, 10000*a+100*b+1};          //top y
Line(10000*a+100*b+4)=      {10000*(a-1)+100*b+0, 10000*a+100*b+0};          //bot x
Line(10000*a+100*b+5)=      {10000*(a-1)+100*b+1, 10000*a+100*b+1};          //top x
Line Loop(10000*a+100*b+1)=      {10000*a+100*(b-1)+1, 10000*a+100*b+3, -(10000*a+100*b+1), -(10000*a+100*b+2)};
Line Loop(10000*a+100*b+2)=      {10000*(a-1)+100*b+1, 10000*a+100*b+5, -(10000*a+100*b+1), -(10000*a+100*b+4)};
Line Loop(10000*a+100*b+3)=      {10000*(a-1)+100*b+2, 10000*a+100*b+4, -(10000*a+100*b+2), -(10000*a+100*(b-
1)+4)};
Line Loop(10000*a+100*b+4)=      {10000*(a-1)+100*b+3, 10000*a+100*b+5, -(10000*a+100*b+3), -(10000*a+100*(b-
1)+5)};
Plane Surface(10000*a+100*b+1)= {10000*a+100*b+1};          //Side with
normal in x direction
Plane Surface(10000*a+100*b+2)= {10000*a+100*b+2};          //Side with
normal in y direction
Plane Surface(10000*a+100*b+3)= {10000*a+100*b+3, 10000*a+100*b+5};          //Bottom Side with cone intersection
removed
Plane Surface(10000*a+100*b+4)= {10000*a+100*b+4};          //Top
Surface Loop(10000*a+100*b+1)= {10000*a+100*b+1, 10000*a+100*b+2, 10000*a+100*b+3, 10000*a+100*b+4,
10000*(a-1)+100*b+1, 10000*a+100*(b-1)+2, 10000*a+100*b+10, 10000*a+100*b+11, 10000*a+100*b+12,
10000*a+100*b+13, 10000*a+100*b+20, 10000*a+100*b+21, 10000*a+100*b+22, 10000*a+100*b+23, 10000*a+100*b+30};
Volume(10000*a+100*b+1)=      {10000*a+100*b+1};

EndFor
EndFor

```

```

//Making the lower part of the channel over the cones:
Point(1000001)=      {0, 0, oh+blt, bl};
Point(1000002)=      {x*os, 0, oh+blt, bl};
Point(1000003)=      {x*os, y*os, oh+blt, bl};
Point(1000004)=      {0, y*os, oh+blt, bl};

Line(1000001)=       {1, 1000001};
Line(1000002)=       {10000*x+1, 1000002};
Line(1000003)=       {10000*x+100*y+1, 1000003};
Line(1000004)=       {100*y+1, 1000004};

Line(1000011)=       {1000001, 1000002};
Line(1000012)=       {1000002, 1000003};
Line(1000013)=       {1000003, 1000004};
Line(1000014)=       {1000004, 1000001};

Line Loop(1000005)=   {1000011, 1000012, 1000013, 1000014};

//*****FIRST SECTION THAT NEEDS MANUAL UPDATE*****
Line Loop(1000001)=   { //Top x lines goes here.
10005 ,
20005 ,
30005 ,
40005 ,
50005 ,
60005 ,
70005 ,
80005 ,
90005 ,
100005 ,
110005 ,
120005 ,
1000002, -1000011, -1000001};

Line Loop(1000002)=   { //Top y lines goes here.
120103 ,
120203 ,
120303 ,
120403 ,
120503 ,
120603 ,
1000003, -1000012, -1000002};

```

```
Line Loop(1000003)=      {      //Top x lines goes here.
10605 ,
20605 ,
30605 ,
40605 ,
50605 ,
60605 ,
70605 ,
80605 ,
90605 ,
100605 ,
110605 ,
120605 ,
1000003, 1000013, -1000004};
```

```
Line Loop(1000004)= {      //Top y lines goes here.
1000004, 1000014, -1000001,
103 ,
203 ,
303 ,
403 ,
503 ,
603 };
```

