

UNIVERSITY OF OSLO
Department of Informatics

**NP domino logic
gates for Ultra Low
Voltage and High
Speed applications**

Master thesis

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Spring 2013



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Abstract

In this thesis we present different configurations of digital circuits exploiting Ultra Low Voltage (ULV) NP domino logic style. The proposed logic style is utilized with the help of Floating gate transistors.

The proposed NP domino logic gates are aimed to perform high speed operations in Ultra Low Voltage applications. The presented circuits may operate near the sub-threshold regime where the supply voltage is near the threshold voltage of the transistors. In terms of frequency, speed, robustness, Power Delay Product (PDP) and Energy Delay Product (EDP), the proposed ULV NO domino logic gates may offer significant improvement compared to the conventional CMOS logic gates.

Different implementations of NOT, NAND and NOR gates are presented using both conventional and Pass Transistor Logic styles. Further, NAND and NOR gates are used to employ different configurations of Carry gates which is a speed limited factor in many arithmetic operations. These ULV NP domino Carry gates are simulated at different supply voltages in the range of 100mV to 400mV, and the performance results are presented with respect to delay, power, PDP and EDP.

The proposed ULV NP domino Carry gates are cascaded together to perform addition in a 32-bit chain. The circuits are operated with respect to worst case scenario where the carry signal propagates through the whole chain. Multi-threshold (MTCMOS) and Variable-threshold (VTCMOS) techniques are employed in the ULV domino 32-bit carry chain in order to reduce the power consumption, meanwhile offering superb speed performance. Although the 32-bit carry chain offers a great advantage of speed improvement in the worst case scenario, the chain also introduces the drawback of enormous power consumption in the idle mode.

The work in this thesis has resulted in three papers. Two of these papers represent various configurations of 1-bit ULV NP domino Carry gates, while the third paper examines the performance of one of the proposed ULV NP domino carry gates in a 32-bit chain.

The simulation results presented in this thesis are obtained using a 90nm *TSMC* CMOS process.

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Acronyms

<i>ALU</i>	Arithmetic Logic Unit
<i>ASIC</i>	Application-Specific Integrated Circuit
<i>Avg</i>	Average
<i>CMOS</i>	Complementary Metal Oxide Semiconductor
<i>Dev</i>	Deviation from the rails
E_N	nMOS evaluation transistor
E_P	pMOS evaluation transistor
<i>EDP</i>	Energy Delay Product
<i>FBB</i>	Forward Body Biasing
<i>FG</i>	Floating Gate
<i>FPU</i>	Floating Point Unit
<i>GND</i>	Ground
<i>H – thr</i>	High threshold transistor
K_N	nMOS keeper transistor
K_P	pMOS keeper transistor
<i>KHz</i>	Kilo Hertz
<i>L – thr</i>	Low threshold transistor
<i>MEP</i>	Minimum Energy Point
<i>MHz</i>	Mega Hertz
<i>MOSFET</i>	Metal Oxide Semiconductor Field-Effect Transistor
<i>MTCMOS</i>	Multi-Threshold CMOS
<i>N type</i>	Output node precharges to 1
<i>NM</i>	Noise Margin

<i>nMOS</i>	N-channel MOSFET
<i>P type</i>	Output node precharges to 0
<i>PDN</i>	Pull Down Network
<i>PDP</i>	Power Delay Product
<i>pMOS</i>	P-channel MOSFET
<i>PTL</i>	Pass Transistor Logic
<i>PUN</i>	Pull Up Network
R_N	nMOS recharge transistor
R_P	pMOS recharge transistor
<i>RBB</i>	Reverse Body Biasing
<i>S - thr</i>	Standard threshold transistor
T_D	Propagation Delay
T_F	Fall Time
T_R	Rise Time
<i>TSMC</i>	Taiwan Semiconductor Manufacturing Company
<i>ULV</i>	Ultra Low Voltage
V_{DD}	The supply voltage
V_{TH}	Threshold Voltage of the transistor
<i>VLSI</i>	Very Large-Scale Integration
<i>VTCMOS</i>	Variable-Threshold CMOS

Preface

This master thesis was carried out at the Department of Informatics, Faculty of Mathematics and Natural Sciences, University of Oslo (UiO) in the period January 2012 - May 2013. The thesis is for the grade as Master of Science in Nano and Micro-electronics and contributes 60 credits.

Executing the master thesis has been both ambitious and interesting. This project contributes a great experience in life. Among those, the most important is the publication of three papers. The work has also provided me the deeper knowledge and understanding for the Nano-electronic field and the challenges as the technology scales down.

First and foremost, I would like to thank my supervisor, Professor Yngvar Berg, for providing all the valuable guidance and inspiration. Thank you for believing in my work and for giving me the freedom to do what I wanted to do. Special thanks go to Amir Hasanbegovic for the technical support and for being an important source of inspiration and knowledge. Thanks to my fellow student Øystein Bjørndal for helping me with \LaTeX which made this thesis book even more beautiful.

A great thanks to the master lab buddies, Erlend, Erik, Dag, Patrick and Alex for fruitful discussions, quiz, jokes, video games at the lab, which makes long days to short. In addition, I would like to thanks all the employers at the micro electronics group for being so helpful, and for providing such a great working environment.

Last but not least, a great thanks to my parents and my family for their support and motivation throughout the whole project. And a very special thanks to my best friend and co-student, Abdul Wahab Majeed for being with me for 8 years in my study life, to support me, to motivate me, to stand-up with me and to tolerate me.

SOHAIL MUSA MAHMOOD

2nd May 2013

Chapter 1

Introduction

Since the first CMOS invention in 1960s, the CMOS technology has grown at an unprecedented rate than any other human invention in the modern era. As the portable devices (ipads, laptops, mobile phones) and wireless systems are becoming more and more common in everyday life, the demand for extended battery life, low weight of electronic devices and superior speed is becoming more and more challenging. CMOS is well known for the ultra-low power systems such as implantable medical devices that require longer lives with tiny batteries. The rapidly growing applications on these portable devices run out their batteries very quickly. Thus power consumption is becoming the major design concern.

1.1 Motivation

Several approaches have been suggested in [1], [2] in order to reduce power consumption of Very Large-Scale Integration (VLSI) circuits. Among those, scaling the supply voltage is one of the most efficient ways to reduce power and energy consumption as the power consumption in digital CMOS circuits is proportional to the square of the power supply voltage. The circuits operate at low supply voltages near or below the threshold voltages of the CMOS transistors. The reduction in the supply voltage degrades the CMOS transistor performance with respect to speed as the nodes are charged and discharged by weak/moderate inversion currents. By using the conventional CMOS technology at ultra low supply voltages, the operating frequencies of the digital circuits have been reduced to the range of KHz and low MHz. Several approaches are proposed in [2],[3], [4] in order to achieve high speed performance in the digital CMOS circuits when the supply voltage is scaled down.

A full adder plays an important role in many arithmetic units such as addition, subtraction, multiplication and division. Addition is the most fundamental arithmetical operation in any kind of processor, and building block for all other units. It has a significant use in Arithmetic Logic Unit (ALU), Floating Point Unit (FPU) and Application-Specific Integrated Circuit (ASIC) where high processing speed is critical. The main aim of this thesis is to implement the digital CMOS logic gates by exploiting the Floating-gate technique in order to enhance the speed performance of the

full adder at ultra low supply voltages.

1.2 Previous work

In the late 1980s, the floating gate transistors were used in non-volatile memory elements. During 1990s, new methods and techniques are suggested in [5], [6], [7], [8] in order to use floating-gate devices in different applications, for example, in audio recording products and flash memories.

In the recent years, floating gate (FG) technique is proposed for Ultra-Low Voltage, Low power applications in both analog and digital circuits. Floating gate technique can be fabricated using a standard CMOS process. It can be either poly-poly, MOS or metal-metal[9] where an extra capacitance is connected serially to the gate terminal of the MOS transistor. This makes the gate terminal charged and discharged and thus floating as the gate terminal is not connected to a fix potential. By tuning the charge at the floating node, a different DC level can be achieved than provided by the supply voltage headroom. This shifts the threshold voltage of the MOS transistor, which affects the active current of the transistor. The gates proposed in this thesis are influenced by ULV non-volatile FG circuits and recharge logic presented in [10] and [11] respectively. The ULV NP domino logic was first presented in [12].

1.3 Thesis Outline

- **Chapter 1** gives a brief introduction to the today's technology, and some challenges are discussed as the technology scales down. Further, the motivation for the thesis is given. The previous works are also stated exploiting the floating gate technology.
- **Chapter 2** follows an introduction to the conventional CMOS logic, dynamic logic, domino logic and NP domino logic. This chapter also provides some common definitions for various CMOS techniques and figure of merits in the CMOS digital circuits.
- **Chapter 3** describes the behavior of the CMOS transistors at ultra low supply voltages. Furthermore, the main challenges at ultra low supply voltages are briefly discussed with respect to speed performance, robustness and power consumption.
- **Chapter 4** represents a detailed description of the ULV NP domino inverters which are utilized in conjunction with floating gate transistors. Different configurations are shown in order to reduce the static current consumption and increase the robustness of the exploiting logic style.
- **Chapter 5** represents NAND and NOR logic gates using the NP domino floating gate logic style. Different implementations of these gates are shown using conventional and pass transistor logic style.

- **Chapter 6** represents the novel configurations of ULV NP domino Carry gates which are implemented with the help of proposed ULV NP domino logic gates. A complete performance of these Carry gates have been simulated and compared with conventional Carry gates at different ultra low supply voltages.
- **Chapter 7** shows different implementations of 32-bit carry propagation chains utilizing ULV NP domino Carry gates. Some challenges are discussed which can occur in long domino chains and suggestions are given to compensate with those challenges.
- **Chapter 8** represents the review and summary for the three papers written throughout the thesis.
- **Chapter 9** discusses some of the main aspects of the thesis.
- **Chapter 10** summarizes the main contributions of the thesis. Some ideas and suggestions are also mentioned in this chapter for the further contribution in the thesis work.
- **Appendix A** shows the truth tables for the main digital logic gates utilized in this thesis.
- **Appendix B** includes the papers written throughout the thesis.

Chapter 2

Background

2.1 Conventional CMOS logic

Conventional CMOS logic use complementary pull-down network (PDN) and pull-up network (PUN) to drive output node to 0 and 1 respectively. Both PDN and PUN are used when a transition arrives at the input nodes. Conventional logic is robust, easy to design and have good noise margins as far as circuits operate in strong inversion (super threshold region). Considering the example of a conventional NAND gate. The PUN consists of two pMOS transistors in parallel, and PDN consists of two serially connected nMOS transistors, which are connected to the power supply voltage (V_{DD}) and ground (GND) respectively.

The major drawback for the conventional logic style is that the transistors in both PDN and PUN switch on when the transitions arrive at the input nodes. This increases the total input capacitance and hence the delay. This logic uses more transistors to perform a logical operation as compared to dynamic logic. Thus it is not suitable for high density circuits.

2.2 Dynamic logic

To enhance the speed performance for the logic gates, the designers have implemented dynamic CMOS logic gates. Dynamic circuits typically use fewer transistors to implement a given logic function, which directly reduces the amount of capacitance being switched and improves the speed performance for the circuits. We use a clock signal ϕ to control the circuits as shown in Figure 2.1*b*.

Dynamic circuit operates in two phases. During the precharge phase, the clock ϕ is 0 which turns on the pMOS transistor P_1 , and the output node precharges to V_{DD} . During the evaluation phase, the clock ϕ is 1 which turns off P_1 . The output may remains high or become low depending upon the transitions at the input nodes in the evaluation phase. In the case of a NAND gate, both nMOS transistors N_1 and N_2 in the PDN must turn on to discharge the output node to GND .

The main advantages of dynamic logic over conventional CMOS logic are reduced switching activity due to hazards, elimination of short-circuit dissipation, and reduced parasitic node capacitances[1].

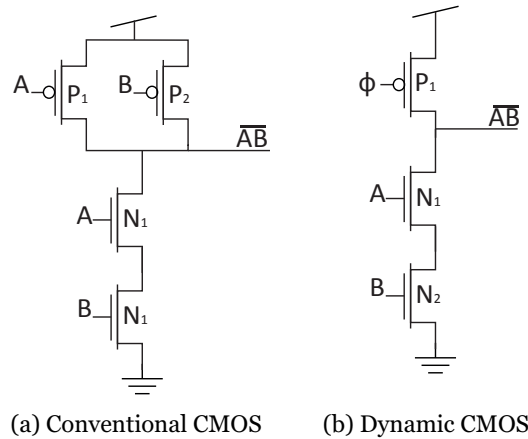


Figure 2.1: NAND gate.

2.2.1 Challenges in Dynamic logic

Timing and clock synchronization is the most critical task in the dynamic logic as the correct operation of the dynamic gates strongly depends upon the timing of the clock signal and the transitions at the input nodes[13]. If transitions arrive at any of the input nodes during the precharge phase in the dynamic gates, footed nMOS transistors must be implemented at the bottom of the PDN. The gate of the footed nMOS transistor will be controlled by ϕ . This prevents the output node to be discharged during the precharge phase.

One other major disadvantage of the dynamic circuits is the charge leakage at the floating nodes. For example, if PDN is off during the evaluation phase, the output node should ideally hold the precharged value. But the charge falls down slowly due to some leakage currents in the transistors. The evaluation phase should be short in order to prevent the leakage at the floating output node. Thus dynamic logic style is not suitable for the low frequency systems.

Another major problem occurs when the dynamic circuits cascaded in a chain as shown in Figure 2.2. As both cascaded inverters are precharged by the same clock signal ϕ , the output nodes of both inverters precharges to V_{DD} . This gives a logically incorrect value at the output node X of the second cascaded inverter when a positive transition arrives at the input node A . This concludes that the dynamic circuits which are sharing the same clock signal cannot cascade directly.

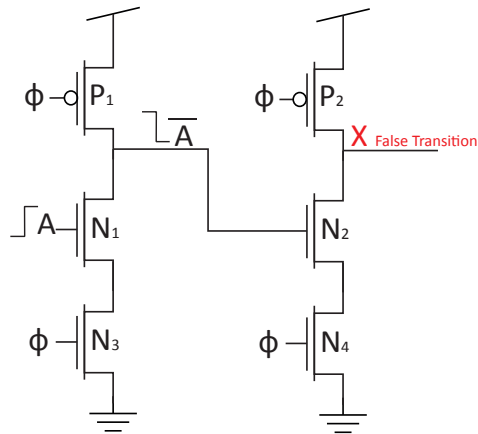


Figure 2.2: Dynamic cascade inverters.

2.3 Domino logic

Domino logic are utilized in the digital circuits such as microprocessors where high speed and area characteristics are critical. It has many advantages such as high speed operation, minimum used area and power consumption savings. Domino logic overcomes the cascaded problem faced by the dynamic logic gates.

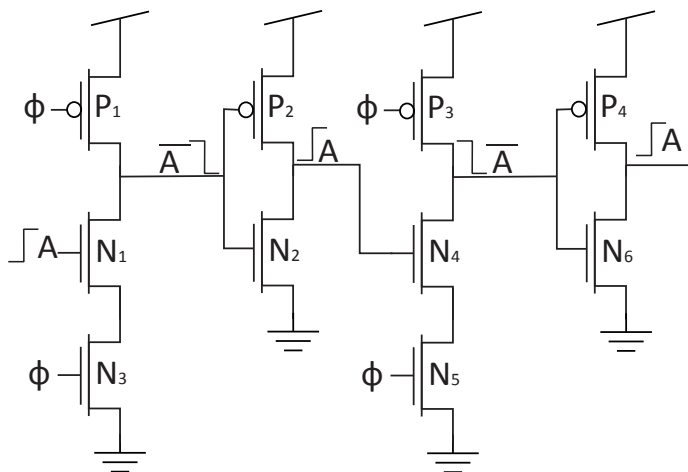


Figure 2.3: Domino cascaded inverters.

Figure 2.3 shows a chain of cascaded inverters connected in a Domino logic. The conventional CMOS inverters are connected at the output nodes of dynamic inverters, which are further connected to the dynamic inverters in the chain. During the precharge phase, the output nodes of the dynamic and the conventional inverters are precharged to V_{DD} and GND respectively. In the evaluation phase, the output node of the first dynamic inverter remains high or discharges to GND , depending upon the transition

at the input node. If the input transition is from 0 to 1, the effect may ripple through the whole chain, from the first to the last inverter, in the same way as the dominos trigger from the first to the last element in the chain.

Domino logic uses a single clock to precharge and evaluate all the logic gates within the chain. By using the same clock signal ϕ , precharging occurs parallel for each element in the chain, but the evaluation occurs serially, from the first to the last element in the domino chain. Domino logic is somehow better than dynamic logic, but the inclusion of conventional CMOS inverters at the output nodes of dynamic high speed inverters limit the speed performance for the proposed logic style.

2.4 NP Domino logic

NP Domino logic is used to substitute the conventional CMOS inverters at the output nodes of dynamic inverters in the domino logic. The conventional CMOS inverters are substituted with the precharged dynamic gates using PUN and an inverted clock signal $\bar{\phi}$ as shown in Figure 2.4. During the precharge phase, ϕ is low and $\bar{\phi}$ is high which precharges PDN and PUN to V_{DD} and GND respectively. During the evaluation phase, PDN discharges to GND and PUN charges to V_{DD} depending upon the transitions at the input nodes. The input transitions at the first NP domino gate ripple through the whole chain in a single evaluation phase.

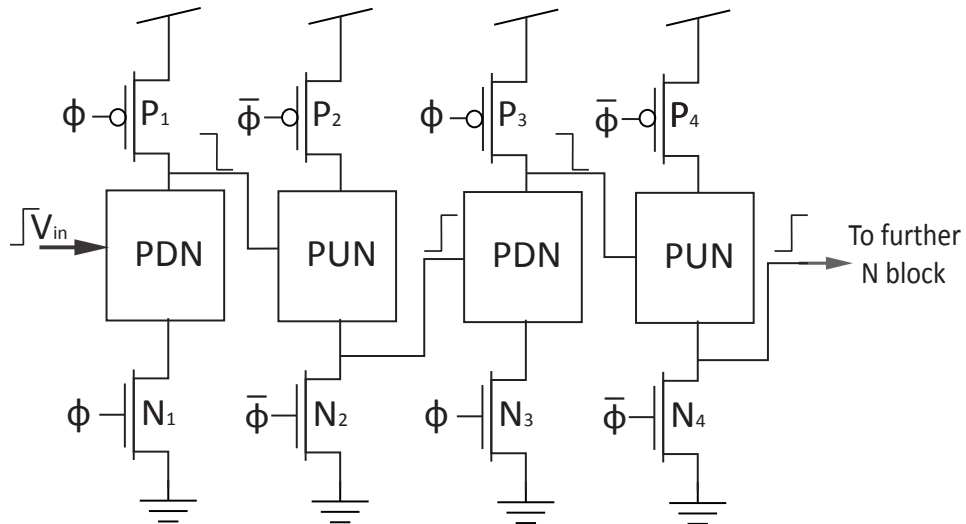


Figure 2.4: NP Domino Logic.

2.5 Keepers

As mentioned earlier, the dynamic circuits suffer from the charge leakage at the dynamic nodes. If a dynamic node is precharged high and then left floating, the voltage on the output node will reduce over time due to subthreshold, gate and junction leakage. Moreover, dynamic nodes have

poor noise margin. These two problems can be overcome by using keeper transistors[14]. The keeper is a weak transistor that holds the output node at the correct level when it would otherwise float. The keeper reduces the static current consumption by draining one of the transistors at the output node. The reduction in the static current reduces the overall power consumption. However the load capacitance at the output node increases, which degrades the speed performance slightly.

2.6 Floating gate

A floating gate transistor is a transistor whose gate terminal is not connected to a fix potential. The voltage at the floating node can be determined by capacitive division as shown in Figure 2.5. V_{in} is the input voltage, C_{in} is the capacitance at the floating terminal, C_{par} is the parasitic capacitance of the nMOS transistor E_{N1} and V is the voltage at the floating gate terminal. Voltage V at the floating node is determined in the following equation:

$$V = V_{init} + V_{in} * \frac{C_{in}}{C_{in} + C_{parasitic}} \quad (2.1)$$

V_{init} is the initial voltage at the floating gate terminal. The voltage at the floating gate terminal is programmed/recharged to an initial voltage by various means presented in [10]. Most often, V_{init} recharges to V_{DD} and GND for the pMOS and nMOS transistors respectively during the precharge phase.

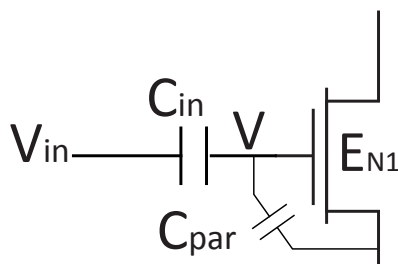


Figure 2.5: Floating gate transistor.

2.7 Pass Transistor Logic

Pass transistor logic (PTL) is a logic style that has been widely used in digital systems[1]. PTL is attractive as fewer transistors are used to implement the important digital gates, offering a huge advantage in terms of area consumption. The input capacitance is reduced, which reduces the overall delay and makes the circuit faster. In PTL, inputs are not only applied to the gate terminals, but also to the drain and source terminals. PTL suffers from threshold voltage drop for the transmitted signal which

results in the swing restoration at the output node and degrades the robustness performance.

2.8 Adder

Addition is the most fundamental arithmetical operation in any kind of processor, and is the building block for many processing operations like ALU, FPU and ASIC. Besides the addition task, it is also nucleus to many other arithmetic operations such as subtraction, multiplication and division etc. This makes the adder of great interest for many digital system designers. There are two types of adder circuits explained below.

2.8.1 Half Adder

If the addition operation of only two input bits is desired, a half adder is suggested. We have two bits input A and B and two bits output Sum and C_{out} . The logic function for the half adder is derived in the following equation.

$$\begin{aligned} Sum &= A \oplus B \\ C_{out} &= A \cdot B \end{aligned} \tag{2.2}$$

The Sum logic function corresponds to the XOR operation for the input bits A and B , while the C_{out} logic function corresponds to the AND operation for the input bits.

2.8.2 Full Adder

If the addition of more than two bits is desired, the half adder should be cascaded in a chain. To achieve the correct arithmetic operation, we should take into consideration the C_{in} bit from the previous adder in the chain. Thus a full adder has 3 inputs and 2 outputs. The logic function for the full adder is given in the following equation.

$$\begin{aligned} Sum &= (A \oplus B) \oplus C_{in} \\ C_{out} &= A \cdot B + C_{in} \cdot (A + B) \end{aligned} \tag{2.3}$$

The Sum and C_{out} for the full adder derives the same logic function as the half adder as far as C_{in} is 0.

2.9 Multi-threshold CMOS Technology

Multi-threshold CMOS (MTCMOS) is an efficient method with an alteration of CMOS chip technology having transistors with multiple/dual threshold voltages in order to optimize power or delay[15]. MTCMOS technique can be employed in the high speed circuits where low threshold transistors $L-thr$ are used in the speed critical paths to minimize the delay. However, high threshold transistors $H-thr$ are used in the non-critical paths to reduce the leakage power consumption.

2.10 Variable-threshold CMOS Technology

Variable Threshold CMOS (VTCMOS) is another efficient method to reduce the leakage power for the high speed circuits[16]. The speed critical transistors can be biased by adopting VTCMOS technology as these transistors should only operate in the active mode of operation. The substrate bias voltage of these speed critical transistors can be varied in order to achieve low threshold voltage in the active mode of operation and high threshold voltage otherwise. However, the main drawback is the fabrication of these VTCMOS devices as it requires twin or triple well technology to achieve different bias voltage levels.

2.11 Delay

One common way to determine the speed performance of the digital circuits is by measuring the propagation time T_D between the input and the output signals. T_D is the time measured from the input signal reaches 50% of its logic swing to the output signal reaches 50% of its logic swing[17]. T_D depends upon various parameters given in the following equation:

$$T_D = \frac{V_{DD} \cdot C_L}{I_{on}} \quad (2.4)$$

V_{DD} is the supply voltage, C_L is the load capacitance and I_{on} is the active current running through the on transistors.

Another common way to measure the delay is by determining the difference between the rise/fall time for the input and output signals. Rise time T_R is the time for a signal to rise from 20% to 80% of its steady state value. Fall time T_F is the time for a signal to fall from 80% to 20% of its steady state value. These two delays are also used to utilize the transition times for different signals.

2.12 Figure of Merit in logic gates

The performance for the digital circuits can be presented according to Power-Delay-Product (PDP) and Energy-Delay-Product (EDP). PDP and EDP are two common figure of merits which are correlated with power and energy efficiency for the digital gates respectively.

2.12.1 Power Delay Product

PDP is the product of power consumed in a switching event times the propagation delay T_D . Power is determined by multiplying the average consuming current I_{on} per transition times the supply voltage V_{DD} . The formula for PDP is driven in the following equation.

$$\begin{aligned} PDP(J) &= Power \cdot T_D \\ &= (I_{on} \cdot V_{DD}) \cdot \left(\frac{V_{DD} \cdot C_L}{I_{on}} \right) \\ &= V_{DD}^2 \cdot C_L \end{aligned} \quad (2.5)$$

The unit of PDP is Joule (j). PDP is only dependent upon the supply voltage V_{DD} and the load capacitance C_L and not on the ON-current I_{on} running through the logic gate.

2.12.2 Energy Delay Product

EDP can be implemented by multiplying the PDP with the input-output delay T_D for the logic gate. The unit for EDP is Joule second (js). Formula for driving the EDP is shown in the following equation:

$$\begin{aligned} EDP(Js) &= PDP \cdot T_D \\ &= (V_{DD}^2 \cdot C_L) \cdot \left(\frac{V_{DD} \cdot C_L}{I_{on}}\right) \\ &= \frac{V_{DD}^3 \cdot C_L^2}{I_{on}} \end{aligned} \tag{2.6}$$

EDP is useful figure of merit in high speed digital circuits as it weights the switching time more than the power consumption. It is dependent upon the supply voltage V_{DD} , load capacitance C_L and the ON-current I_{on} . As EDP is inversely proportional to the I_{on} , thus increasing the current results in low EDP.

Chapter 3

Performance of CMOS at ultra low supply voltages

Scaling down the supply voltage V_{DD} is one of the most efficient way to reduce the power consumption in many new applications, such as ambient intelligence, wireless sensor networks, mobiles, laptops and other energy-scavenging systems. It reduces the cost for the system maintenance and extends the battery's life time.

3.1 Challenges at low supply voltages

Although there are many advantages as the supply voltage scales down to the near-threshold region where the transistors may operate in the weak inversion or moderate inversion region. There are also arising some major challenges in the performance of the digital CMOS circuits. The major impact is on the speed performance as the ON-current I_{on} degrades exponentially when the transistor is on. A current model for the transistor operating at ultra low supply voltages is given in the following equation[18]:

$$I = I_0 \cdot \frac{W}{L} \cdot e^{(V_{GS}-V_{TH})/nv_t} \cdot (1 - e^{-V_{DS}/v_t}) \quad (3.1)$$

where I_0 is the technology-dependent subthreshold current, v_t is the thermal voltage, n is the subthreshold factor, $\frac{W}{L}$ is the sizing ratio of the transistor, V_{GS} represents the gate source voltage, V_{DS} represents the drain source voltage and V_{TH} represents the threshold voltage of the transistor.

When the transistor is switched on, the ON-current I_{on} degrades exponentially with the scaling of the supply voltage V_{DD} . As mentioned earlier, this directly impacts on the speed performance of the CMOS circuits as the switching delay T_D is inversely proportional to I_{on} . To compensate with the speed performance, the transistor's threshold voltage V_{TH} should be reduced by increasing the strength factor F of the transistor.

However lowering the threshold voltage of the transistor causes an exponential increase in the transistor's OFF-current I_{off} at ultra low supply voltages. This is due to the exponential dependency of current I on $V_{GS} - V_{TH}$. In the super threshold region, V_{TH} is high enough at $V_{GS} = 0$ that I is very small when the transistor is off. However, when the supply voltage

scales down and V_{TH} is reduced to compensate with the speed performance, I_{off} increases at $V_{GS} = 0$ due to exponential inverse proportionality. I_{off} is also known as the weak inversion current and the subthreshold leakage current I_{lk} [19].

Scaling down the supply voltage also degrades the robustness performance of the circuit to a certain extent. Robustness can be determined by obtaining the Noise Margin (NM). NM allows to determine the allowable noise voltage on the input of a gate so that the output will not be corrupted. One way to derive NM is shown in the following equation:

$$NM = \frac{I_{on}}{I_{off}} \quad (3.2)$$

NM is the ratio between the ON-current I_{on} and OFF-current I_{off} . This ratio reduces as both I_{on} decreases and I_{off} increases at low supply voltages.

3.2 F : The strength tunable factor of the transistor

The strength factor of the transistor is dependent upon the threshold voltage V_{TH} of the transistor. I_{on} increases by lowering V_{TH} . V_{TH} is tuned by tuning the strength factor of the transistor F . The strength tunable factor F is driven in the equation below[18]:

$$F = I_0 \frac{W}{L} e^{-(V_{TH0} - \lambda_{BS} V_{SB})/n\phi_t} \quad (3.3)$$

where λ_{BS} is the body effect coefficient, V_{SB} is the substrate bias voltage through the body effect and V_{TH0} is the zero-bias threshold voltage. The strength Factor can be tuned by:

- Adjusting the W/L ratio.
- Selecting the zero-bias threshold V_{TH0} among the low/standard or high values available in the adopted technology.
- Adjusting the substrate bias voltage V_{SB} .

The plots shown in Figure 3.1 determines I_{ON} through an nMOS transistor at a supply voltage of 300mV with different sizing parameters of the transistor. The graph demonstrates that increasing the length L of the transistor is more preferable than width W in order to achieve higher I_{ON} at ultra low supply voltages. This happens due to the reverse short channel effect (RSCE) which increases I_{ON} that further lowers the threshold voltage V_{TH} of the transistor[20]. I_{ON} increases linearly as L increases up to $2.5 \times L_{min}$, however increasing L over $2.5 \times L_{min}$ is not helpful due to the inverse proportionality between F and L as shown in the equation above.

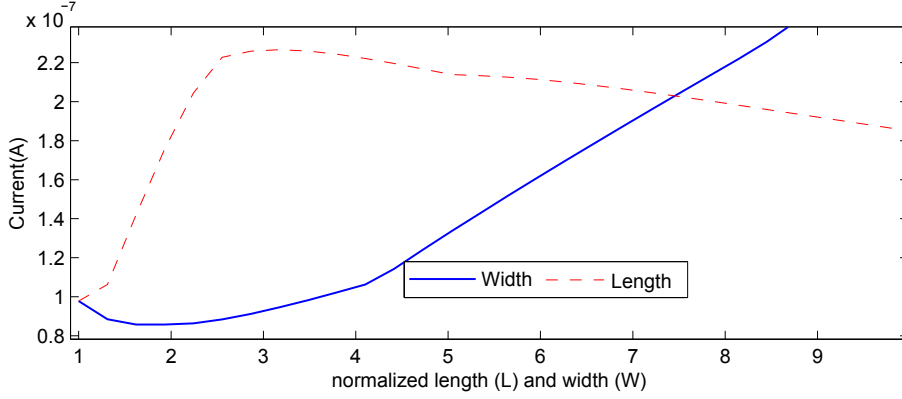


Figure 3.1: The ON-current I_{ON} through an nMOS transistor with different dimensions.

According to the graph in Figure 3.1, increasing the transistor's width W is not an effective node up to $3 \times W_{min}$ as I_{ON} decreases in this range. W should be almost $7 \times W_{min}$ to increase I_{ON} with the same factor as achieved by increasing L $2.5 \times L_{min}$.

The second method to increase the transistor strength is to select the zero-bias threshold V_{TH0} among the low threshold ($L-thr$), standard threshold ($S-thr$) and high threshold ($H-thr$) transistors available in the adopted technology, as V_{TH0} affects exponentially the transistor strength F . As shown in Table 3.1, implementing a $L-thr$ transistor instead of a $H-thr$ transistor lowers the relative threshold voltage almost 25%. However, $L-thr$ transistor increases the OFF-current I_{off} . Table 3.1 also represents different performance parameters for the various configurations of nMOS transistor. I_{ON} and P_{ON} represents the ON-current and the power consumption by nMOS transistor when transistor is on. I_{off} and P_{off} represents the off-current and power consumption by nMOS transistor when transistor is off.

F parameters			Relative thr (%)	I_{ON} (nA)	P_{ON} (nW)	I_{off} (pA)	P_{off} (pW)
Transistor	Sizing	Body biasing					
$S-thr$	$\frac{W_{min}}{L_{min}}$	RBB	100	87.8	26.34	22.97	6.89
$L-thr$	$\frac{W_{min}}{L_{min}}$	RBB	97	97.79	29.34	26.5	7.9
$H-thr$	$\frac{W_{min}}{L_{min}}$	RBB	122	6.37	1.91	1.8	0.567
$L-thr$	$\frac{W_{min}}{3 \times L_{min}}$	RBB	71	226.4	67.92	68.77	20.63
$L-thr$	$\frac{3 \times W_{min}}{L_{min}}$	RBB	118	92.65	27.97	27	8.105
$L-thr$	$\frac{W_{min}}{L_{min}}$	Flt	95	150.8	45.23	54.23	16.27
$L-thr$	$\frac{W_{min}}{L_{min}}$	FBB	90	235	70.54	116.4	34.9

Table 3.1: Relative threshold voltage (thr), I_{ON} , P_{ON} , I_{off} and P_{off} for various configurations of nMOS transistor.

The third method to increase the transistor strength is by tuning the substrate bias voltage V_{SB} as it has also an exponential dependency on the transistor strength F . This tuning node is not so effective in the above-threshold circuits, as F has a much weaker dependency on V_{SB} .

Three common techniques for body biasing are Forward Body Biasing (*FBB*), Reverse Body Biasing (*RBB*) and keep the body terminal floating (*Flt*). The conventional CMOS circuits are connected traditionally by using *RBB* technique, which increases the threshold voltage V_{TH} of the transistor, reducing the power consumption at the cost of reduced speed performance.

Flt and *FBB* are often used in the speed critical paths. The substrate of an nMOS transistor can be either remain floating or connect by V_{DD} by utilizing *Flt* or *FBB* schemes respectively. This decreases the threshold voltage V_{TH} of the transistor which further increases the speed performance of the gates, however the drawback is the increment in the power consumption. Table 3.1 concludes that the threshold voltage is only 95% and 90% relative to *RBB* by utilizing *Flt* and *FBB* body biasing technology respectively. As concluded from the simulation results, Forward Body Biasing is the most effective body biasing scheme to reduce the threshold voltage of the transistor in order to achieve high speed performance.

3.2.1 Implementation of Deep n-well

Although Forward Body Biasing *FBB* and floating bulk terminals are the most effective biasing schemes to achieve higher ON-current I_{ON} by lowering the transistor threshold voltage. However applying these schemes can be a challenging task and increase the complexity of the circuit during the layout stage in the TSMC 90nm process as the demand of implementing deep n-well is necessary in order to isolate the body of nMOS transistors.

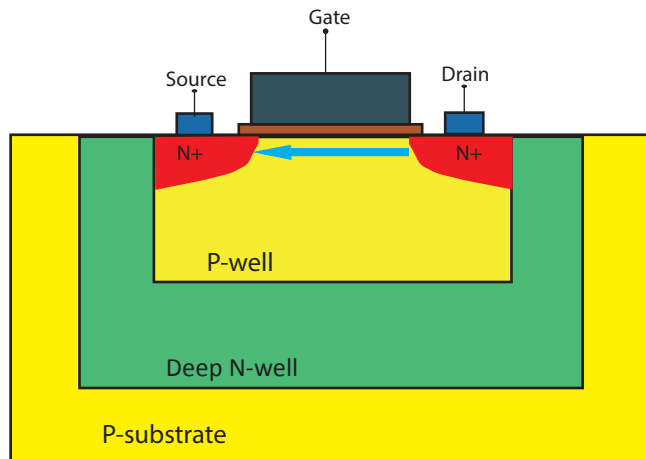


Figure 3.2: Deep n-well process architecture.

Generally a deep n-well is used to isolate the substrates of one or more nMOS transistors from the substrates of other nMOS transistors[21]. For

this purpose, deep n-well process is applied. The main disadvantage of implementing deep n-well is the increment in the area. An nMOS transistor with deep n-well can enlarge the area on the chip from 10 to 80 times depending upon different technologies. An nMOS transistor with deep n-well is shown in Figure 3.2. This approach is very common to use in order to suppress the substrate noise coupling injected by the digital logic in the mixed/RF environment[21].

A solution to avoid the use of deep n-well process is to implement the Dynamic Threshold Voltage MOSFET (DTMOS)[22] process instead of standard CMOS process. In DTMOS process, Silicon On Insulator (SOI) transistor is used which employs insulating substrate instead of silicon as the substrate. No wells or substrate contacts are needed in the design of the SOI process. However, some new challenges occur in the layout stage as mentioned in [23].

3.2.2 Imbalance factor between nMOS and pMOS

For a conventional CMOS inverter in the super threshold region, the mobility difference between nMOS and pMOS transistors are $\mu_n \approx 2\mu_p$, thus the width W of the pMOS transistor is $2 \times W_{\min}$ to obtain the same strength as the nMOS transistor. According to [20, 18], the imbalance factor IF between nMOS and pMOS transistors is given in the following equation:

$$IF = \left(\frac{\beta_n}{\beta_p}, \frac{\beta_p}{\beta_n} \right) \geq 1 \quad (3.4)$$

IF is defined as the strength ratio between the stronger and the weaker transistor. IF between the nMOS and pMOS is not a big issue in the superthreshold region as the nMOS transistor is twice as stronger as pMOS transistor. However as the supply voltage scales down, the transistor strength depends exponentially upon the threshold voltage V_{TH} . Thus a small difference in V_{TH} results in a higher imbalance factor.

When a logic gate suffers from a higher IF factor, its stronger transistor increases the leakage current of the corresponding logic gate due to its higher strength. On the other hand, the weaker transistor increases the gate delay. This concludes that a large imbalance tends to increase the leakage power and degrades the performance of the logic gate[20].

The DC analysis of the conventional CMOS inverter at a supply voltage of 300mV concludes that the IF between nMOS and pMOS is quite larger. The bulk terminal of the pMOS transistor remains *Floating* and the width W of the pMOS transistor is increased $2 \times W_{\min}$ to achieve the same strength as nMOS transistor, while nMOS transistor is minimum sized with conventional *RBB* scheme at the body terminal.

3.3 Power Dissipation in CMOS

The total power dissipation in a digital CMOS circuit consists of two main sources shown in the equation below:

$$P_{\text{Total}} = P_{\text{dynamic}} + P_{\text{static}} \quad (3.5)$$

where P_{dynamic} is the dynamic power consumption and P_{static} is the static power consumption.

3.3.1 Dynamic power dissipation

Dynamic power mostly consists of the switching power $P_{\text{switching}}$ and the short-circuit power P_{sc} in the digital CMOS circuits. When the transistors switch, $P_{\text{switching}}$ is dissipated during the charging/discharging of the load capacitance C_L at the output node. The general formula for driving the switching power consumption is given in the equation below:

$$P_{\text{switching}} = p_t \cdot f_{\text{clk}} \cdot C_L \cdot V_{\text{DD}}^2 \quad (3.6)$$

where f_{clk} is the switching frequency and p_t is the probability that a power consuming transition occurs which is also defined as the activity factor[1].

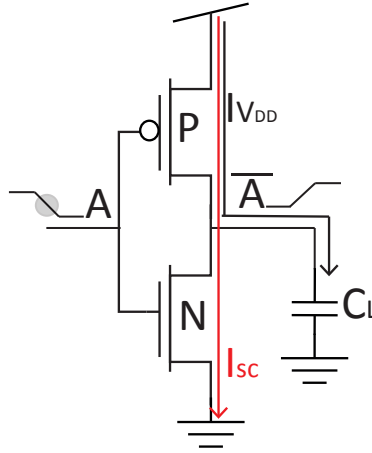


Figure 3.3: Dynamic power dissipation in a conventional CMOS inverter[24].

Short-circuit power P_{sc} is another main source of dynamic power dissipation. It occurs due to the direct flow of current I_{sc} from V_{DD} to GND during a transition at the input node, when both PUN and PDN are partially on for a short period of time. A conventional CMOS inverter implemented in Figure 3.3 shows the path of I_{sc} . The grey shaded circle at the negative input transition indicates the interval when the I_{sc} conducts a direct path from V_{DD} to GND . I_{sc} flows as long as the input voltage A is higher than nMOS threshold voltage (V_{THn}) and lower than pMOS threshold voltage (V_{THp}). According to [25], the short circuit power P_{sc} dissipation in conventional CMOS inverter is given in the following equation:

$$P_{\text{sc}} = K \cdot f_{\text{clk}} \cdot T_{\text{R,F}} \cdot (V_{\text{DD}} - 2V_{\text{TH}})^3 \quad (3.7)$$

where K is the constant that depends upon transistors dimensions and other process parameters, $T_{\text{R,F}}$ is the rise/fall time of the input signal, f_{clk} is

the switching frequency, V_{DD} is the supply voltage and V_{TH} is the threshold voltage of the transistors. The short-circuit power dissipation P_{sc} is linearly proportional to the $T_{R,F}$. Thus reducing $T_{R,F}$ would lead to a reduction in P_{sc} .

Dynamic power dissipation is the dominant power source in the digital CMOS circuits in the superthreshold regime. $P_{dynamic}$ contributes about 90% of the total power dissipation in the superthreshold regime[24]. However, $P_{dynamic}$ reduces significantly as the supply voltage V_{DD} scales down. This is due to the quadratically dependence of the switching power dissipation $P_{switching}$ upon V_{DD} . On the other hand, reducing V_{DD} also offers a significant reduction in the short-circuit power dissipation P_{sc} due to $(V_{DD} - 2V_{TH})^3$ factor.

3.3.2 Static power dissipation

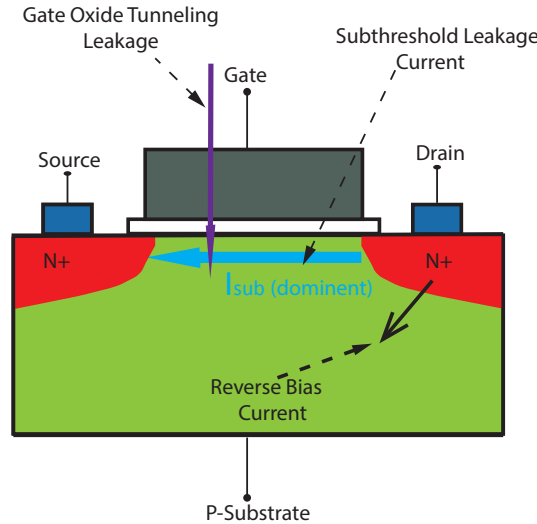


Figure 3.4: Leakage currents in a MOS transistor[26].

Dynamic power dissipation is often related to the transitions at the gate terminals of the transistors. However, static power consumption is caused by the leakage currents I_{lkg} without any transitions at the gate terminals. Ideally, CMOS digital circuits should not consume any power consumption in this mode. However, there are some leakage currents in the transistors which consume a certain amount of power.

The main leakage current sources I_{lkg} in a transistor are subthreshold leakage current I_{sub} , gate oxide tunneling current, gate-induced drain leakage and reverse bias current as shown in Figure 3.4. The leakage power can be determined by using the formula given in the equation below:

$$P_{lkg} = I_{lkg} \cdot V_{dd} \quad (3.8)$$

The static power consumption is not a dominant issue when the CMOS circuit operates in the superthreshold regime. However, it is the most

dominant power contributor as V_{DD} scales down. This happens due to the reduction in transistor's threshold voltage in order to enhance the speed performance. However lowering the threshold voltage gives an adverse affect on the static power consumption.

The subthreshold leakage current I_{sub} is the most dominant among all the leakage currents. I_{sub} is also known as the off-current I_{off} of the transistor. I_{sub} is the current flowing between the drain and source terminals in a CMOS transistor when the transistor operates in the cut-off region. Subthreshold leakage power can consume up to 60% of the total power consumption in 65nm technology[26].