```
Plane Surface(1000001)= {1000001};
Plane Surface(1000002)= {1000002};
Plane Surface(1000003)= {1000003};
Plane Surface(1000004)= {1000004};
Plane Surface(1000005)= {1000005};
```

```
Surface Loop(1000001)=   {1000001, 1000002, 1000003, 1000004, 1000005,
10104 ,
10204 ,
10304 ,
10404 ,
10504 ,
10604 ,
20104 ,
20204 ,
20304 ,
20404 ,
20504 ,
20604 ,
30104 ,
```

30204 ,
30304 ,
30404 ,
30504 ,
30604 ,
40104 ,
40204 ,
40304 ,
40404 ,
40504 ,
40604 ,
50104 ,
50204 ,
50304 ,
50404 ,
50504 ,
50604 ,
60104 ,
60204 ,
60304 ,
60404 ,
60504 ,
60604 ,
70104 ,
70204 ,
70304 ,
70404 ,
70504 ,
70604 ,
80104 ,
80204 ,
80304 ,
80404 ,
80504 ,
80604 ,
90104 ,
90204 ,
90304 ,
90404 ,
90504 ,
90604 ,
100104 ,
100204 ,
100304 ,
100404 ,

100504 ,
100604 ,
110104 ,
110204 ,
110304 ,
110404 ,
110504 ,
110604 ,
120104 ,
120204 ,
120304 ,
120404 ,
120504 ,
120604 };

//*****END OF FIRST SECTION THAT NEEDS MANUAL UPDATE*****

Volume(1000001)= {1000001};

//Middle flow

Point(2000001)= {0, 0, th-bl, bl};
Point(2000002)= {x*os, 0, th-bl, bl};
Point(2000003)= {x*os, y*os, th-bl, bl};
Point(2000004)= {0, y*os, th-bl, bl};

Line(2000001)= {1000001, 2000001};
Line(2000002)= {1000002, 2000002};
Line(2000003)= {1000003, 2000003};
Line(2000004)= {1000004, 2000004};

Line(2000011)= {2000001, 2000002};
Line(2000012)= {2000002, 2000003};
Line(2000013)= {2000003, 2000004};
Line(2000014)= {2000004, 2000001};

Line Loop(2000001)= {1000011, 2000002, -2000011, -2000001};
Line Loop(2000002)= {1000012, 2000003, -2000012, -2000002};
Line Loop(2000003)= {-1000013, 2000003, 2000013, -2000004};
Line Loop(2000004)= {2000004, 2000014, -2000001, -1000014};
Line Loop(2000005)= {2000011, 2000012, 2000013, 2000014};


```

Plane Surface(2000001)= {2000001};
Plane Surface(2000002)= {2000002};
Plane Surface(2000003)= {2000003};
Plane Surface(2000004)= {2000004};
Plane Surface(2000005)= {2000005};

Surface Loop(2000001)= {2000001, 2000002, 2000003, 2000004, 2000005, 1000005};
Volume(2000001)= {2000001};

//Upper boundary layer
Point(3000001)= {0, 0, th, ot};
Point(3000002)= {x*os, 0, th, ot};
Point(3000003)= {x*os, y*os, th, ot};
Point(3000004)= {0, y*os, th, ot};

Line(3000001)= {2000001, 3000001};
Line(3000002)= {2000002, 3000002};
Line(3000003)= {2000003, 3000003};
Line(3000004)= {2000004, 3000004};

Line(3000011)= {3000001, 3000002};
Line(3000012)= {3000002, 3000003};
Line(3000013)= {3000003, 3000004};
Line(3000014)= {3000004, 3000001};

Line Loop(3000001)= {2000011, 3000002, -3000011, -3000001};
Line Loop(3000002)= {2000012, 3000003, -3000012, -3000002};
Line Loop(3000003)= {-2000013, 3000003, 3000013, -3000004};
Line Loop(3000004)= {3000004, 3000014, -3000001, -2000014};
Line Loop(3000005)= {3000011, 3000012, 3000013, 3000014};