The second most dominant leakage current is the Gate Oxide Tunneling Current. As the technology scales down, the gate oxide is becoming thinner. Thus aggressive scaling of the oxide thickness gives rise to high electric field, which results in high tunneling current through transistor's gate insulator. The gate leakage current increases exponentially with decreased oxide thickness. For the gate oxide thickness less than 15-20 Å, the gate tunneling current contributes the same amount of leakage current as the subthreshold leakage current[27].

Chapter 4

ULV NP domino Inverters

This chapter describes how the ULV NP domino logic style can be utilized in conjunction with floating gate transistors to realize high speed CMOS inverters. The original ULV domino inverters are first presented in [12] and shown in Figure 4.1.

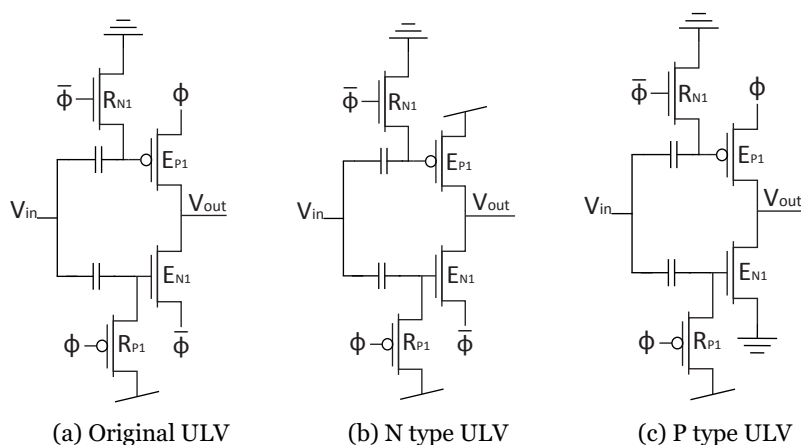


Figure 4.1: Different configurations of ULV domino inverters [12].

The configuration of various standard transistors exploiting ULV domino logic style is described below:

- **Evaluation transistors** labeled E_P or E_N . The evaluation transistors are the most important transistors in the proposed logic style which drive the output nodes.
- **Recharge transistors** labeled R_P or R_N . The recharge transistors are used to recharge the semi floating gate terminals of the evaluation transistors in the precharge phase.

The original ULV domino inverter shown in Figure 4.1a can be configured by applying the clock signals to power the inverter, i.e. the source terminals of E_P and E_N are connected to the clock drivers ϕ and $\bar{\phi}$ respectively. During the precharge phase, ϕ and $\bar{\phi}$ switches from 1 to 0 and 0 to 1 respectively, and the output node is precharged to $V_{DD}/2$. The output

node will be forced to 0 or 1 depending upon the positive or negative input transition respectively in the evaluation phase.

The ULV domino inverters shown in Figure 4.1b and 4.1c can be configured by applying the clock signals to power the inverters, i.e. either by connecting the source terminals of E_P and E_N to $\bar{\phi}$ and V_{DD} respectively (N type) or by connecting the source terminals of E_P and E_N to ϕ and GND respectively (P type). During the precharge phase, the output node is precharged to 1 and 0 for N and P type gate respectively, resembling the NP domino logic style. In the evaluation phase, the output node will be forced to 0 or 1 depending upon the positive or negative input transition for the N and P type ULV domino inverter respectively.

The main differences between the Original and NP ULV domino gates are:

1. **Precharging.** The output nodes are precharged to $V_{DD}/2$ for the original ULV domino gates, while the output nodes are precharged to 0 and 1 for the P and N type ULV domino gates respectively.
2. **Input transitions.** Original ULV domino gates can response to both rising and falling input transitions in the evaluation phase, whereas the NP ULV domino gates can either response to rising or falling input transitions for N and P type ULV domino gates respectively.
3. **Current level.** The input current level for the NP ULV domino logic style is quite higher than original ULV domino logic style due to large input transition, as the input transition for the original ULV domino gate is $|V_{DD}/2|$ and the input transition for the NP ULV domino gate is $|V_{DD}|$.

4.1 N type ULV domino inverter

The ULV NP domino inverters presented in [12] can be modified by removing one of the input capacitors from the gate terminals of the evaluation transistors, i.e. E_P for the N type and E_N for the P type ULV domino inverters.

The N type ULV domino inverter is shown in Figure 4.2. The clock drivers ϕ and $\bar{\phi}$ are used as control signals for the recharge transistors R_{P1} and R_{N1} , and $\bar{\phi}$ is used as power signal for E_{N1} . The precharge and evaluation phase of the N type ULV domino inverter is characterized by:

- **Precharge phase.** The precharge phase starts when ϕ switches from 1 to 0. This turns on R_{P1} and recharges the gate of E_{N1} to V_{DD} . Meanwhile $\bar{\phi}$ switches from 0 to 1 which turns on R_{N1} and recharges the gate of pMOS transistor P_1 to 0. Thus both E_{N1} and P_1 turn on in the precharge phase and drive the output node V_{out} to V_{DD} . Figure 4.2a describes the precharge phase of the N type inverter. The gray shaded lines indicate the components which are not active during the precharge phase.
- **Evaluation phase.** The evaluation phase starts when the clock signals ϕ and $\bar{\phi}$ switch from 0 to 1 and 1 to 0 respectively. Both

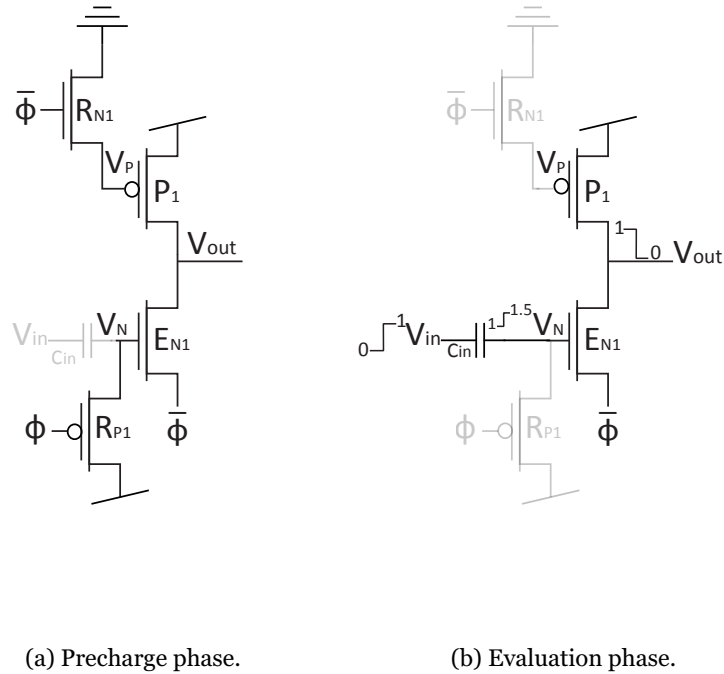


Figure 4.2: N type ULV domino inverter.

recharge transistors switch off which leaves the charge on nodes V_P and V_N temporarily floating allowing an input transition to affect the current running through the evaluation transistor E_{N1} . The output node V_{Out} floats as well until an input transition occurs. The gray shaded lines in Figure 4.2b indicate the components which are not active during the evaluation phase.

The input signal V_{in} must be *monotonically rising* to ensure the correct operation for the N type ULV domino inverter[28]. This can be only satisfied if

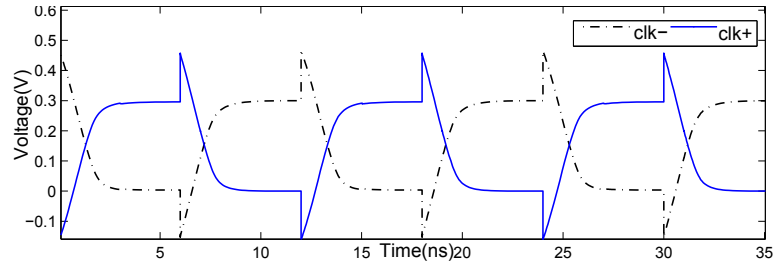
- Input signal V_{in} is low at the beginning of the evaluation phase, and
- V_{in} is only able to make a positive transition from 0 to 1 in the evaluation phase.

As a positive transition is applied at the input node V_{in} , the input capacitance C_{in} at the gate terminal of E_{N1} charges and discharges. Thus the voltage at the floating node V_N alters. The voltage at V_N can be estimated by using the following equation:

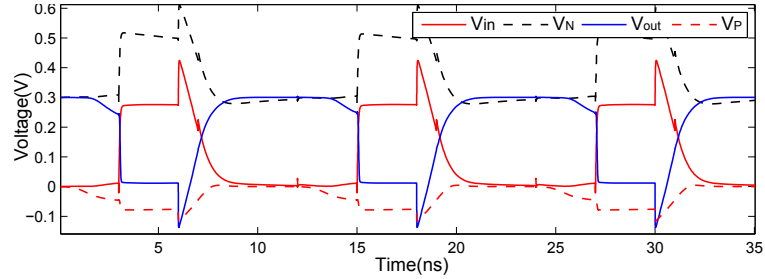
$$V_N = V_{init} + V_{in} * \left(\frac{C_{in}}{C_{in} + C_{parasitic}} \right) \quad (4.1)$$

We may assume that the initial voltage V_{init} at the floating node V_N is V_{DD} as the recharge transistor R_{P1} has recharged the floating node to V_{DD} in

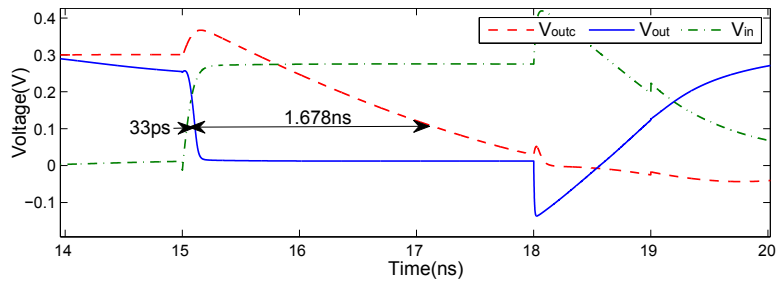
the previous precharge phase. V_{in} is charged up to V_{DD} as well due to the positive input transition. C_{in} is the input capacitance at the gate terminal of E_{N1} and C_{par} is the parasitic capacitance of E_{N1} . Assuming that C_{in} and C_{par} are equally sized, the potential at the floating node V_N becomes $1.5 \times V_{DD}$. This concludes that by using the floating capacitance to the transistors gate terminals, the floating nodes can achieve a different voltage than the voltage provided by the supply voltage V_{DD} [9]. This makes the evaluation transistor E_{N1} strongly biased which increases the current level of the transistor. Thus PDN becomes much stronger than PUN and the output node V_{out} discharges to 0.



(a) Waveforms of Clock signals for an ULV domino logic style.



(b) Voltage plot representing different nodes of N type domino inverter.



(c) N type domino compared to Conventional CMOS Inverter.

Figure 4.3: Simulation results of N type ULV domino inverter.

Simulation results for the N type ULV domino inverter implemented in Figure 4.2 are shown in Figure 4.3. The clock signals are operating at a frequency of 83.3MHz. To avoid underestimation of the implemented circuit and to obtain more realistic waveforms, clock signals have been made by inserting two symmetric conventional inverters between the ideal voltage sources and the clock signals. In the same way, input signal has been made by inserting ULV domino inverter between the voltage source

and the input nodes.

Plots in Figure 4.3b represents the simulated voltage at every node of N type domino inverter. Curve V_N indicates the floating node at the gate of E_{N1} . The voltage at this node varies in the evaluation phase when a positive input transition is applied. This makes the voltage at V_N much higher than V_{DD} which is proved by using the equation (4.1).

Figure 4.3c shows a comparison between the proposed N type ULV domino inverter and a conventional CMOS inverter. V_{out} indicates the output signal from N type ULV domino inverter while V_{outc} indicates the output signal from the conventional inverter. As shown in Table 4.1, the falling time T_F for N type domino inverter is almost 34 times faster than the conventional CMOS inverter in the evaluation phase when the output discharges from V_{DD} to GND . Curves in Figure 4.3c also demonstrates that the N type ULV domino inverter is almost 50 times faster than the conventional inverter, which is determined by finding the propagation delay between the input-output signals.

Delay (ps)	ϕ	$\bar{\phi}$	V_{in}	V_{out}	V_{outc}
T_R	846	844	81	X	X
T_F	805	813	X	63	2136
T_D	X	X	0	33	1678

Table 4.1: Simulation Results of different Delays of N type domino inverter.

Table 4.1 shows a summary of the delays between the most important curves shown in Figure 4.3. T_R of the input signal V_{in} is almost 10 times faster than the clock signals. The relative delay for the proposed N type UVL domino inverter is only 1.96% compared to the conventional CMOS inverter. X are the cases where we don't care about the falling or rising edge time. As we are dealing with N type domino inverter, we are only interested in the rising edge of the input signal and falling edge of the output signal. However, we do consider both rising and falling edges while operating with sequential circuits, for example, latches and flip-flops.

The performance of the proposed N type ULV domino inverter degrades due to a negative transition at the floating node V_p of the gate terminal of transistor P_1 in the evaluation phase. This is due to the parasitic capacitance associated with R_{N1} as $\bar{\phi}$ switches from 1 to 0. Furthermore, when a positive input transition occurs, the output node starts to pull down towards 0 which may add some additional negative transition at V_p . This makes P_1 slightly stronger in the evaluation phase. Thus the contention current is increased as PUN attempts to hold the precharged value, while the PDN attempts to discharge the output node V_{out} to GND . Both speed and robustness performance for the N type ULV domino inverter degrades due the floating node at the gate terminal of P_1 .

The leakage problem mentioned in the previous paragraph can be minimized or eliminated by modifying the NP domino inverter as shown in Figure 4.4.

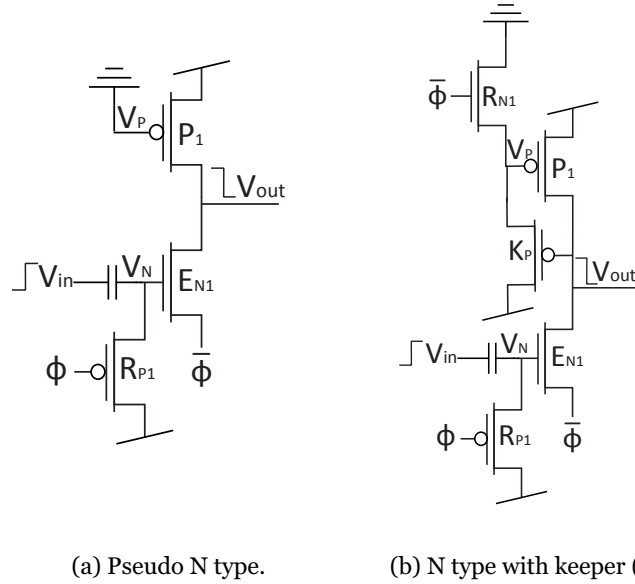
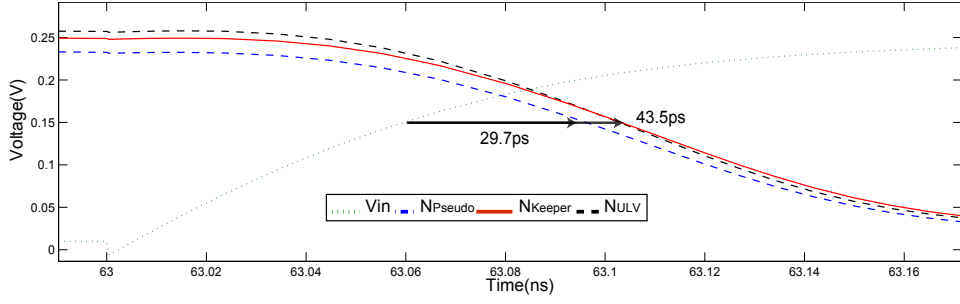


Figure 4.4: Different configurations of N type ULV domino inverter.

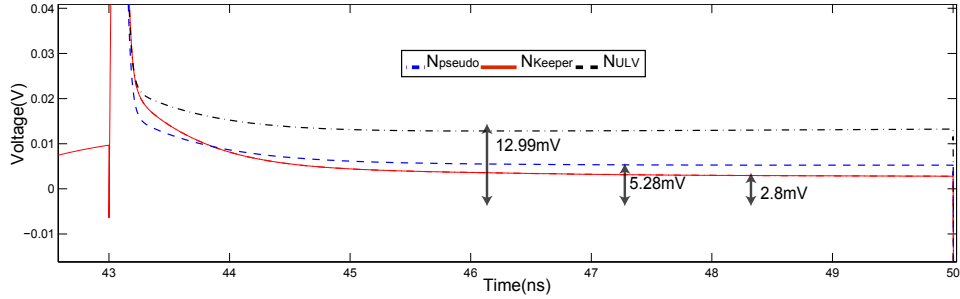
In Figure 4.4a, the gate terminal of P_1 is connected to a fix potential (GND) which is not affected by the parasitic capacitance associated with any recharge transistor. The circuit resembles pseudo nMOS logic. However, as P_1 is still switched on, the current I_{OFF} running through P_1 will increase the contention current as both PDN and PUN is on and impact on the total power consumption.

One other modified solution of N type ULV domino inverter is shown in Figure 4.4b. The pMOS keeper transistor K_P is connected in a feedback configuration to the gate terminal of P_1 in order to increase the ratio between ON-current I_{ON} and OFF-current I_{OFF} by decreasing I_{OFF} running through P_1 . K_P is not active during the precharge phase as the output node precharges to 1. In the evaluation phase, K_P does not turn on until the output node changes from 1 to 0 with a positive transition at the input node V_{in} . When K_P turns on, the voltage at the floating node V_P rises from 0 to 1 and P_1 turns partially off. This reduces I_{OFF} running through P_1 . The PUN becomes weaker, and the output node V_{out} fully discharges to GND . This proves that using the keeper transistor in the proposed ULV domino logic style eliminates the problem of poor noise margin by increasing I_{ON}/I_{OFF} . The power consumption is minimized as well due to the reduction in I_{OFF} .

Different configurations of N type ULV domino inverter are simulated and the results are demonstrated in the graphs in Figure 4.5. V_{in} represents the monotonically rising input signal, N_{pseudo} , N_{Keeper} and N_{ULV} represents the outputs from N type ULV inverter, N type ULV pseudo inverter and N type ULV inverter with keeper transistor which are implemented in Figure 4.4a, 4.4b and 4.2 respectively. With respect to speed performance, N type ULV pseudo inverter offers the minimum delay of only 29.7ps, whereas the delay of N type ULV inverter with keeper transistor is somehow increased



(a) Delay of different configurations.



(b) Robustness of different configurations.

Figure 4.5: Simulation results of different configurations of N type ULV domino inverter.

due to extra load at the output node. With respect to robustness, N type ULV inverter with keeper transistor provides the best performance as expected, offering a deviation of only 2.8mV from the rail (GND) after the transition at the output node. N type ULV pseudo inverter and N type ULV inverter offer the deviation of 5.28mV and 12.99mV respectively.

Parameters	N_{ULV}	N_{pseudo}	N_{Keeper}
Delay (ps)	43.5	29.7	43.5
Power (nW)	38.9	20.81	10.5
Energy (aj)	1.69	.618	0.456
EDP (10^{-29} js)	7.36	1.83	1.98
Relative Delay(%)	1.96	1.76	2.6
Relative PDP(%)	37.5	13.7	10.1
Relative EDP(%)	0.97	0.24	0.26

Table 4.2: Performance of different configurations of N type ULV inverter relative to conventional CMOS inverter at a supply voltage of 300mV.

Table 4.2 represents the performance of different configurations of N type ULV domino inverter with respect to speed, power consumption, PDP and EDP. Further, the performance parameters are compared with the conventional CMOS inverter at a supply voltage of 300mV. N type ULV inverter with keeper transistor offers the best relative PDP and EDP of 10.1% and 0.26% respectively, with the best robustness performance.

4.2 P type ULV domino inverter

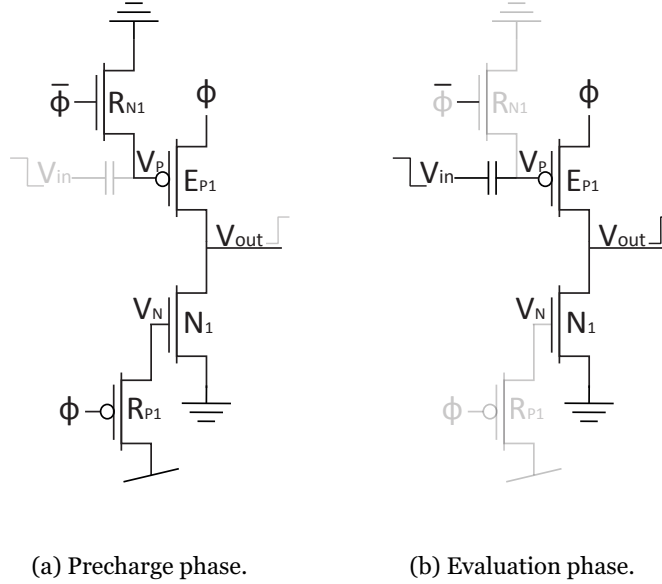


Figure 4.6: P type ULV domino inverter.

The circuit implemented in Figure 4.6 represents a P type ULV domino inverter, where the input capacitance is only applied to the gate terminal of evaluation transistor E_{P1} . The recharge/precharge and the evaluation phase for the P type ULV domino inverter is characterized below:

- **Precharge/Recharge phase.** Figure 4.6a shows the precharge phase, where the grey shaded lines indicate the components which are not active during the precharge phase. When ϕ switches from 1 to 0, the circuit operates in the precharge/recharge phase. During this phase, R_{P1} turns on and recharges the gate of N_1 transistor to 0. Meanwhile $\bar{\phi}$ switches from 0 to 1 which turns on R_{N1} and recharges the gate of E_{P1} to 0. Thus both evaluation transistors N_1 and E_{P1} turn on and precharge the output node V_{out} to GND .
- **Evaluation phase.** Figure 4.6b shows the evaluation phase of P type ULV domino inverter, where the grey shaded lines indicate the components which are inactive in this phase. Clock drivers ϕ and $\bar{\phi}$ switch from 0 to 1 and 1 to 0 respectively. Both recharge transistors R_{P1} and R_{N1} switch off which make the voltage V_N and V_P on the gate terminals of N_1 and E_{P1} floating. The output node V_{out} floats as well until an input transition occurs.