Plane Surface(3000001)= {3000001};
Plane Surface(3000002)= {3000002};
Plane Surface(3000003)= {3000003};
Plane Surface(3000004)= {3000004};
Plane Surface(3000005)= {3000005};

Surface Loop(3000001)= {3000001, 3000002, 3000003, 3000004, 3000005, 2000005};

Volume(3000001)= {3000001};

```

//*****SECOND SECTION THAT NEEDS MANUAL UPDATE*****

Physical Surface("inlet")={1000004, 2000004, 3000004,
101 ,
201 ,
301 ,
401 ,
501 ,
601 };

Physical Surface("outlet")={1000002, 2000002, 3000002,
120101 ,
120201 ,
120301 ,
120401 ,
120501 ,
120601 };

Physical Surface("right")={1000001, 2000001, 3000001,
10002 ,
20002 ,
30002 ,
40002 ,
50002 ,
60002 ,
70002 ,
80002 ,
90002 ,
100002 ,
110002 ,
120002 };

Physical Surface("left")={1000003, 2000003, 3000003,
10602 ,
20602 ,
30602 ,
40602 ,
50602 ,
60602 ,
70602 ,
80602 ,
90602 ,
100602 ,
110602 ,
120602 };

Physical Surface("top")={3000005};

Physical Surface("ground")={

10103 , 10110 , 10111 , 10112 , 10113 , 10120 , 10121 , 10122 , 10123 , 10130 ,
10203 , 10210 , 10211 , 10212 , 10213 , 10220 , 10221 , 10222 , 10223 , 10230 ,
10303 , 10310 , 10311 , 10312 , 10313 , 10320 , 10321 , 10322 , 10323 , 10330 ,
10403 , 10410 , 10411 , 10412 , 10413 , 10420 , 10421 , 10422 , 10423 , 10430 ,
10503 , 10510 , 10511 , 10512 , 10513 , 10520 , 10521 , 10522 , 10523 , 10530 ,
10603 , 10610 , 10611 , 10612 , 10613 , 10620 , 10621 , 10622 , 10623 , 10630 ,
20103 , 20110 , 20111 , 20112 , 20113 , 20120 , 20121 , 20122 , 20123 , 20130 ,
20603 , 20610 , 20611 , 20612 , 20613 , 20620 , 20621 , 20622 , 20623 , 20630 ,
30103 , 30110 , 30111 , 30112 , 30113 , 30120 , 30121 , 30122 , 30123 , 30130 ,
30603 , 30610 , 30611 , 30612 , 30613 , 30620 , 30621 , 30622 , 30623 , 30630 ,
40103 , 40110 , 40111 , 40112 , 40113 , 40120 , 40121 , 40122 , 40123 , 40130 ,
40603 , 40610 , 40611 , 40612 , 40613 , 40620 , 40621 , 40622 , 40623 , 40630 ,
50103 , 50110 , 50111 , 50112 , 50113 , 50120 , 50121 , 50122 , 50123 , 50130 ,
50603 , 50610 , 50611 , 50612 , 50613 , 50620 , 50621 , 50622 , 50623 , 50630 ,
60103 , 60110 , 60111 , 60112 , 60113 , 60120 , 60121 , 60122 , 60123 , 60130 ,
60603 , 60610 , 60611 , 60612 , 60613 , 60620 , 60621 , 60622 , 60623 , 60630 ,
70103 , 70110 , 70111 , 70112 , 70113 , 70120 , 70121 , 70122 , 70123 , 70130 ,
70603 , 70610 , 70611 , 70612 , 70613 , 70620 , 70621 , 70622 , 70623 , 70630 ,
80103 , 80110 , 80111 , 80112 , 80113 , 80120 , 80121 , 80122 , 80123 , 80130 ,
80603 , 80610 , 80611 , 80612 , 80613 , 80620 , 80621 , 80622 , 80623 , 80630 ,