The input signal V_{in} must be *monotonically falling* to ensure the correct operation for the P type ULV domino inverter. This can only be satisfied if

- input signal V_{in} is high at the beginning of the evaluation phase, and

- V_{in} only makes a single transition from 1 to 0 in the evaluation phase.

Negative transition at the input node V_{in} decreases the voltage at the floating node V_P on the gate terminal of E_{P1} . Thus E_{P1} becomes strongly biased compared to N_1 in the evaluation phase, and the output node V_{out} charges to V_{DD} .

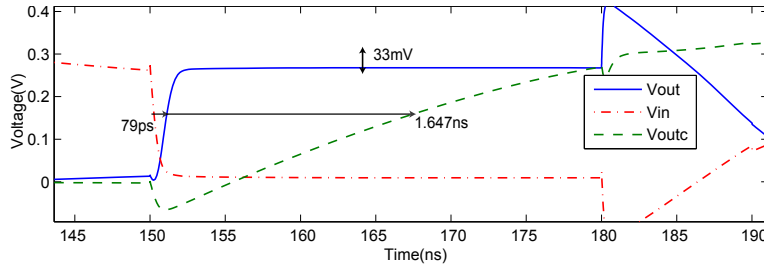


Figure 4.7: Speed performance of P type ULV domino inverter compared with conventional CMOS inverter.

Figure 4.7 shows the simulation results where the speed performance of the P type ULV domino inverter is compared with the conventional CMOS inverter. V_{in} represents the input signal, V_{out} and V_{outc} represents the output signals from proposed P type ULV inverter and the conventional inverter respectively. P type ULV domino inverter is 30 times faster than the conventional inverter at a supply voltage of 300mV, providing a delay of only 4.7% relative to standard CMOS inverter. However the robustness performance degrades as the deviation from the rail (V_{DD}) is almost 33mV when the output node V_{out} is pulled up to V_{DD} in the evaluation phase.

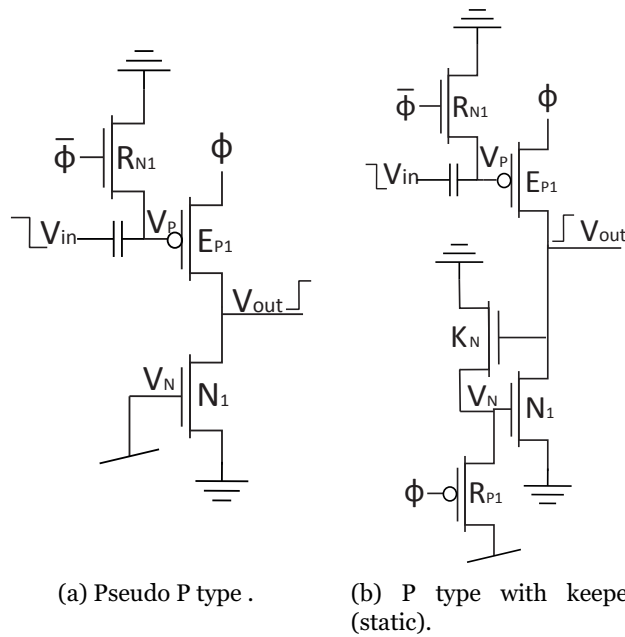


Figure 4.8: Different configurations of P type ULV domino inverter.

The robustness problem can be eliminated by modifying the P type ULV domino inverter as shown in Figure 4.8. Figure 4.8a resembles the pseudo logic style where the floating gate of N_1 is connected to a fixed potential (V_{DD}). This partially turns off N_1 which decreases the contention current and offers better robustness performance.

A new configuration of P type inverter is shown in Figure 4.8b, where a keeper transistor K_N is connected in a feedback configuration. K_N is connected at the floating gate terminal of N_1 transistor. K_N is inactive during the precharge phase as the output node V_{out} precharges to 0. In the evaluation phase, K_N does not turn on until V_{out} switches from 0 to 1 with a correct transition at the input node V_{in} . When K_N turns on, the voltage at the floating node V_N falls from 1 to 0. This partially turns off the evaluation transistor N and let the output node swings fully to V_{DD} . This helps to reduce the contention current which directly impacts on the robustness and power consumption of the proposed P type ULV domino inverter.

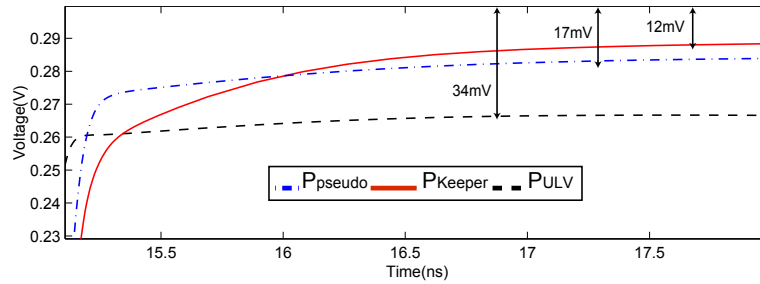


Figure 4.9: Robustness performance of different configurations of P type ULV domino inverter.

The graph in Figure 4.9 demonstrates the robustness performance of different configurations of P type ULV domino inverter in the evaluation phase. P_{ULV} , P_{psuedo} and P_{Keeper} represents the output signals from P type ULV domino inverter, pseudo P type ULV domino inverter and P type ULV domino inverter with keeper respectively. As expected, P_{Keeper} offers the best robustness performance, providing the deviation of only 12mV from the rail (V_{DD}). P_{ULV} and P_{psuedo} offers a deviation of 17mV and 34mV respectively.

4.3 A chain of ULV NP domino inverters

So far, the proposed ULV NP domino inverters are only simulated with small capacitive loads at the input and output nodes. To obtain more correct and realistic performance, the proposed logic style should be simulated in a domino chain. The output node of an N type domino inverter is connected at the input node of a P type domino inverter, as shown in Figure 4.10. A chain of 8 NP domino inverters is implemented to observe speed and robustness behavior of ULV NP domino inverters with a certain load both at the input and the output of each inverter.

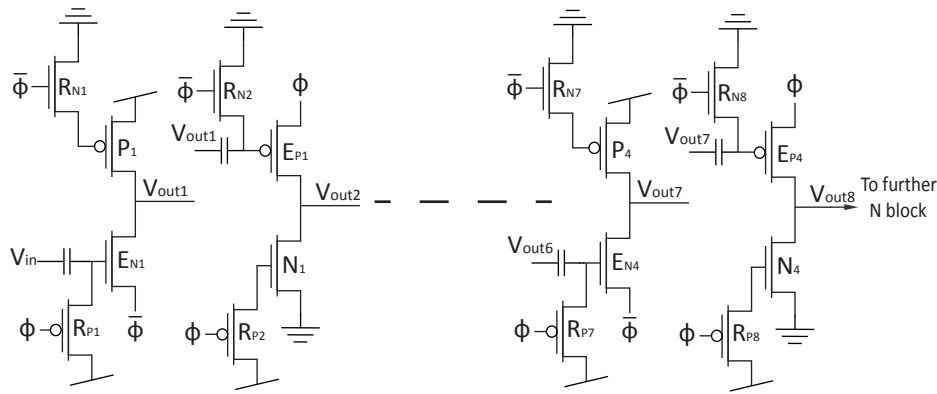
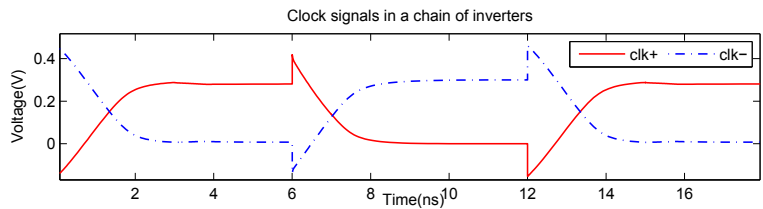
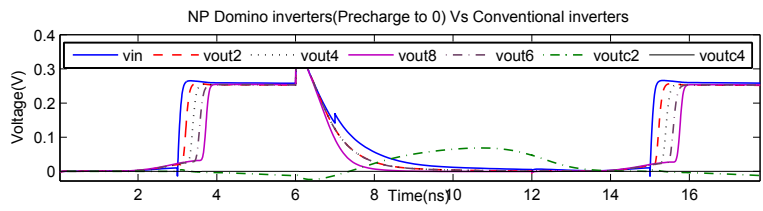


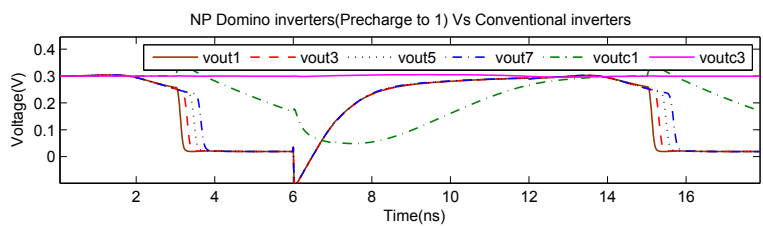
Figure 4.10: ULV NP domino chain with 8 inverters.



(a) Clock drivers presenting precharge and evaluation phase.



(b) Output nodes of P type ULV domino Inverters.



(c) Output nodes of N type ULV domino Inverters.

Figure 4.11: Simulation results of 8 ULV NP inverters in a domino chain.

The simulation results for a domino chain of 8 ULV NP inverters are shown in Figure 4.10. The curves in Figure 4.11a represent the clock signals ϕ and $\bar{\phi}$ which are used both as control and reference signals for ULV NP domino inverters. The graph in Figure 4.11b represents the input signal V_{in} which has a positive transition. The input arrives at the floating node of an N type ULV domino inverter that has an output which precharges to 1 in the precharge phase. The output signal V_{out1} discharges to 0 in the evaluation phase, which is connected further to the input node of P type ULV domino

inverter whose output precharges to 0 in the precharge phase. The curves in Figure 4.11b represent the outputs from 2nd, 4th, 6th and 8th P type domino inverters in the chain. In the same graph, the outputs from a chain of 8 conventional CMOS inverters V_{outc} have been compared with the domino inverters.

The subgraph in Figure 4.11c represents the outputs from 1st, 3rd, 5th and 7th N type domino inverters in the chain. The outputs from N domino inverters have been compared with the conventional inverters. The plots in Figure 4.11 demonstrates the working principle of a domino logic. It states that all the output nodes precharge in parallel, while in the evaluation phase, depending upon the input transition at the 1st N type domino inverter, the output from the 1st N type inverter is triggered to the next P type inverter, and further in the domino chain. Within a single clock period, the input signal propagates through 8 NP domino inverters in a chain, utilizing the propagation delay of only 711ps.

The propagation delay from the input signal to every output signal in the ULV NP domino 8 inverters chain is shown in Table 4.3. The propagation delay between the input signal and the output from the 8th NP domino inverter is only 711ps, providing an average propagation delay of 88.8ps between each of the ULV NP domino inverters in the chain. The propagation delay between the input signal V_{in} and the output from the 1st conventional inverter V_{outc1} is about 3,033ns. This concludes that NP domino inverter is almost 50 times faster than the conventional CMOS inverter, while operating in a chain of 8 inverters. As seen in Figure 4.11, later output signals from the conventional inverter chain are obstructed due to low supply voltage and a high clock frequency of 83.3MHz.

Waveform	Waveform	Delay(ps)
V_{in}	V_{out1}	64
V_{in}	V_{out2}	178
V_{in}	V_{out3}	239
V_{in}	V_{out4}	361
V_{in}	V_{out5}	419
V_{in}	V_{out6}	548
V_{in}	V_{out7}	605
V_{in}	V_{out8}	711
V_{in}	V_{outc1}	3033

Table 4.3: Speed performance of ULV NP domino 8 inverters chain.

Chapter 5

ULV NP domino Logic gates

In the previous chapter, ULV NP domino inverters are taken into considerations which are dependent upon a single input transition in the evaluation phase, that results in an inverted transition at the output nodes. To implement larger and complex digital systems such as microprocessors and ALU, we need to deal with complex systems having multiple inputs. Logical gates like NAND and NOR are the main building blocks for these complex digital systems.

5.1 ULV NP domino NAND Gates

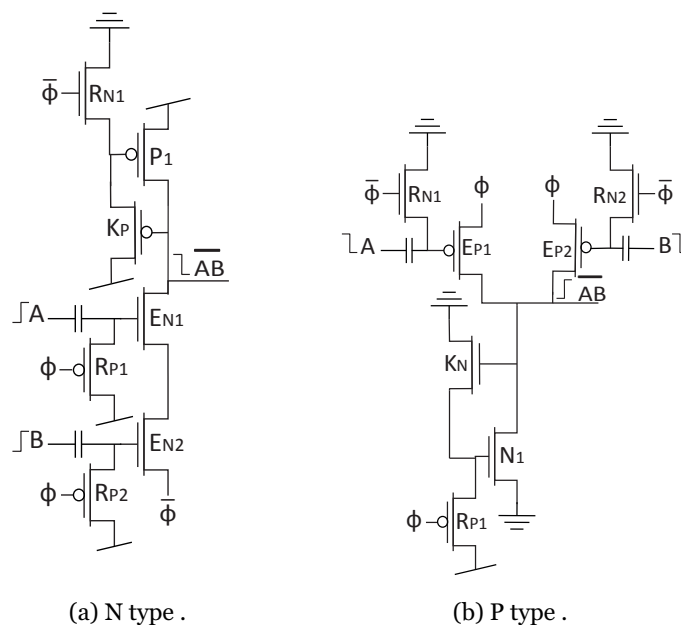


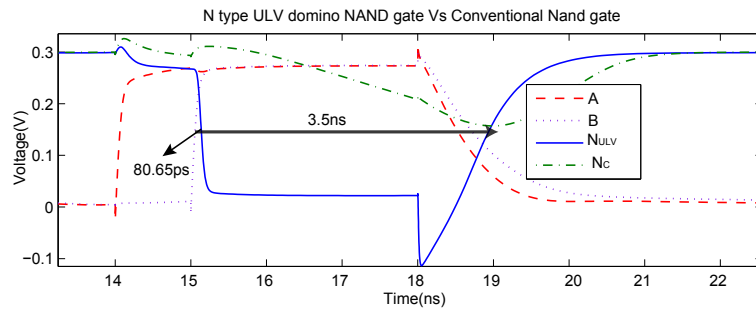
Figure 5.1: NP ULV domino NAND gate.

Figure 5.1 represents two different implementations of ULV domino NAND gates. Both implementations are utilized by NP domino logic in conjunction with floating gates on the evaluation transistors. ULV domino NAND gates in Figure 5.1a and 5.1b precharge the output node to 1 and 0 respectively

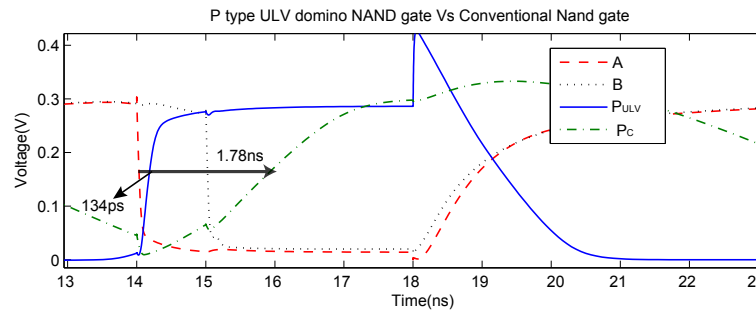
during the precharge phase. The precharge phase operates in the same way as described in the previous chapter. In the evaluation phase, the main difference is the two input signals A and B at the floating nodes of the gate terminals of the evaluation transistors.

In Figure 5.1a, both evaluation transistors E_{N1} and E_{N2} are serially connected, resembling the PDN for the conventional NAND gate. The output node is precharged to 1 in the precharge phase. In the evaluation phase, depending upon the transitions at the input nodes A and B , the output node is discharged to 0. Both evaluation transistors should turn on in the evaluation phase in order to discharge the output node to GND , otherwise there will be no direct path from the output node to GND and the output node will remain high and floating. The only case for the output node of a NAND gate to become 0 is when both of the inputs become high.

Figure 5.1b represents a P type ULV domino NAND gate which is implemented using two parallel pMOS evaluation transistors E_{P1} and E_{P2} in the PUN which resembles the PUN of the conventional NAND gate. Transistors E_{P1} , E_{P2} and N_1 precharge the output node to 0 during the precharge phase. In the evaluation phase, the output node is pulled up to V_{DD} when one of the two evaluation transistors E_{P1} or E_{P2} turns on. The only case for the output node to hold the precharged value is when both E_{P1} and E_{P2} remain switched off in the evaluation phase.



(a) N type



(b) P type

Figure 5.2: Simulation results of ULV NP domino NAND gates.

The subplot in Figure 5.2a demonstrates the simulation results of N type ULV domino NAND gate and a comparison is made against the conventional NAND gate with respect to speed performance. A and B are

the input signals with a positive transition from 0 to 1 in the evaluation phase. N_{ULV} is the output from the proposed N type domino NAND gate while N_C is the output from the conventional NAND gate. The output is high when both inputs are low, the output remains high as A has a positive transition because there is still no direct path from output nodes to GND . The output node N_{ULV} gets a negative transition when B changes from 0 to 1 while A has already got a positive transition. The propagation delay between the input signal and output N_{ULV} is only 81ps, which is almost 43 times faster than the conventional NAND gate. The conventional NAND gate has a propagation delay of 3.5ns. The conventional NAND gate is almost unable to operate on such a high frequency of 83MHz as the output node N_C needs more time to change its state from 1 to 0.

Simulation results in Figure 5.2b demonstrates the speed performance between the P type ULV domino NAND gate and the conventional NAND gate. A and B are the input signals. P_{ULV} and P_C are the output nodes from the proposed P type domino NAND gate and conventional NAND gate respectively. When one of the two inputs gets a negative transition in the evaluation phase, one of the two parallel connected evaluation transistor E_{P1} or E_{P2} turns on and the output node P_{ULV} is pulled up to V_{DD} . The propagation delay for the proposed P type ULV domino NAND gate is only 7.5% relative to the conventional NAND gate.

5.2 ULV NP domino NOR gates

In this Section, NOR gate is proposed by exploiting ULV NP domino logic style in conjunction with floating gate transistors. In general, NOR gate gives a high output when both of the input signals are low.

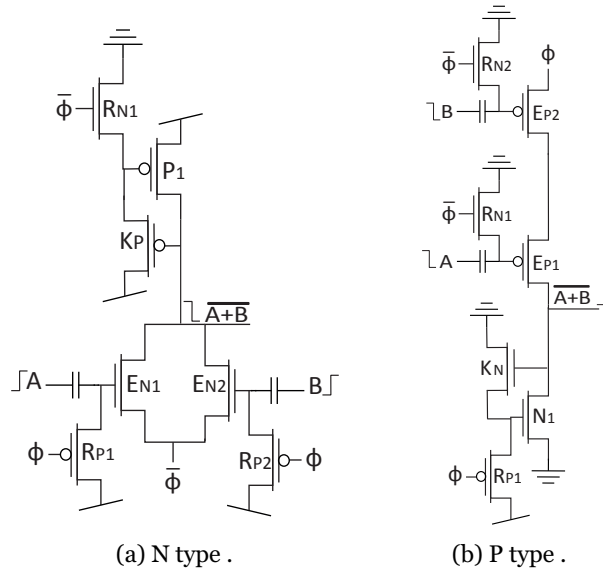
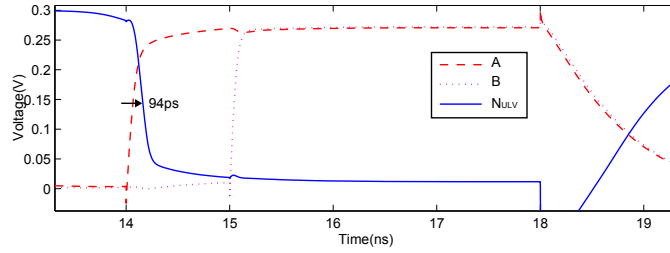


Figure 5.3: NP ULV domino NOR gate.

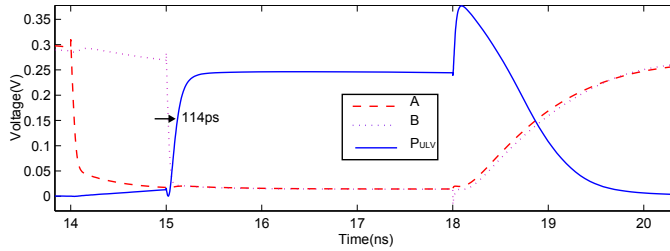
Two implementations of ULV NP domino NOR gates are proposed in

Figure 5.3. The output node of the N type ULV domino NOR gate in Figure 5.3a precharges to 1 in the precharge phase and discharges to 0 if one of the two input signals A or B switches from 0 to 1 in the evaluation phase.

The output node of the P type ULV domino NOR gate implemented in Figure 5.3b precharges to 0 in the precharge phase. The reference signal ϕ propagates through both serially connected pMOS evaluation transistors E_{P1} and E_{P2} when both transistors switch on in the evaluation phase and pulls up the output node to V_{DD} . This is only possible when negative transitions arrive at both input nodes A and B in the evaluation phase.



(a) N type.



(b) P type.

Figure 5.4: Simulation results of ULV NP domino NOR gates.

The graphs in Figure 5.4 shows the simulation results of NP ULV domino NOR gates with respect to speed performance. The simulation results in Figure 5.4a corresponds to the N type ULV domino NOR gate. The output node N_{ULV} is precharged to 1 in the precharge phase, and discharges to 0 when one of the two inputs A or B becomes high in the evaluation phase. The propagation delay between the input and the output node is about 94ps.

The graphs in Figure 5.4b corresponds to the simulation results for the P type ULV domino NOR gate. The output node P_{ULV} precharges to 0 in the precharge phase, and pulls to V_{DD} when both of the input signals A and B become 0. The propagation delay from the inputs switch to the output response is only 114ps. The output node of conventional NOR gate was unable to operate at such a high frequency with a supply voltage of 300mV.

5.3 ULV NP domino NAND/NOR gate using Pass Transistor Logic

Various configurations of digital logic circuits are implemented in [29] exploiting Pass Transistor logic (PTL) in conjunction with floating gate transistors. PTL is determined to obtain the same logic function by using

fewer number of transistors compared to the conventional logic style, which helps to reduce the overall delay and save the area on the chip. In this section, ULV NP domino NAND and NOR gates are proposed exploiting this logic style.

Circuit in Figure 5.5a operates as an N type ULV domino NAND gate. The evaluation transistor E_{N1} works as a pass transistor for the input signal \bar{B} with the increased current level at the gate terminal of E_{N1} as E_{N1} is strongly biased in the evaluation phase when a positive transition arrives at the input node A . In the evaluation phase, if both input signals A and B are 0, the output will remain to the precharged value. If A is high and B is low, E_{N1} turns on and transmits high \bar{B} from source to drain, which does not change the output node. If A is low and B is high, the output node holds the precharged value as E_{N1} is switched off. The only case for the output node to pull down to GND is when A switches from 0 to 1, while \bar{B} switches from 1 to 0 in the evaluation phase. This concludes that the implemented N type ULV domino gate operates as a NAND gate, by utilizing only a single evaluation transistor E_{N1} .

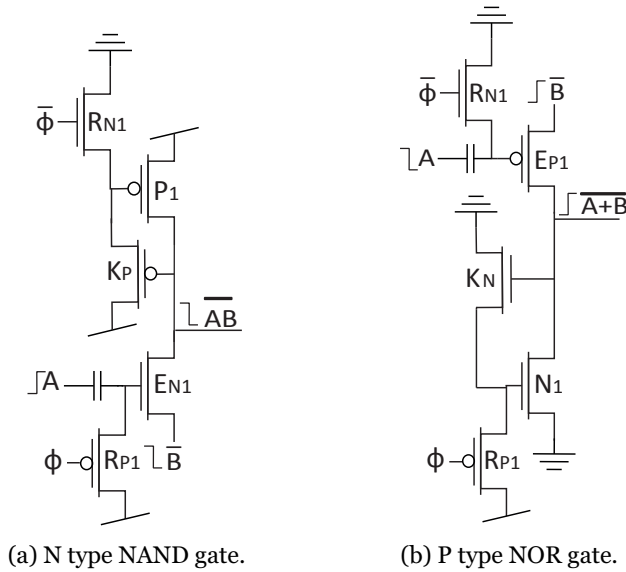
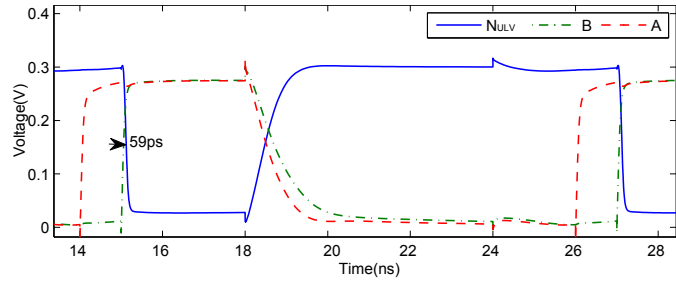


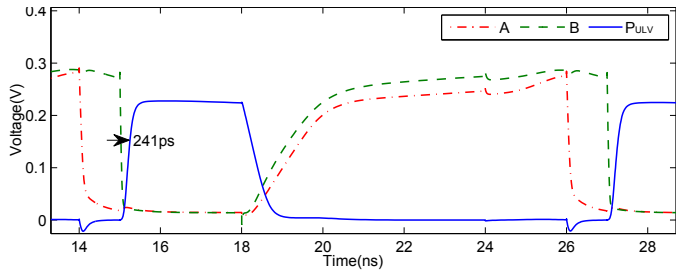
Figure 5.5: ULV NP domino logic Gates using PTL.

An ULV P type domino NOR gate is implemented in Figure 5.5b by exploiting PTL. The output node is precharged to 0 in the precharge phase. Evaluation transistor E_{P1} works as a pass transistor where the input signal A is applied at the floating gate of E_{P1} in the evaluation phase. The other input signal \bar{B} is applied to the source terminal of E_{P1} . The only possibility for the output node to become high is when A switches from 1 to 0 and \bar{B} switches from 0 to 1 in the evaluation phase. This concludes that the proposed P type ULV domino gate behaves as the NOR gate for input signals A and B .

The graphs shown in Figure 5.6 demonstrates the speed performance of proposed ULV NP domino NAND and NOR gates exploiting PTL. The subplot in Figure 5.6a corresponds to the proposed ULV N type domino



(a) N type NAND gate.



(b) P type NOR gate.

Figure 5.6: Simulation results of ULV NP domino logic gates using PTL.

NAND gate with PTL. The only possibility for the output node N_{ULV} to become 0 is when both of the input signals A and B receive positive transitions. The propagation delay for the proposed NAND gate is only 59ps, which shows a significant improvement in the speed performance as the overall capacitance of the logic gate is reduced by reducing the total number of transistors.

Simulation results in plot 5.6b corresponds to the P type ULV domino NOR gate using PTL. The output node P_{ULV} precharges to GND in the precharge phase and pulls only to V_{DD} when both of the input nodes A and B receive negative transitions in the evaluation phase. The propagation delay for the proposed NOR gate is 241ps, offering a high speed performance.

Chapter 6

ULV NP domino Carry gates for high speed Full Adders

A full adder plays an important role in many arithmetic units such as addition, subtraction, multiplication and division. Addition is the most fundamental arithmetical operation in any kind of processor, and building block for all other units. It has a significant use in ALU, FPU and ASIC where high processing speed is critical. Due to the high speed requirement, the full adder should be able to provide a superb speed feature as the supply voltage scales down.

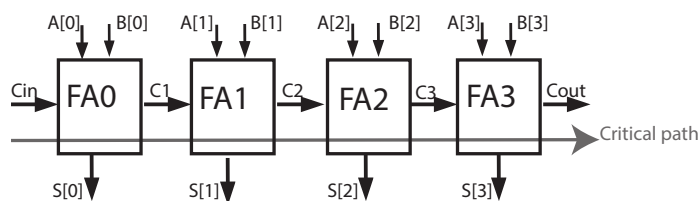


Figure 6.1: Four Bits Full Adder

A 4-bits full adder is implemented in Figure 6.1[28]. Four full adders are cascaded in a chain. The full adder is in the propagation mode when the input signals $A \neq B$ which makes $C_{out} = C_{in}$. The overall worst case delay is obtained when all the full adders are in the propagation mode and the carry signal propagates from the first to the last full adder in the chain. Thus carry propagation path is the most critical path when an addition of more than two bits is desired, which makes it a speed limiting factor for many high speed applications.

Different ULV NP domino logical gates implemented in the previous chapters operate at ultra low supply voltages while offering excellent speed performance. In this chapter, ULV NP domino carry gates are implemented exploiting the same logic style which enhance the speed performance when the carry signal propagates through all the full adders in the worst case scenario[30].

The logic function for the carry gate C_{out} is shown in the following equation:

$$C_{out} = A \cdot B + C_{in} \cdot (A + B) \quad (6.1)$$

Equation 6.1 states that C_{out} provides an AND function for the adding bits A and B as far as C_{in} is low. When C_{out} becomes high, C_{out} provides an OR function for the input bits A and B .

6.1 Ultra-Low-Voltage and High Speed NP domino Carry circuit

One common way to implement the Carry gate is by combining NAND and NOR gates. A control signal C_{in} should be included in addition which ascertains whether the output node $\overline{C_{out}}$ provides either NAND or NOR function for the input bits A and B .

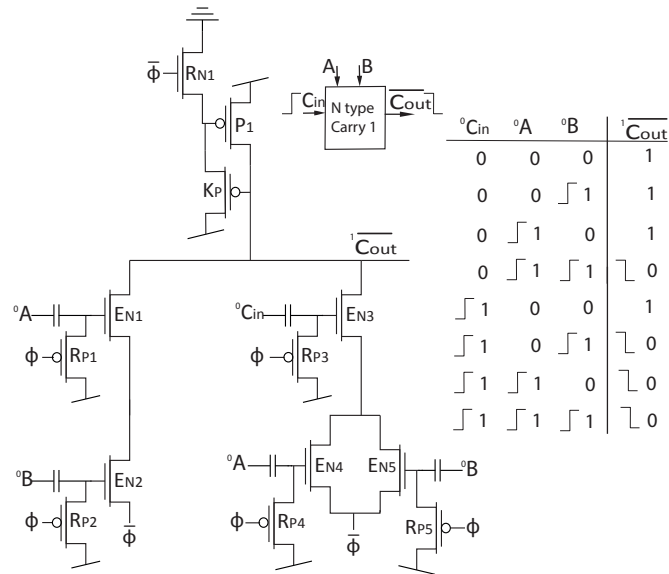


Figure 6.2: N type ULV domino Carry Gate (Carry 1a).

An N type ULV domino Carry gate is implemented in Figure 6.2. The PUN resembles the PUN of all other N type ULV domino logic gates which are implemented so far. In the PDN, the PDNs of ULV N type NAND and NOR gates proposed in the previous chapter are connected in parallel. An extra input C_{in} is serially connected with the PDN of ULV NOR gate. The PDN of the proposed N type ULV domino Carry gate resembles PDN of conventional CMOS Carry gate implemented in [17] to some extent.

The output node $\overline{C_{out}}$ precharges to V_{DD} in the precharge phase. In the evaluation phase, $\overline{C_{out}}$ discharges to GND depending upon the input transitions at the floating gates of the evaluation transistors. If A and

B switches from 0 to 1 prior to the C_{in} signal, both serially connected evaluation transistors E_{N1} and E_{N2} turn on and makes a direct path from $\overline{C_{out}}$ to GND . This resembles the working behavior of a NAND gate.

When C_{in} switches from 0 to 1 in the evaluation phase, the evaluation transistor E_{N3} turns on. Only one of the two inputs A or B needs a positive transition to conduct a path from $\overline{C_{out}}$ to GND . This resembles the working behavior of a NOR gate for the input bits A and B . The proposed ULV P type domino inverter should be connected at the output node $\overline{C_{out}}$ to obtain C_{out} signal.

The graphs obtained in Figure 6.3 demonstrates the simulation results for the proposed N type ULV domino Carry gate. In Figure 6.3a, C_{in} bit is low which let the circuit operates as a half adder. The output node $\overline{C_{out}}$ operates as an NAND gate for the input bits A and B . The propagation delay is 118ps between the input and the output signal. The simulated case in not a worst case as C_{in} is low. Thus the full adder is not operating in the propagation mode.

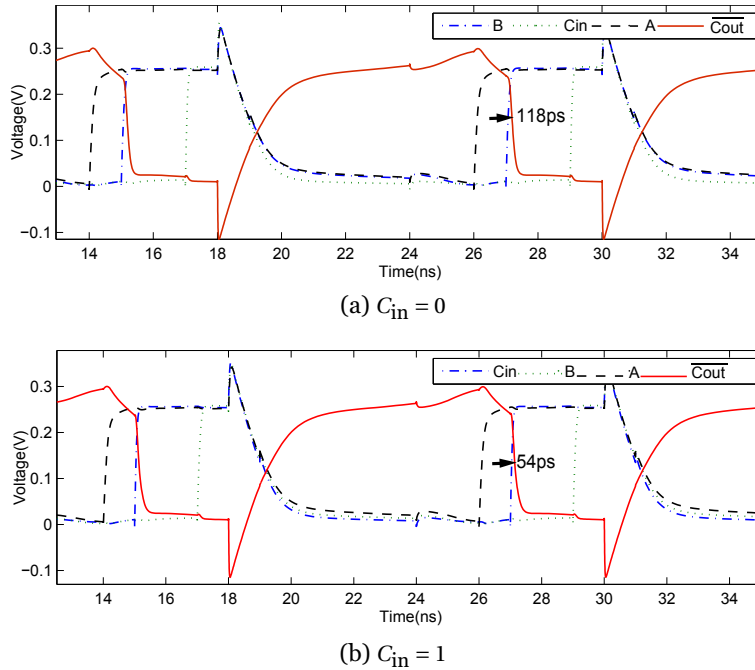


Figure 6.3: Simulation results for N type ULV domino Carry gate.

Figure 6.3b represents the simulation results for the proposed N type ULV domino Carry gate when the full adder operates in the propagation mode. Input signals $A \neq B$ and C_{in} is high which leads to a worst case scenario for the full adder. As far as the C_{in} is high, only one of the two inputs A or B needs to be high to conduct a path from the output node $\overline{C_{out}}$ to GND . Thus the Carry gate offers an NOR function for the input bits A and B . Simulation results demonstrates that the propagation delay is only 54ps between input and output signals.

Circuit implemented in Figure 6.4 represents an ULV domino P type Carry gate where the output node $\overline{C_{out}}$ precharges to 0 in the precharge phase. The proposed P type Carry gate is designed by parallel connecting

the PUNs of P type ULV domino NAND and NOR gates implemented in the previous chapter. The evaluation transistor E_{P3} determines whether the Carry gate should perform as NAND or NOR gate for the input signals A and B . PUN of proposed P type ULV domino Carry gate resembles the PUN of the conventional Carry gate implemented in [17]. The working principle for the proposed P type domino Carry gate is identical to the N type ULV domino Carry gate which is described in the above paragraphs. However the precharged level is opposite, requiring the monotonically falling transitions at the floating gate terminals of the pMOS evaluation transistors.

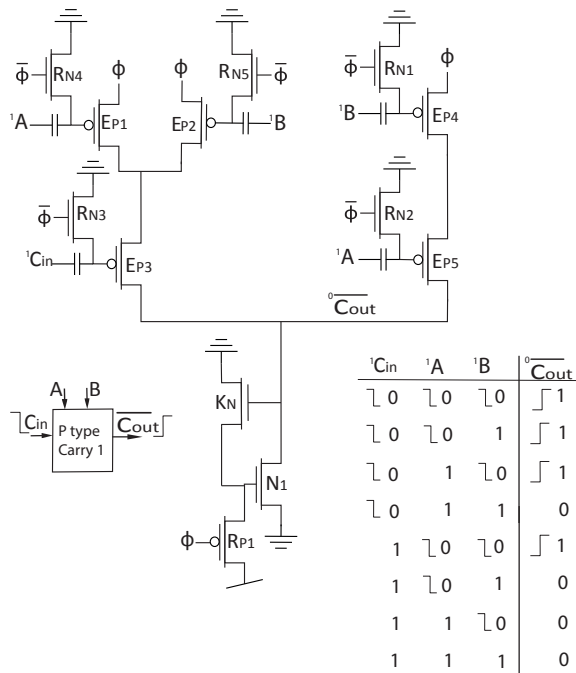


Figure 6.4: P type ULV domino Carry Gate (Carry 1b).

The simulation results plotted in Figure 6.5 represents the speed performance for the proposed P type ULV domino Carry gate. The output node $\overline{C_{out}}$ precharges to 0 in both subgraphs in the precharge phase, and pulls towards 1 in the evaluation phase depending upon the transitions at the input nodes. Subgraph in Figure 6.5a represents the best case scenario for the Carry gate as $\overline{C_{out}}$ pulls to 1 because of the input signals A and B , independent for the carry input signal C_{in} . The simulated propagation delay is 225ps between the input and the output node.

Subgraph in Figure 6.5b represents the simulation results for the proposed P type ULV domino Carry gate for the worst case scenario. A negative transition arrives input node A prior to the C_{in} bit while a negative transition arrive at C_{in} node prior to other input node B . The simulated worst case propagation delay is only 153ps.

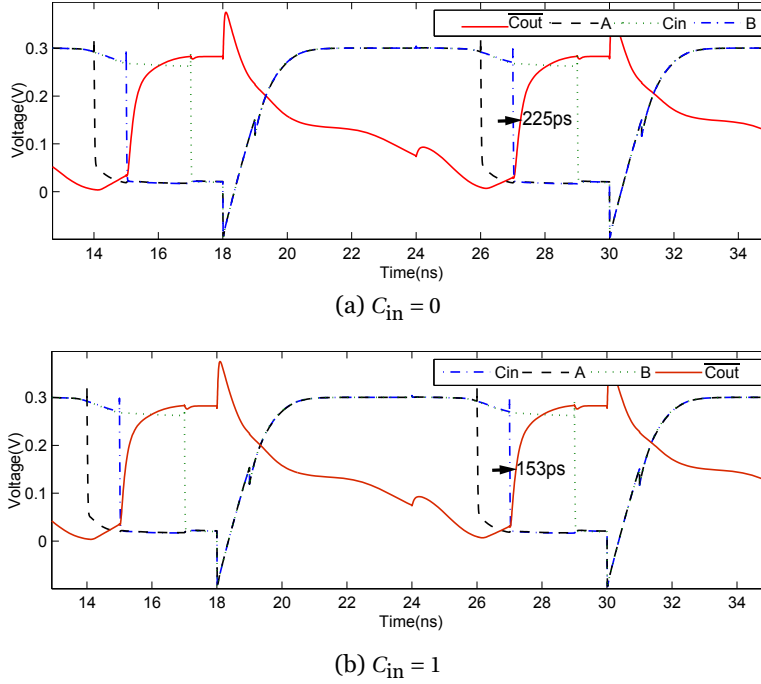


Figure 6.5: Simulation results for P type ULV domino Carry gate.

6.2 ULV NP domino Carry gates utilizing Pass Transistor Logic

ULV NP domino Carry gates proposed in the previous section resembles to the conventional CMOS Carry gate[17] to a certain extent with the implementation of serially connected evaluation transistors in the PDN and PUN for N and P type ULV domino Carry gates respectively. This may degrade the speed performance of the circuit and occupies more area on the chip. These drawbacks can overcome by exploiting pass transistor logic (PTL). ULV domino NAND and NOR gates are implemented in the previous chapter using PTL.

ULV NP domino Carry gates exploiting PTL are proposed in Figure 6.6, where all the evaluation transistors labeled E operate as pass transistors with an increased current level by using floating capacitance at the gate terminals.

Figure 6.6a shows N type ULV domino Carry gate with PTL where the output node $\overline{C_{out}}$ precharges to 1 in the precharge phase. As far as C_{in} is low, $\overline{C_{out}}$ only switches from 1 to 0 when input signal A switches from 0 to 1 and the other input signal \overline{B} switches from 1 to 0 in the evaluation phase.

When C_{in} bit becomes high, only one of the two parallel connected evaluation pass transistors E_{N2} or E_{N3} needs to switch on to discharge the output node $\overline{C_{out}}$ to GND . This implies that E_{N2} or E_{N3} acts as pass transistor for input $\overline{C_{in}}$ when $\overline{C_{in}}$ switches from 1 to 0 and one of the two inputs A or B switches from 0 to 1. $\overline{C_{in}}$ only requires to pass through a single evaluation transistor E_{N2} or E_{N3} to reach to the output node in the worst case scenario.

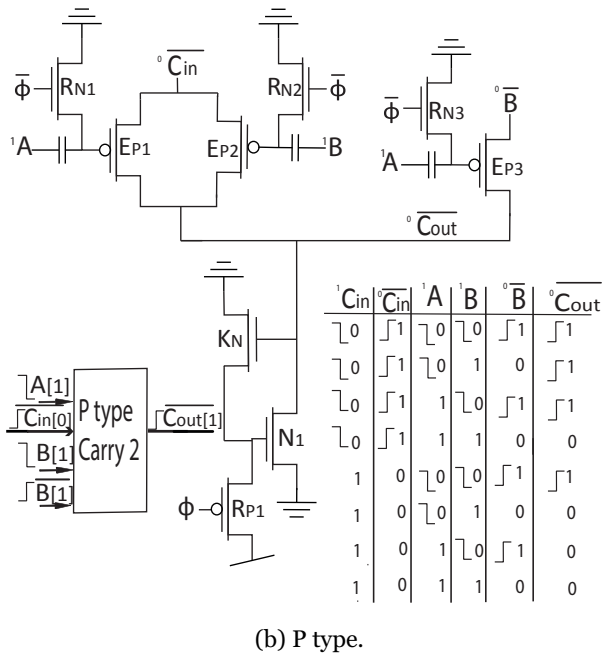
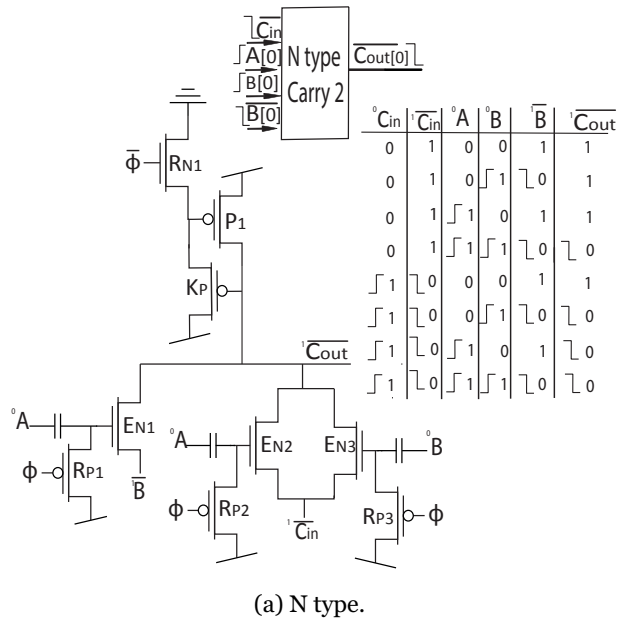
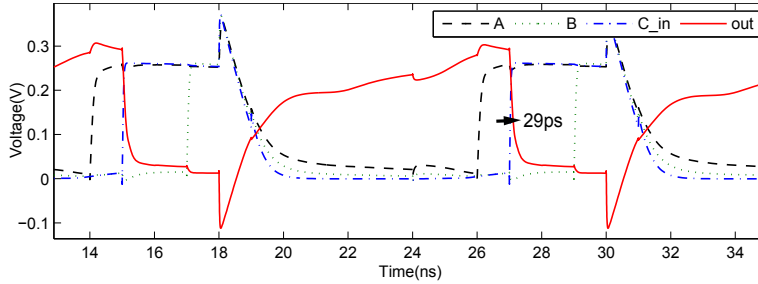


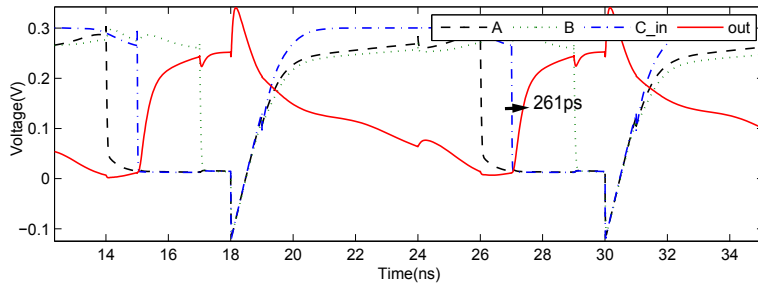
Figure 6.6: ULV domino Carry Gates using PTL (Carry 2).