90103 , 90110 , 90111 , 90112 , 90113 , 90120 , 90121 , 90122 , 90123 , 90130 ,
90603 , 90610 , 90611 , 90612 , 90613 , 90620 , 90621 , 90622 , 90623 , 90630 ,
100103 , 100110 , 100111 , 100112 , 100113 , 100120 , 100121 , 100122 , 100123 , 100130 ,
100603 , 100610 , 100611 , 100612 , 100613 , 100620 , 100621 , 100622 , 100623 , 100630 ,
110103 , 110110 , 110111 , 110112 , 110113 , 110120 , 110121 , 110122 , 110123 , 110130 ,
110603 , 110610 , 110611 , 110612 , 110613 , 110620 , 110621 , 110622 , 110623 , 110630 ,
120103 , 120110 , 120111 , 120112 , 120113 , 120120 , 120121 , 120122 , 120123 , 120130 ,
120203 , 120210 , 120211 , 120212 , 120213 , 120220 , 120221 , 120222 , 120223 , 120230 ,
120303 , 120310 , 120311 , 120312 , 120313 , 120320 , 120321 , 120322 , 120323 , 120330 ,
120403 , 120410 , 120411 , 120412 , 120413 , 120420 , 120421 , 120422 , 120423 , 120430 ,
120503 , 120510 , 120511 , 120512 , 120513 , 120520 , 120521 , 120522 , 120523 , 120530 ,
120603 , 120610 , 120611 , 120612 , 120613 , 120620 , 120621 , 120622 , 120623 , 120630 };

Physical Surface("plate")= {

20203 , 20210 , 20211 , 20212 , 20213 , 20220 , 20221 , 20222 , 20223 , 20230 ,
20303 , 20310 , 20311 , 20312 , 20313 , 20320 , 20321 , 20322 , 20323 , 20330 ,
20403 , 20410 , 20411 , 20412 , 20413 , 20420 , 20421 , 20422 , 20423 , 20430 ,
20503 , 20510 , 20511 , 20512 , 20513 , 20520 , 20521 , 20522 , 20523 , 20530 ,
30203 , 30210 , 30211 , 30212 , 30213 , 30220 , 30221 , 30222 , 30223 , 30230 ,
30303 , 30310 , 30311 , 30312 , 30313 , 30320 , 30321 , 30322 , 30323 , 30330 ,
30403 , 30410 , 30411 , 30412 , 30413 , 30420 , 30421 , 30422 , 30423 , 30430 ,

30503 , 30510 , 30511 , 30512 , 30513 , 30520 , 30521 , 30522 , 30523 , 30530 ,
40203 , 40210 , 40211 , 40212 , 40213 , 40220 , 40221 , 40222 , 40223 , 40230 ,
40303 , 40310 , 40311 , 40312 , 40313 , 40320 , 40321 , 40322 , 40323 , 40330 ,
40403 , 40410 , 40411 , 40412 , 40413 , 40420 , 40421 , 40422 , 40423 , 40430 ,
40503 , 40510 , 40511 , 40512 , 40513 , 40520 , 40521 , 40522 , 40523 , 40530 ,
50203 , 50210 , 50211 , 50212 , 50213 , 50220 , 50221 , 50222 , 50223 , 50230 ,
50303 , 50310 , 50311 , 50312 , 50313 , 50320 , 50321 , 50322 , 50323 , 50330 ,
50403 , 50410 , 50411 , 50412 , 50413 , 50420 , 50421 , 50422 , 50423 , 50430 ,
50503 , 50510 , 50511 , 50512 , 50513 , 50520 , 50521 , 50522 , 50523 , 50530 ,
60203 , 60210 , 60211 , 60212 , 60213 , 60220 , 60221 , 60222 , 60223 , 60230 ,
60303 , 60310 , 60311 , 60312 , 60313 , 60320 , 60321 , 60322 , 60323 , 60330 ,