Graphs plotted in Figure 6.7 demonstrates the speed performance for the proposed ULV NP domino Carry gates implemented in Figure 6.6. The worst case scenario is assumed for both circuits where input signal A arrives prior to carry input signal \bar{C}_{in} . The supgraph in Figure 6.7a and 6.7b corresponds to the N and P type ULV domino Carry gates respectively. The propagation delay for the P type Carry gate is 261ps which is higher than propagation delay of N type Carry gate (29ps) due to the mobility difference between pMOS and nMOS transistor. The strength of pMOS

evaluation transistors can be increased by lowering the threshold voltage of the transistor with various means mentioned in Chapter 3.



(a) N type Carry gate.



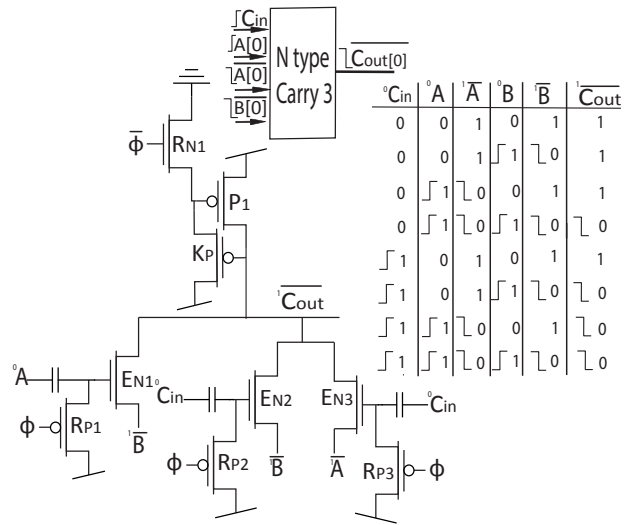
(b) P type Carry gate.

Figure 6.7: Simulation results for the worst case scenario of ULV NP domino Carry gates implemented in Figure 6.6.

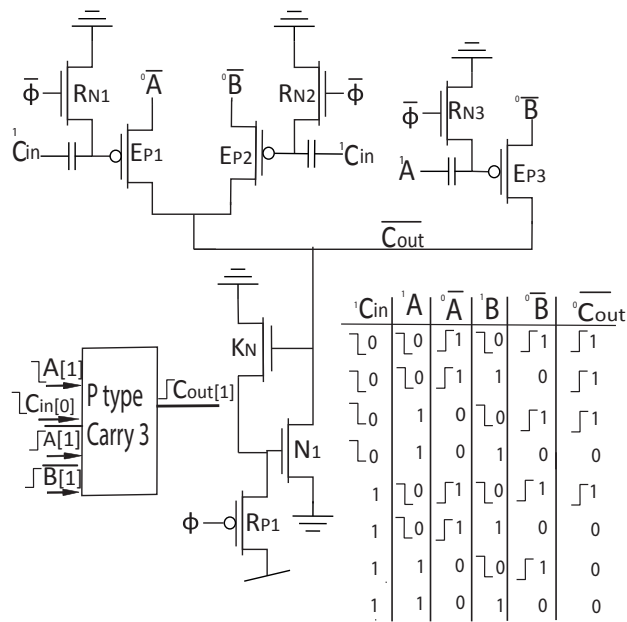
Another alternative solution of ULV domino NP Carry gate using PTL is implemented in Figure 6.8. The proposed solution of ULV NP domino Carry gates resembles the previous solution of ULV NP domino Carry gates with PTL implemented in Figure 6.6 to some extent as both proposed ULV NP domino Carry gates operate entirely the same way as far as the carry input signal C_{in} is low.

Taking into consideration the N type ULV domino Carry gate with PTL implemented in Figure 6.8a. When the carry input bit C_{in} switches from 0 to 1 in the evaluation phase, both parallel connected evaluation transistors E_{N2} and E_{N3} turn on and act as pass transistors for the input bits \bar{A} and \bar{B} . Under this instance, only one of the two inputs \bar{A} or \bar{B} requires to switch from 1 to 0 to pull the output node \bar{C}_{out} to 0.

The working principle for the proposed P type ULV domino Carry gate with PTL implemented in Figure 6.8b is identical to the N type ULV domino Carry gate described in the above two paragraphs. However the precharged level is opposite, requiring opposite transitions at the floating gate and source terminals for the pMOS evaluation transistors labeled E_p .



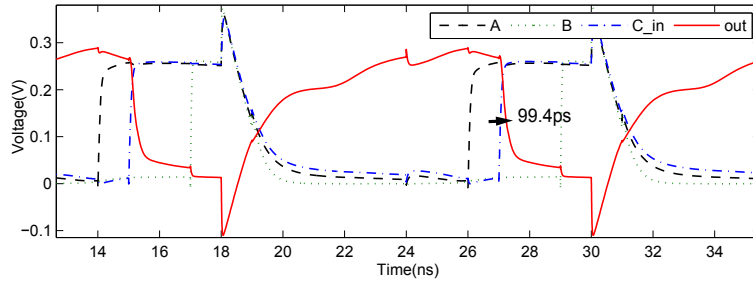
(a) N type.



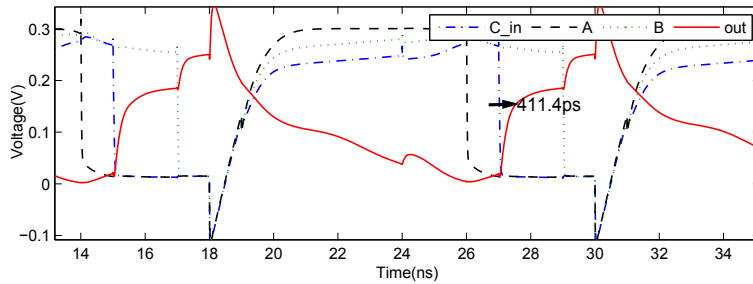
(b) P type.

Figure 6.8: ULV domino Carry Gates using PTL (Carry 3).

Graphs plotted in Figure 6.9 demonstrates the speed performance for the proposed ULV NP domino Carry gates implemented in Figure 6.8. The worst case scenario is considered for both N and P type ULV domino carry gates, where the input bits A and \bar{A} arrive prior to carry input bit C_{in} , while no transition arrives at the other input bit B and \bar{B} . The supgraph in Figure 6.9a and 6.9b corresponds to the N and P type ULV domino Carry gates respectively. The propagation delay of P type Carry gate is 411ps, while the propagation delay for the proposed N type ULV domino Carry gate is only 99.4ps.



(a) N type Carry gate.



(b) P type Carry gate.

Figure 6.9: Simulation results for the worst case scenario of ULV NP domino Carry gates implemented in Figure 6.8.

6.3 NP domino Carry gates Performance

In this section, different performance parameters for the proposed ULV NP domino Carry gates implemented in this chapter are compared with the conventional CMOS carry gate[17] at different ultra low supply voltages. Table 6.1 demonstrates the speed performance, together with the power consumption and other figure of merits (PDP and EDP) in order to optimize the *Minimum Energy Point* MEP for the proposed ULV domino Carry gates comparable with conventional CMOS carry gate. The table also represents the speed, PDP and EDP performance relative to the conventional Carry gate in %.

The power consumed by the clock drivers are not included and must be taken into consideration for each specific application. Besides this, the table also presents the operating limits for the clock frequency which changes rapidly as the supply voltage varies. In Table 6.1, the style labeled N Carry and P Carry represents the proposed N and P type domino Carry gates respectively. *Avg* represents the average delay or power consumption between the specific N and P type ULV domino Carry gates.

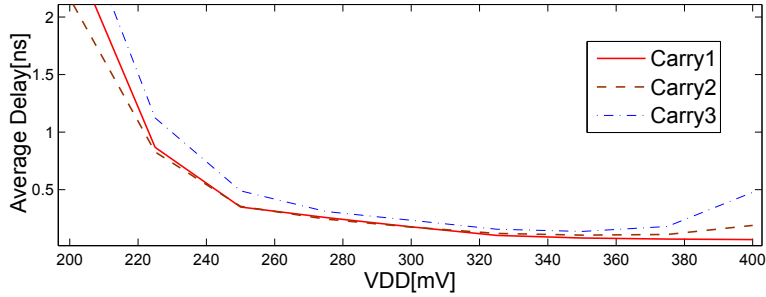
Style	Comment	100mV	150mV	200mV	250mV	300mV	350mV	400mV
CLK	f_{clk} (MHz)	0.83	2.5	8.3	16.67	66.67	83.3	125
Conventional Carry	Delay (ns)	328	101	25.4	10.4	2.56	1.55	0.782
	Power (nW)	0.008145	0.055	0.34	1.12	6.83	10.35	23
	PDP (10^{-18} J)	2.672	5.55	8.64	11.65	17.48	16.04	17.97
	EDP (10^{-27} J/s)	876.4	560.5	219.5	121	44.75	24.9	14.05
N Carry 1	Delay (ns)	53	18.74	2.49	0.318	0.162	0.05	0.022
P Carry 1	Delay (ns)	194	36.83	2.75	0.38	0.19	0.109	0.1086
Carry 1	Avg.Delay (ns)	123.5	27.785	2.62	0.349	0.176	0.0795	0.0653
	Relative delay (%)	37.65	27.52	10.31	3.36	6.88	5.11	8.36
	Avg.Power (nW)	0.0358	0.3078	1.907	7.55	41.1	100.8	265
	Avg.PDP (10^{-18} J)	4.423	8.552	4.996	2.635	7.234	8.014	17.305
	Relative PDP (%)	165	154	57.8	22.6	41.4	50	96.3
	Avg.EDP (10^{-27} J/s)	546.4	237.6	13.1	0.919	1.273	0.637	1.13
	Relative EDP (%)	62.35	42.4	5.97	0.76	2.84	2.56	8.04
	N Carry 2	Delay (ns)	141.5	25.38	3.07	0.4127	0.183	0.0725
P Carry 2	Delay (ns)	92.06	11.72	1.26	0.2976	0.166	0.1375	0.333
Carry 2	Avg.Delay (ns)	116.8	18.5	2.165	0.35	0.1745	0.105	0.189
	Relative delay (%)	35.61	18.32	8.52	3.36	6.82	6.77	24.18
	Avg.Power (nW)	0.01867	0.209	1.461	5.21	28.45	56.9	137
	Avg.PDP (10^{-18} J)	2.181	3.86	3.16	1.823	4.96	5.97	25.9
	Relative PDP (%)	81.6	69.55	36.57	15.65	28.37	37.22	144.13
	Avg.EDP (10^{-27} J/s)	254.7	71.41	6.84	0.638	0.865	0.627	4.897
	Relative EDP (%)	29.06	12.74	3.116	0.527	1.93	2.518	34.85
	N Carry 3	Delay (ns)	141.5	22.5	3.35	0.475	0.22	0.092
P Carry 3	Delay (ns)	265.7	31.1	2.75	0.504	0.248	0.182	0.883
Carry 3	Avg.Delay (ns)	203.6	26.8	3.05	0.489	0.234	0.137	0.477
	Relative delay (%)	62.07	26.53	12	4.7	9.14	8.84	61
	Avg.Power (nW)	0.01948	0.245	1.572	5.47	30.75	71.15	176.5
	Avg.PDP (10^{-18} J)	3.96	6.58	4.79	2.68	7.19	9.747	84.235
	Relative PDP (%)	148.4	117.35	55.1	23.01	41.15	60.57	468
	Avg.EDP (10^{-27} J/s)	807.5	176.4	14.63	1.312	1.684	1.335	40.2
	Relative EDP (%)	92.1	31.14	6.62	1.08	3.76	5.34	286

Table 6.1: Performance of ULV domino Carry gates compared to conventional CMOS Carry gate at different supply voltages.

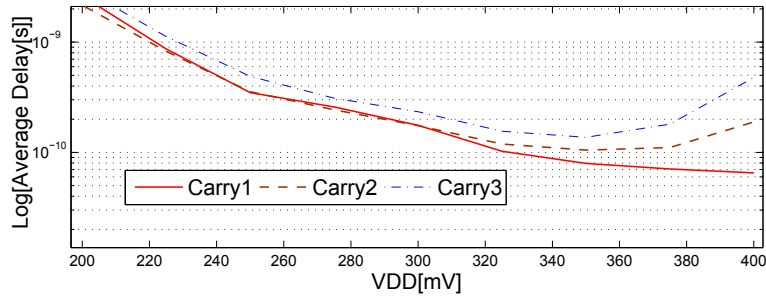
The average propagation delay between N and P type Carry gates for the proposed ULV domino logic style is shown in Figure 6.10. As concluded from the subgraph in Figure 6.10a, the propagation delay is in the range of ns for the supply voltages under 225mV and decreases rapidly as the supply voltage increases. Below 300mV, the propagation delay is only in the range of tens of ps. The logarithmic scale for the propagation delay in Figure 6.10b concludes that Carry 1 and Carry 2 ULV domino gates contribute almost equal propagation delay when the supply voltage varies between 220mV and 320mV. Below 220mV, Carry 2 provides minimum propagation delay. On the other hand, Carry 1 gives minimum propagation delay when the supply voltage exceeds over 320mV.

Carry 3 is the slowest and less preferable in high speed applications due to low noise margin, as both parallel connected evaluation transistors E_{N2} or E_{N3} turn on in the worst case scenario, while only one of the two inputs \overline{A} or \overline{B} switches from 1 to 0. Thus both \overline{A} and \overline{B} simultaneously contends

at the output node, which makes the output transition slower and degrades the robustness performance. However, it offers a more efficient solution in terms of area and power consumption as compared to Carry 1 ULV domino gate.



(a) Average Delay in ns.



(b) Average Delay with logarithmic scale.

Figure 6.10: Average Delay for the proposed ULV NP domino Carry gates for different supply voltages.

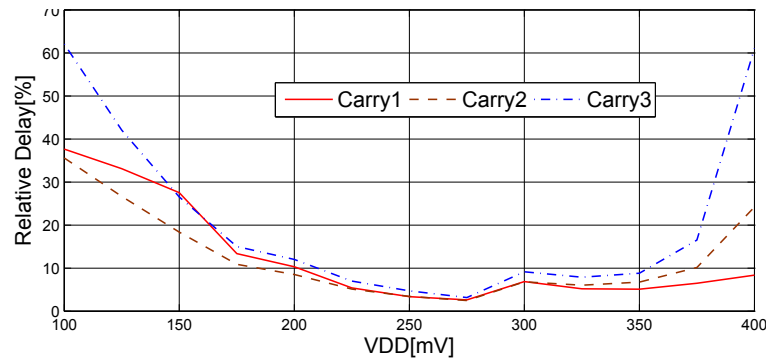


Figure 6.11: Delay of proposed ULV domino carry gates relative to conventional CMOS carry gate for different supply voltages.

The average delay between N and P type Carry gates for the proposed ULV domino logic style is compared with the conventional CMOS Carry gate in Figure 6.11. The delay is less than 20% for all the proposed ULV domino Carry gates relative to conventional Carry gate when the supply voltage varies between 175mV and 375mV. The overall best relative delay is achieved by Carry 2 ULV domino Carry gate with PTL. The reason

is because the input carry bit $\overline{C_{in}}$ only needs to propagate through a single evaluation transistor to reach the output node. Compared to the conventional Carry gate, the least average relative delay is achieved at the supply voltage of 275mV where Carry 2 ULV domino gate only utilizes a delay of 2.48%.

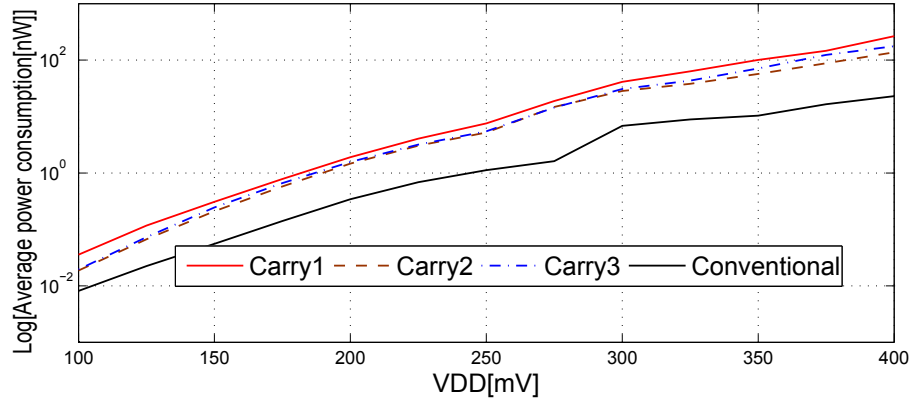


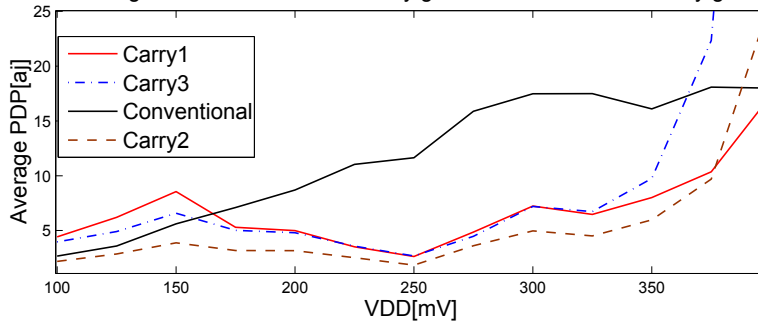
Figure 6.12: Average power consumption per ULV domino Carry gate compared to conventional CMOS carry gate.

The average power consumption per ULV domino Carry gate is compared with the conventional Carry gate in Figure 6.12. The total power consumption per gate increases with the supply voltage. As expected, the power consumption for the ULV domino Carry gates exceeds the power consumption for the conventional Carry gate, giving the advantage of superb speed performance. As shown in Figure 6.12, ULV domino Carry gates with PTL contributes minimum power consumption than other proposed ULV NP domino Carry gate as the total number of evaluation transistors reduces from 5 to 3 by using PTL.

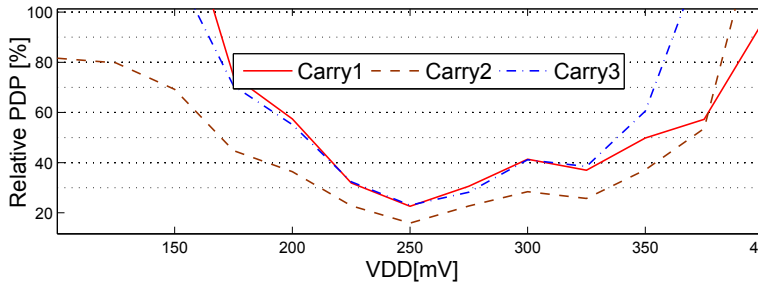
The average energy consumed by the proposed ULV domino Carry gates compared with conventional CMOS carry gate at different supply voltages is shown in Figure 6.13. The subgraph presented in Figure 6.13a shows the energy consumption in terms of *joule* while the subgraph in Figure 6.14b shows the average energy of the ULV domino Carry gates relative to the conventional CMOS Carry gate. The PDP for the proposed ULV Carry gates is lower than the conventional Carry gate for the supply voltage between 175mV and 350mV. This is mainly caused due to the superb speed performance for the proposed ULV domino Carry gates relative to the conventional Carry gate.

Comparing the graphs in Figure 6.11 and 6.13 conclude that minimum relative PDP corresponds to the maximum relative speed for the proposed ULV NP domino Carry gates. All the three domino Carry gates have the minimum relative PDP of lower than 25% at the supply voltage of 250mV, which makes it the Minimum Energy Point (MEP). Carry 2 is the most efficient solution as it only contributes 15.65% PDP relative to conventional Carry gate. For the supply voltage below 175mV, the relative PDP for Carry 1 and Carry 3 exceeds 100% while the relative PDP of Carry 2 is still below the PDP of conventional Carry gate. However, the relative PDP of Carry 2

becomes worse than Carry 1 as the supply voltage exceeds 375mV.



(a) Average Energy ($10^{-18}j$).

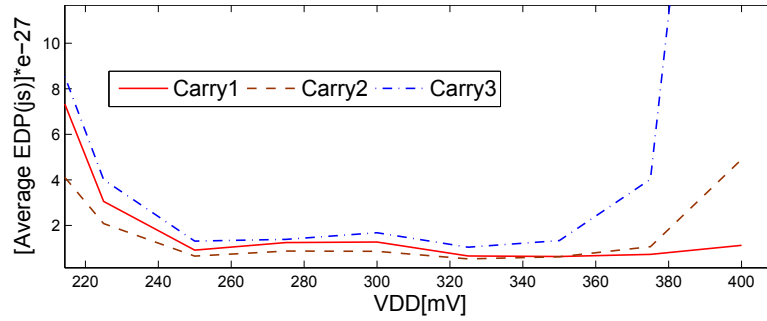


(b) Average relative energy (%).

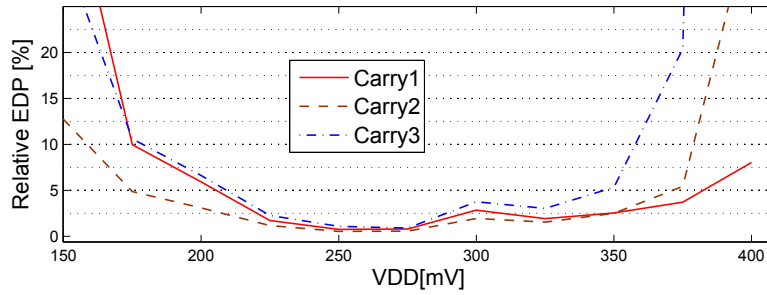
Figure 6.13: Average energy of ULV domino carry gates relative to the Conventional Carry gate at different supply voltages.

The Energy Delay Product EDP for the proposed ULV domino Carry gates for different supply voltages is shown in Figure 6.14. The subgraph in Figure 6.14a shows the average EDP in terms of js while the subgraph in Figure 6.14b shows the EDP relative to conventional Carry gate. The relative EDP for all the proposed ULV domino Carry gates is less than 30% for the supply voltage between 175mV and 375mV which directly corresponds to the same supply voltage range where the PDP is minimum as shown in Figure 6.13.

At Minimum Energy point (250mV), the EDP for all the proposed ULV domino Carry gates is lower than 1.5% relative to the conventional Carry gate. However, Carry 2 is characterized by least relative EDP with a value closer to 0.527% at 275mV. The relative EDP of Carry 2 is far better than Carry 1 and Carry 3 when the supply voltage is below 175mV, but becomes worse than Carry 1 when the supply voltage exceeds 375mV.



(a) Average EDP (10^{-27} js).



(b) Average relative EDP of ULV domino Carry gates.

Figure 6.14: Average Energy Delay Product of ULV domino Carry gates compared to conventional Carry gate at different supply voltages.

6.3.1 MonteCarlo Simulations

In this section, the performance of proposed ULV NP domino Carry gates are presented at different supply voltages with 100 montecarlo simulations including process and mismatch variations at each supply voltage. The performance for ULV NP domino Carry gates is not compared with the conventional CMOS Carry gate with the montecarlo simulations as the conventional CMOS carry gate is unable to operate at low supply voltages and high operating frequencies.

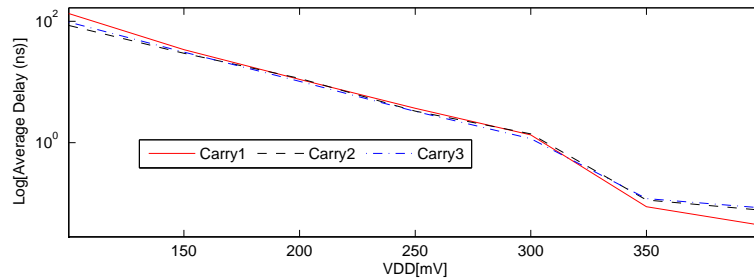


Figure 6.15: Average Delay per ULV domino Carry gate with 100 montecarlo simulations.

The graph in Figure 6.15 represents the average delay of 100 montecarlo simulations at each of the supply voltages in the range of 100mV to 400mV. The average delay is high for low supply voltages and decreases as the

supply voltage increases.

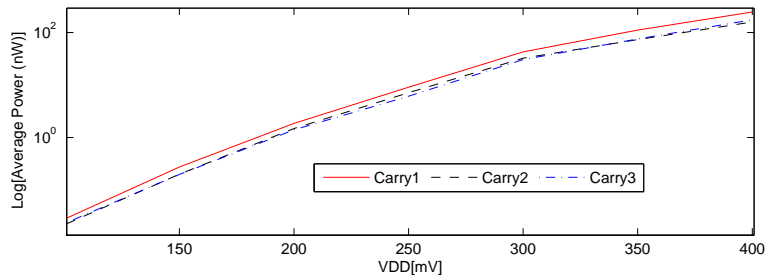


Figure 6.16: Average Power consumption per ULV domino Carry gate with 100 montecarlo simulations.

The graph in Figure 6.16 represents the average power consumption with 100 montecarlo simulations for the proposed ULV NP domino Carry gates. As expected, Carry 1 consumes slightly more power than other two proposed ULV Carry gates. The power consumption for each of the ULV domino Carry gates increases as the supply voltage increases.

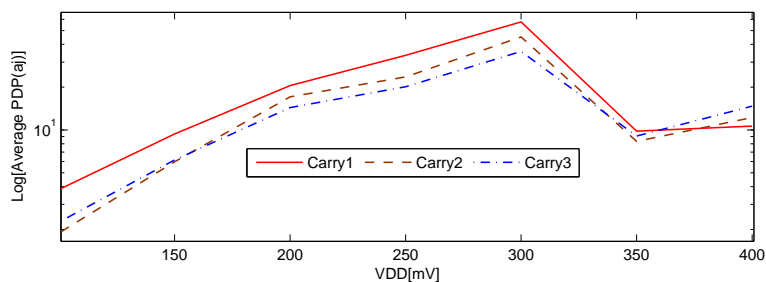


Figure 6.17: Average PDP per ULV domino Carry gate with 100 montecarlo simulations.

Average PDP of 100 montecarlo simulations at each of the supply voltage for the proposed ULV NP domino Carry gates is shown in Figure 6.17. Carry 1 offers worst average PDP performance than the other proposed Carry gates at the supply voltages below 300mV, however as the supply voltage increases, the significant improvement is achieved in PDP performance for Carry 1 domino gate.

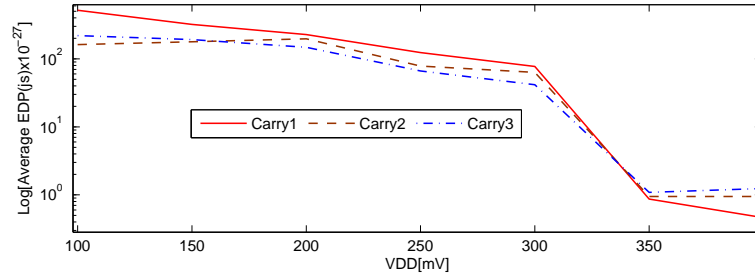


Figure 6.18: Average EDP per ULV domino Carry gate with 100 montecarlo simulations.

Average EDP of 100 montecarlo simulations for the proposed ULV NP domino Carry gates is presented in Figure 6.18. Better EDP performance is achieved for all the proposed ULV NP domino Carry gates at higher supply voltages due to significantly reduced propagation delay.

6.3.2 Summary

Table 6.2 summarizes the speed, PDP and EDP performance for the proposed ULV NP domino Carry gates relative to conventional Carry gate at Minimum Energy Point. Carry 1 and Carry 2 have the same relative delay of 3.36% thus both solutions are efficient for ultra low voltage and high speed applications. However for low power applications, Carry 2 is the most efficient solution as it consumes less power than the other two ULV domino Carry gates and results in better PDP and EDP. Carry 3 is the slowest and may not be the best solution for high speed applications, however it offers a more efficient solution than Carry 1 in terms of area and power.

	CARRY 1	CARRY 2	CARRY 3
Relative Delay(%)	3.36	3.36	4.7
Relative PDP(%)	22.6	15.65	23.01
Relative EDP(%)	0.76	0.527	1.08

Table 6.2: The delay, PDP and EDP of ULV domino carry gates at Minimum Energy Point (250mV) relative to conventional CMOS carry gate.

Chapter 7

Different configurations of 32-bit Carry chain by exploiting ULV NP domino logic style

All the ULV domino Carry gates implemented in the previous Chapter are one-bit Carry gates[31][30], as they add only 2 single bits. If the arithmetic operation of more than 2 bit is desired, every single one-bit Carry gate should be cascaded in a serial chain. In this chapter, we exploit various ULV NP domino 32-bit Carry chains using NP domino logic style.

7.1 32-bit carry chain using NP domino Carry 1 gates

N and P type ULV domino Carry 1 gates implemented in previous chapter in Figure 6.2 (on page 40) and 6.4 (on page 42) respectively are serially cascaded in a chain of n-bits in Figure 7.1. Every other Carry gate is P type where all the input bits have monotonically falling transitions in the evaluation phase.

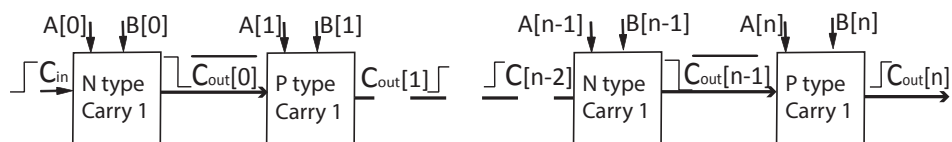


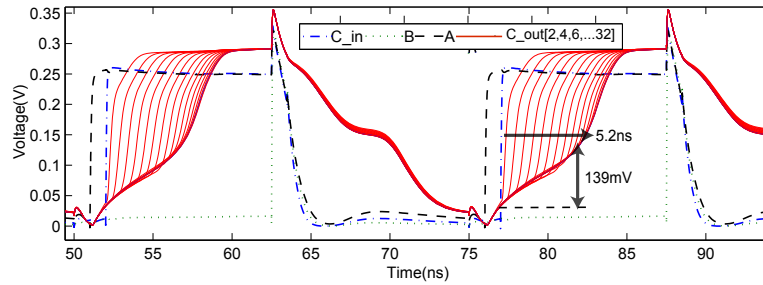
Figure 7.1: NP domino n-bit carry chain 1.

Table 7.1 states the working principle for NP domino Carry gates in a chain. \uparrow and \downarrow symbols indicate the positive and negative transition in the evaluation phase. Output $\overline{C_{n+1}}$ from an N type is applied further to a P type Carry gate. In the same way, $\overline{C_{n+2}}$ is applied further to the next N type Carry gate. In this way, the carry signal propagates through the NP domino chain.

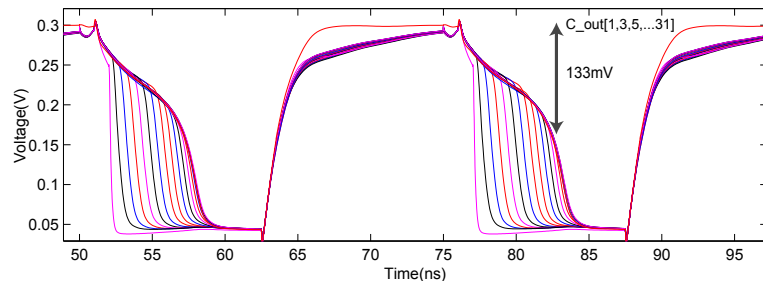
Inputs N type			Output N type		Inputs P type			Output P type	
C_n	A_n	B_n	$\overline{C_{n+1}}$	C_{n+1}	$\overline{C_{n+1}}$	A_{n+1}	B_{n+1}	$\overline{C_{n+2}}$	C_{n+2}
0	0	0	1	0	1	0↓	0↓	1↑	0↓
0	0	1↑	1	0	1	0↓	1	0	1
0	1↑	0	1	0	1	1	0↓	0	1
0	1↑	1↑	0↓	1↑	0↓	1	1	0	1
1↑	0	0	1	0	1	0↓	0↓	1↑	0↓
1↑	0	1↑	0↓	1↑	0↓	0↓	1	1↑	0↓
1↑	1↑	0	0↓	1↑	0↓	1	0↓	1↑	0↓
1↑	1↑	1↑	0↓	1↑	0↓	1	1	0	1

Table 7.1: The working principle for the NP Carry gates in a Domino chain.

Simulation results shown in Figure 7.2 demonstrates a 32-bit NP domino carry chain implemented in Figure 7.1. Simulation results are considered for the worst case scenario, where all the full adders operate in the propagation mode. One of the two input signals A or B arrive prior to the C_{in} signal, however other input signal assume to retain the precharged value. All the input signals arrive in parallel for every NP domino Carry gate, assuming that all the input signals originate from a register or flip flop. All the transistors except the evaluation transistors labeled N and P assumed to be minimum sized during the simulation response. The bulks of N and P transistors are floating in order to lower the threshold voltage of the transistors by increasing the strength.



(a) Output nodes from P type Carry gates and the input signals.



(b) Output nodes from N type Carry gates.

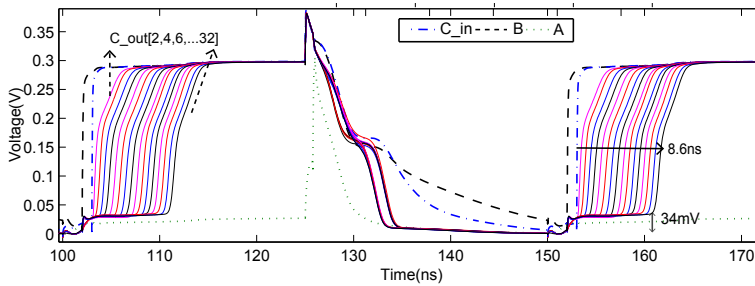
Figure 7.2: Simulation result of 32-bit carry chain 1.

The subgraph in Figure 7.2a shows the input signal to the first N type

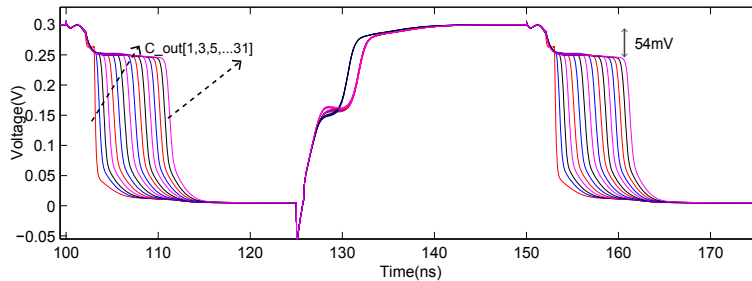
Carry gate and the output signals from the P type Carry gates, however plots in subgraph 7.2b demonstrates output signals from N type carry gates. The total propagation delay is $5.2ns$ from the C_{in} bit switches to the last C_{out} bit response in the chain. However last carry bits are obstructed.

The reason for the obstruction is clarified from the plots. During the evaluation phase, the output nodes from the last Carry gates in the chain drift to $139mV$ and $167mV$ for the P and N type Carry gates respectively prior to the correct input bits arrive. This turns on the evaluation transistors labeled E_{N3} and E_{P3} in the N and P type UIV domino Carry 1 gates respectively, which results in false rising and falling transitions at the output nodes of the later Carry 1 gates in the chain. The power signals ϕ and $\bar{\phi}$ slowly leaks toward the output nodes through the PUN and PDN for N and P type respectively, meanwhile the floating output nodes still wait for the correct input transitions. As all the output nodes are serially cascaded, so the leakage voltage to a certain extent on the output nodes able to turn on the evaluation transistor in the following Carry gate which further gives false transitions on all the following NP domino Carry gates. In the simulation results shown in Figure 7.2, this false transition occurs after 20-bit in the 32-bit carry chain.

To overcome the leakage problem discussed in the above paragraph, the evaluation transistors labeled N and P should make stronger enough to hold the precharged value until the correct input transitions occur. The strength of the transistor is increased by lowering the threshold voltage of the transistor.



(a) Output nodes from P type Carry gates and the input signals.



(b) Output nodes from N type Carry gates.

Figure 7.3: Simulation result of 32-bit carry chain 1 with *FBB* on N and P transistors.

The strength of the evaluation transistors labeled P is increased by

increasing the transistor length $L \geq 3 \times L_{\min}$. Furthermore, *FBB* is applied at the bulk terminals of P transistors by connecting the bulks to *GND*. To make the transistor more stronger, the width W of the pMOS is increased $1.5 \times W_{\min}$ as increasing the length more than $3 \times L_{\min}$ is not anymore an effective knob.

On the other hand, the evaluation transistor N should make stronger as well to retain the precharged value. As the nMOS transistor has a much higher mobility than the pMOS transistor, thus N transistor does not need to make as stronger as P. The strength of N transistor is increased by applying *FBB* on the bulk terminals by connecting bulks to V_{DD} .

The simulation results of ULV NP domino 32-bit carry chain by tuning the evaluation transistors N and P is shown in Figure 7.3. All the transistors except the evaluation transistors N and P are minimum sized low-threshold transistors.

The simulation results in Figure 7.3 conclude that the leakage problem is solved by increasing the strength of the specific transistors. The voltage deviation at the output nodes of P type carry gates is reduced from 139mV to 34mV. On the other hand, the voltage deviation at the output nodes of N type carry gates is reduced from 133mV to 54mV. However, the propagation delay is slightly increased from 5.2ns to 8.6ns in the worst case scenario. The simulated power consumption is only 667nW for this scenario. The delay and EDP relative to conventional CMOS 32-bit carry chain is only 2.68% and 8.11% respectively.

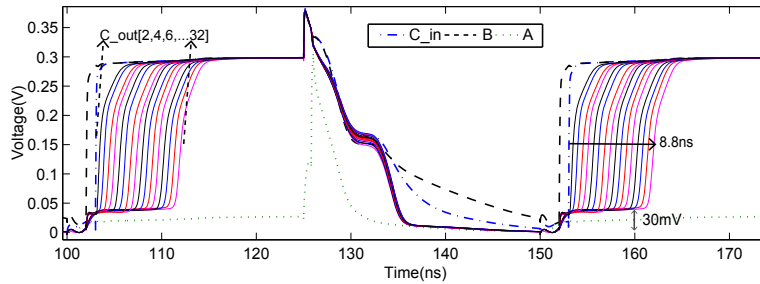
The simulation results conclude that the worst case speed scenario for a 32-bit carry chain is not probably the worst case power consumption scenario for the proposed ULV domino logic style. The proposed ULV domino 32-bit carry chain consumes a certain amount of power in the evaluation phase when the output nodes hold the precharged value and *Wait* for the correct transitions at the input nodes. The power consumption for the proposed 32-bit chain in the *Wait* mode is 687nW with an average deviation of 28mV from the rails at the output nodes.

7.1.1 A solution without Forward Body Biasing on nMOS transistor

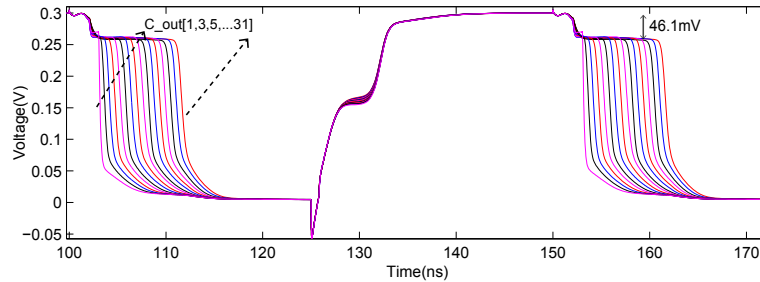
Applying Forward Body Biasing (FBB) scheme at the body of the nMOS transistors or keep the bulks floating can be a challenging task and increase the complexity during the layout stage in the *TSMC* process as the demand of implementing deep n-well is necessary in order to isolate the body of nMOS transistors. Assuming the N type ULV domino Carry 1 gate, all the nMOS recharge transistors labeled R_N and the keeper transistor labeled K_N are minimum sized low threshold transistors sharing the same P-substrate which is connected to *GND*. However the substrate of the evaluation transistor labeled N is connected to V_{DD} in order to increase the strength of the transistor. In this case, the substrate of the evaluation transistor N should be isolated; otherwise there will be short via substrate. To do this, we apply a deep n-well. The main disadvantage of implementing deep n-well is increment in the area.

To avoid the problems which can be faced during *FBB* of nMOS

transistors due to the implementation of deep n-well, the standard *RBB* technique has been used on the bulk terminal of evaluation transistor *N* by connecting the bulk terminal to *GND*. In order to retain the precharged value until the correct input transitions occur, the *N* transistor's sizing has been modified to increase the transistor strength. The transistor's length *L* is increased by $2 \times L_{\min}$ and the width *W* is increased by $2 \times W_{\min}$. Furthermore, the strength of *P* evaluation transistor is also increased by increasing *L* $3 \times L_{\min}$ and *W* $2 \times L_{\min}$ to retain the precharged value in a cascaded chain.



(a) Output nodes from *P* type Carry gates and the input signals.



(b) Output nodes from *N* type Carry gates.

Figure 7.4: Simulation result of 32-bit carry chain 1 without *FBB* on nMOS transistor *N*.

Figure 7.4 demonstrates the simulation results of 32-bit carry chain by applying *RBB* technique at the bulk terminals of evaluation transistor *N*. The propagation delay is slightly increased to 8.8ns, giving the advantage of better noise margin and probably less area consumption for nMOS transistor *N* during the layout stage as compared to the implementation of deep n-well. The noise margin is increased as the off-current I_{off} is reduced by connecting the substrate to *GND* for *N* transistor. The total power consumption of 32-bit carry chain in the worst case scenario is 705.5nW which is slightly increased compared to the previous solution as the dimensions of both *N* and *P* evaluation transistors are increased. The delay and EDP relative to conventional CMOS 32-bit carry chain is only 2.8% and 9.3% respectively.

The power consumption for the proposed 32-bit carry chain in the *Wait* mode is 685nW with an average deviation of 24mV from the rails at the output nodes.