60403 , 60410 , 60411 , 60412 , 60413 , 60420 , 60421 , 60422 , 60423 , 60430 ,
60503 , 60510 , 60511 , 60512 , 60513 , 60520 , 60521 , 60522 , 60523 , 60530 ,
70203 , 70210 , 70211 , 70212 , 70213 , 70220 , 70221 , 70222 , 70223 , 70230 ,
70303 , 70310 , 70311 , 70312 , 70313 , 70320 , 70321 , 70322 , 70323 , 70330 ,
70403 , 70410 , 70411 , 70412 , 70413 , 70420 , 70421 , 70422 , 70423 , 70430 ,
70503 , 70510 , 70511 , 70512 , 70513 , 70520 , 70521 , 70522 , 70523 , 70530 ,
80203 , 80210 , 80211 , 80212 , 80213 , 80220 , 80221 , 80222 , 80223 , 80230 ,
80303 , 80310 , 80311 , 80312 , 80313 , 80320 , 80321 , 80322 , 80323 , 80330 ,
80403 , 80410 , 80411 , 80412 , 80413 , 80420 , 80421 , 80422 , 80423 , 80430 ,
80503 , 80510 , 80511 , 80512 , 80513 , 80520 , 80521 , 80522 , 80523 , 80530 ,
90203 , 90210 , 90211 , 90212 , 90213 , 90220 , 90221 , 90222 , 90223 , 90230 ,
90303 , 90310 , 90311 , 90312 , 90313 , 90320 , 90321 , 90322 , 90323 , 90330 ,
90403 , 90410 , 90411 , 90412 , 90413 , 90420 , 90421 , 90422 , 90423 , 90430 ,
90503 , 90510 , 90511 , 90512 , 90513 , 90520 , 90521 , 90522 , 90523 , 90530 ,
100203 , 100210 , 100211 , 100212 , 100213 , 100220 , 100221 , 100222 , 100223 , 100230 ,
100303 , 100310 , 100311 , 100312 , 100313 , 100320 , 100321 , 100322 , 100323 , 100330 ,
100403 , 100410 , 100411 , 100412 , 100413 , 100420 , 100421 , 100422 , 100423 , 100430 ,
100503 , 100510 , 100511 , 100512 , 100513 , 100520 , 100521 , 100522 , 100523 , 100530 ,
110203 , 110210 , 110211 , 110212 , 110213 , 110220 , 110221 , 110222 , 110223 , 110230 ,
110303 , 110310 , 110311 , 110312 , 110313 , 110320 , 110321 , 110322 , 110323 , 110330 ,
110403 , 110410 , 110411 , 110412 , 110413 , 110420 , 110421 , 110422 , 110423 , 110430 ,
110503 , 110510 , 110511 , 110512 , 110513 , 110520 , 110521 , 110522 , 110523 , 110530 };

Physical Volume("Internal")={1000001, 2000001, 3000001,

10101 ,
10201 ,
10301 ,
10401 ,
10501 ,
10601 ,
20101 ,

20201 ,
20301 ,
20401 ,
20501 ,
20601 ,
30101 ,
30201 ,
30301 ,
30401 ,
30501 ,
30601 ,
40101 ,
40201 ,
40301 ,
40401 ,
40501 ,
40601 ,
50101 ,
50201 ,
50301 ,
50401 ,
50501 ,
50601 ,
60101 ,
60201 ,
60301 ,
60401 ,
60501 ,
60601 ,
70101 ,
70201 ,
70301 ,
70401 ,
70501 ,
70601 ,
80101 ,
80201 ,
80301 ,
80401 ,
80501 ,
80601 ,
90101 ,
90201 ,
90301 ,
90401 ,

90501 ,
90601 ,
100101 ,
100201 ,
100301 ,
100401 ,
100501 ,
100601 ,
110101 ,
110201 ,
110301 ,
110401 ,
110501 ,
110601 ,
120101 ,
120201 ,
120301 ,
120401 ,
120501 ,
120601 };

//*****END OF SECOND SECTION THAT NEEDS MANUAL UPDATE*****