7.1.2 32-bit carry chain utilizing Multi-threshold CMOS Technique (MTCMOS)

MTCMOS technique is employed to maintain both speed and power performance. Low threshold transistors $L\text{-thr}$ are used in speed critical paths while the leakage power is suppressed on the other paths by implementing high threshold transistors $H\text{-thr}$. The threshold voltage

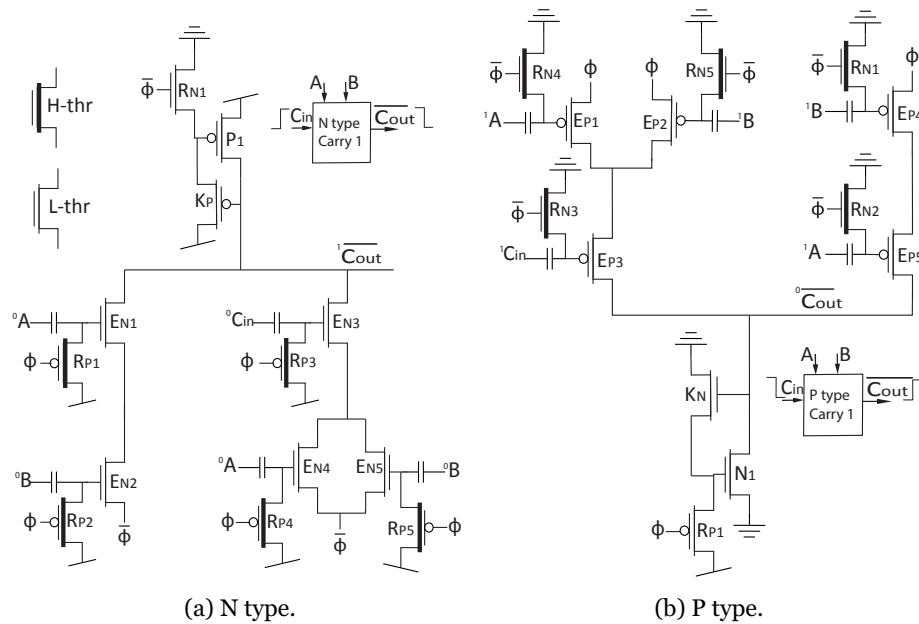
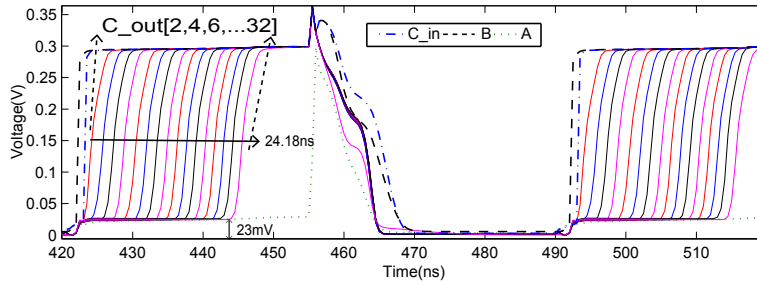


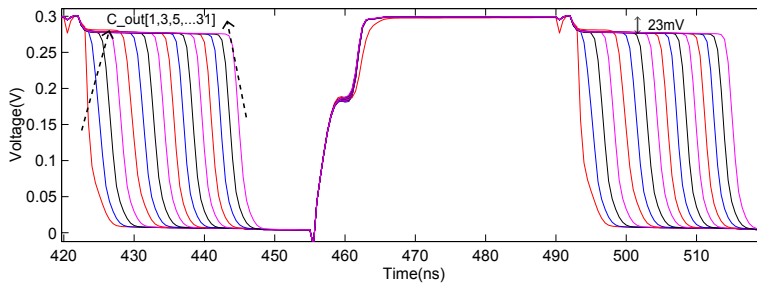
Figure 7.5: ULV domino Carry 1 Gates utilizing MTCMOS technology.

of the transistors for ULV NP domino Carry 1 gate is modified by applying MTCMOS technique. All the evaluation transistors labeled E , N and P are $L\text{-thr}$ transistors in order to enhance the speed performance and produce the correct transitions at the output nodes. All the keeper transistors labeled K are also minimum sized $L\text{-thr}$ transistors. The recharge transistors R_N for N type Carry gates and R_P for P type Carry gates are also minimum sized $L\text{-thr}$ transistors as shown in the schematic in Figure 7.5.

All the recharge transistors labeled R_P in N type ULV domino Carry 1 gate and R_N in P type ULV domino Carry 1 gate are minimum sized $H\text{-thr}$ transistors in order to suppress the leakage problem as shown in Figure 7.5.



(a) Output nodes from P type Carry gates and the input signals.



(b) Output nodes from N type Carry gates.

Figure 7.6: Simulation result of 32-bit carry chain 1 utilizing MTCMOS technique.

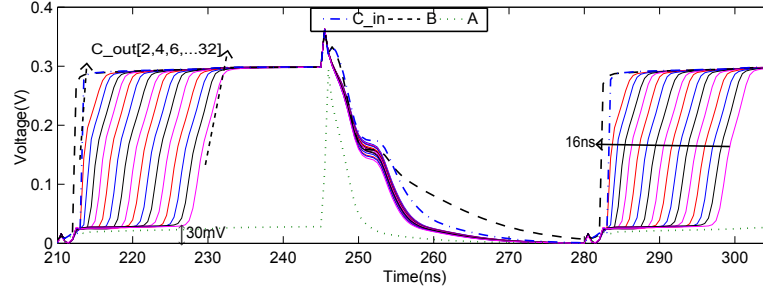
Figure 7.6 demonstrates the simulation results for the 32-bit carry chain 1 which is utilized by MTCMOS technology in order to reduce the power consumption. As the simulation results conclude, the propagation delay is increased to 24.18ns by implementing $H-thr$ recharge transistors. The floating output nodes of P and N type carry gates are pulled slightly towards 1 and 0 respectively before the carry input signal arrives, but the deviation is decreased compared to the previous simulation results. The greatest advantage is on the power consumption as expected. The 32-bit carry chain only consumes a power of 517nW in the worst case scenario, which is far lower than the previous simulation results. The delay and EDP relative to conventional CMOS 32-bit carry chain is 7.54% and 49% respectively.

The power consumption for the proposed 32-bit carry chain in the *Wait* mode is 655nW with an average deviation of 26mV from the rails at the output nodes.

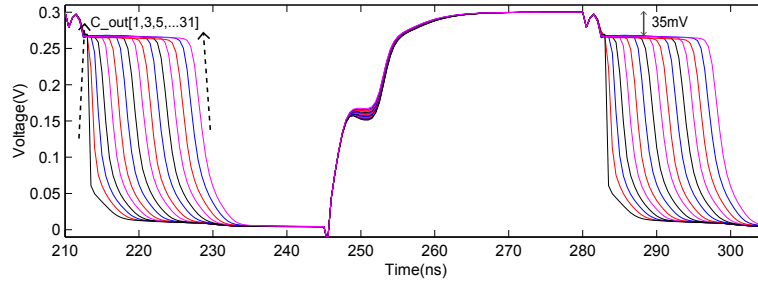
7.1.3 32-bit carry chain utilizing Variable-threshold CMOS Technique (VTCMOS)

Variable-threshold CMOS (VTCMOS) is another efficient method to reduce the leakage power of the circuits. The speed critical transistors can be biased by adopting VTCMOS technology. As mentioned in the previous sections, the evaluation transistors labeled N and P in ULV NP domino Carry 1 gate should be made stronger in order to retain the precharged value until the correct input transitions arrive. These transistors can be made stronger by lowering the threshold voltage by different means as mentioned earlier. One of the efficient node to lower the transistor

threshold voltage is the body biasing scheme by having either floating or *FBB* bulks. This lowers the transistor threshold voltage at the cost of high leakage power.



(a) Output nodes from P type Carry gates and the input signals.



(b) Output nodes from N type Carry gates.

Figure 7.7: Simulation result of 32-bit carry chain implemented in Circuit 7.1 utilizing VTCMOS technique.

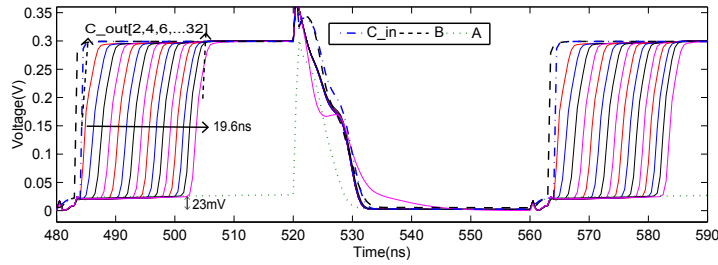
Using VTCMOS, the body voltage of the evaluation transistors labeled *N* is dynamically switched to V_{DD} and GND in the evaluation and precharge phase respectively. This lowers the threshold voltage of *N* transistor only in the speed critical evaluation phase, otherwise the bulk terminal is *RBB*. This can be achieved by connecting the bulk terminal to the clock signal ϕ . In the same way, VTCMOS technique is applied on the P type evaluation transistor by connecting the bulk terminal to clock signal $\bar{\phi}$.

The graphs presented in Figure 7.7 demonstrate the simulation results of a 32-bit carry chain in the propagation mode where all the domino Carry gates are enhanced by VTCMOS technology. The speed performance is improved compared to the previous simulation results using MTCMOS technology at the cost of reduction in noise margin before the transition occurs at the output nodes. Somehow the total propagation delay and power consumption is 16ns and 718nW respectively. Relative to the conventional 32-bit carry chain, the delay and EDP is only 4.99% and 30.24% respectively.

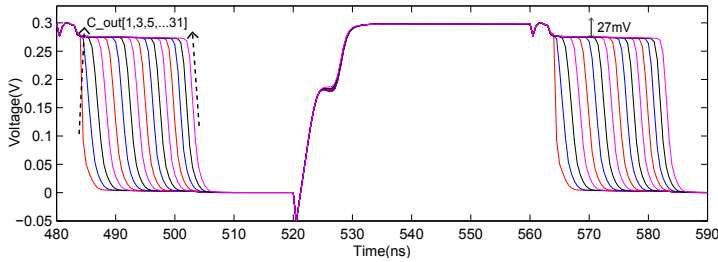
The power consumption for the proposed 32-bit carry chain in the *Wait* mode is 660.7nW with an average deviation of 20.5mV from the rails at the output nodes. The power consumption is increased in both the propagation and the *Wait* mode as compared to the simulation results obtained by utilizing MTCMOS technology.

7.1.4 VTCMOS and MTCMOS Technique

In this section, a hybrid solution of both MTCMOS and VTCMOS techniques is applied. MTCMOS technique is employed by implementing both $H-thr$ and $L-thr$ transistors. All the transistors are $L-thr$ except the recharge transistors labeled R_p in N type ULV domino Carry 1 gate and R_N in P type ULV domino Carry 1 gate which are $H-thr$ transistors. Meanwhile, VTCMOS technique is applied on the evaluation transistors labeled N and P by connecting the bulk terminals to ϕ and $\bar{\phi}$ respectively.



(a) Output nodes from P type Carry gates and the input signals.



(b) Output nodes from N type Carry gates.

Figure 7.8: Simulation result of 32-bit carry chain implemented in Circuit 7.1 utilizing both MTCMOS and VTCMOS techniques.

Graphs in Figure 7.8 represents the simulation results for the 32-bit ULV NP domino carry chain utilizing both combination of both MTCMOS and VTCMOS techniques. The speed performance for the hybrid style is better than only MTCMOS technique. However, the delay is slightly increased compared to VTCMOS technology. But the figure of merits are much better compared either to VTCMOS or MTCMOS technique. The total propagation delay and power consumption is 19.6ns and 410nW respectively. The proposed hybrid style consumes minimum amount power than all the previous simulation results. Relative to the conventional 32-bit carry chain, the delay and EDP is only 6.1% and 25.9% respectively.

The power consumption for the proposed 32-bit carry chain in the *Wait* mode is 652nW with an average deviation of 26.5mV from the rails at the output nodes. The proposed hybrid style consumes minimum power than all the previous implementations in both propagation mode and *Wait* mode.

7.2 32-bit carry chain using NP domino Carry 2 gates

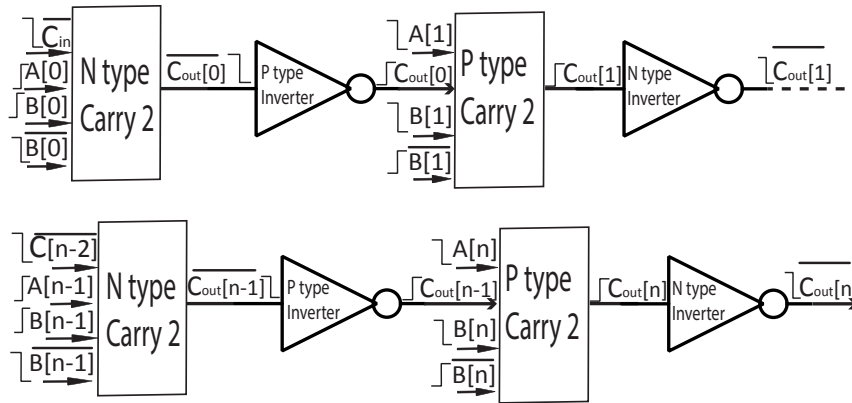
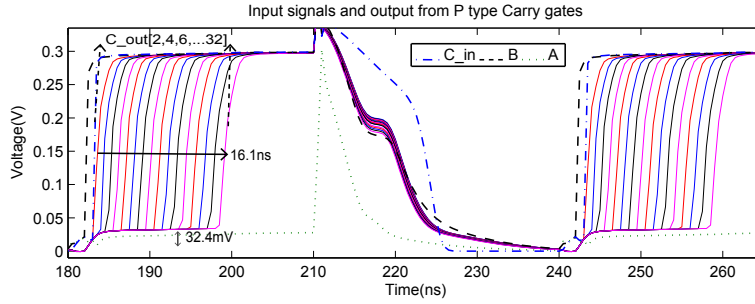


Figure 7.9: NP domino n-bit carry chain 2.

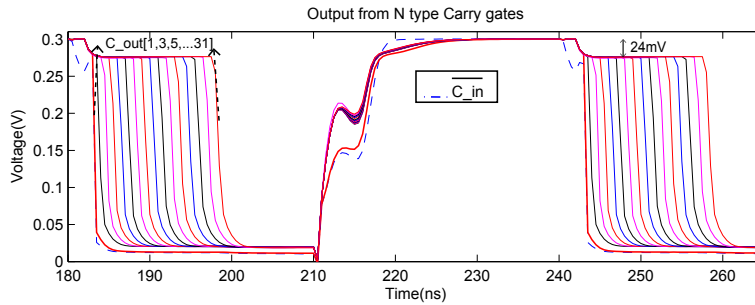
Schematic in Figure 7.9 represents an n-bit chain of NP domino Carry 2 gates which are implemented utilizing Pass Transistor Logic (PTL). The main difference from the previous n-bit carry chain (in Figure 7.9) is the $\downarrow B$ and $\downarrow C_{in}$ signals to the N type carry gate together with the other input bits $\uparrow A$ and $\uparrow B$. The \uparrow and \downarrow symbols represent the monotonically rising and falling transitions in the evaluation phase. This topology reduces the total number of evaluation transistors.

Although the proposed topology is very efficient in terms of speed, area and power as concluded from the simulation results obtained in the previous chapter. However, cascading the proposed NP domino Carry 2 gates is quite challenging as the necessity of connecting an ULV domino inverter is compulsory in order to obtain the required carry signal for the further carry gate in the chain. Considering the example of N type carry gate shown in Figure 7.9. A P type ULV domino inverter is connected at the output node of an N type ULV domino Carry 2 gate in order to obtain a monotonically rising carry signal for the further P type carry gate in the chain.

Simulation results shown in Graph 7.10 demonstrates the 32-bit carry chain shown in Figure 7.9. The carry chain is simulated with the worst case scenario, considering that B switches from 0 to 1 prior to carry input signal in the start of evaluation phase, while A holds the precharged value in the whole evaluation phase. The propagation delay is 16.1ns which shows the degradation in the speed performance compared to the first 2 simulation results (implemented in Figure 7.3 and 7.4) for the carry 1 chain implemented in Figure 7.1. This is due to the addition of extra ULV NP domino inverters at the output nodes of every ULV NP domino Carry 2 gate.



(a) Output nodes from P type Carry gates and the input signals.



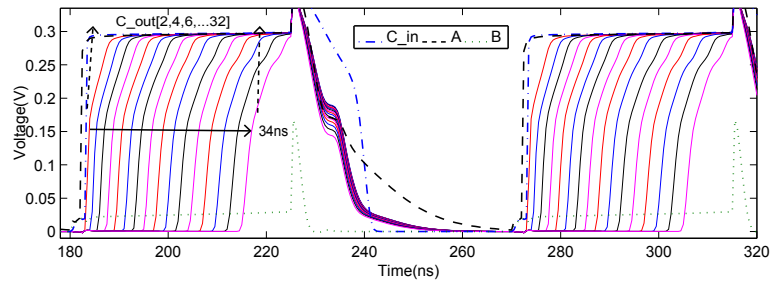
(b) Output nodes from N type Carry gates.

Figure 7.10: Simulation result of 32-bit carry chain implemented in Circuit 7.9 when only input bits B get transitions.

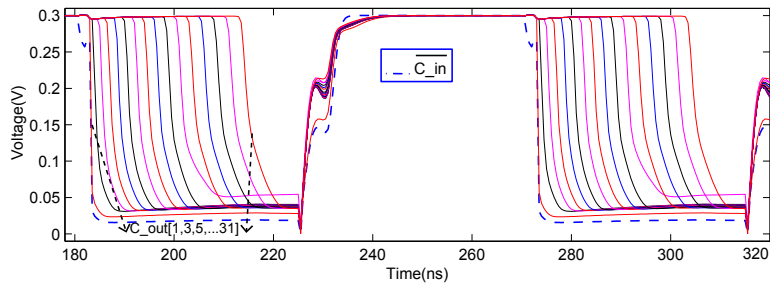
On the other hand, the presented simulation results offer an advantage in terms of robustness as the deviation is very close to rails, i.e. V_{DD} and GND before the transition occurs at the output node. This concludes that removing the serially connected evaluation transistors suppress the leakage problem at the output nodes. Although 32 extra NP domino inverters are added in the proposed chain, the power consumption is 1067nW which is still acceptable compared to previous simulation results obtained in Section 7.1. Relative to the conventional 32-bit carry chain, the delay and EDP is only 5.02% and 45.4% respectively.

Unlike the simulation results in the previous section, the propagation delay of the proposed carry chain varies enormously as input bits A get transitions instead of input bits B in the evaluation phase as shown in simulation results in Figure 7.11. This is due to the fact that both evaluation transistors, for example in an N type ULV domino 2 Carry gates, E_{N1} and E_{N2} turn on as A switches from 0 to 1. This increases the contention current at the output node as \bar{B} attempts to hold the output node to 1, while \bar{C}_{in} pulls the output node to 0. The propagation delay is 34ns and the propagation delay is 973.6nW. However, the proposed ULV NP domino carry chain offers the best robustness performance with almost no deviation from the rails.

The proposed carry chain offers a great advantage in robustness and power consumption of only 396.4nW when no input bits arrive in the evaluation phase. There is almost no deviation from the rails in the *Wait* mode.



(a) Output nodes from P type Carry gates and the input signals.



(b) Output nodes from N type Carry gates.

Figure 7.11: Simulation result of 32-bit carry chain implemented in Circuit 7.9 when only input bits A get transitions.

7.3 32-bit carry chain using NP domino Carry 3 gates

An n -bit carry chain is implemented in Figure 7.12 where the ULV NP domino Carry 3 gates with PTL (implemented in Figure 6.8 on page 46) are cascaded together. The main advantage of the proposed carry chain in Figure 7.12 compared to the previous NP domino carry chain 2 (implemented in Figure 7.9) is the obviation of the ULV NP domino inverters at the output nodes of each NP ULV domino Carry 3 gate. This impacts on both speed and power performance. The bulks of the evaluation transistors labeled E_p in the P type ULV domino Carry 3 gates are floating in order to increase the strength of these transistors.

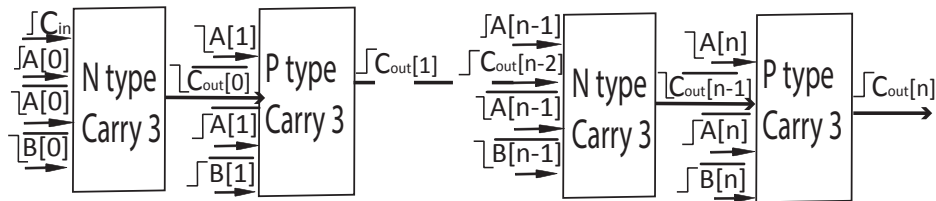
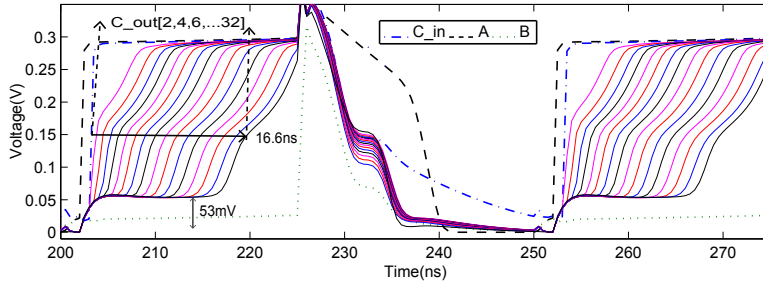


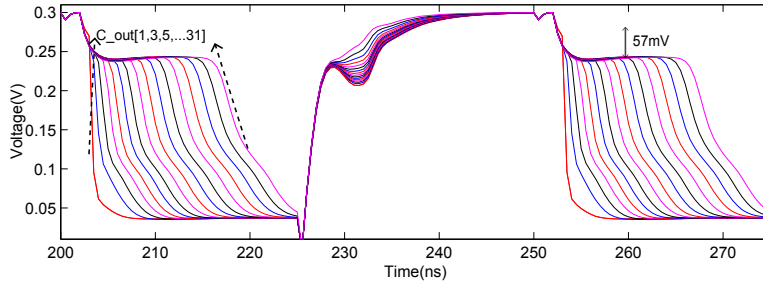
Figure 7.12: NP domino n -bit carry chain 3.

The graphs plotted in Figure 7.13 demonstrates the simulation result of 32-bit carry chain 3, considering the worst case scenario when the transitions only arrive at the input nodes B in the evaluation phase.

Comparing with the simulation results in the carry chain 2 (implemented in Figure 7.10 which is simulated for the same scenario) concludes that the speed performance is almost the same, i.e. 16.6ns, while the power consumption is reduced to 795nW with the proposed ULV domino carry chain 3. However, the noise margin is decreased before the transition occurs at the output nodes. Relative to the conventional 32-bit carry chain, the delay and EDP is only 5.17% and 36% respectively.



(a) Carry output nodes from P Type Carry gates and input signals.

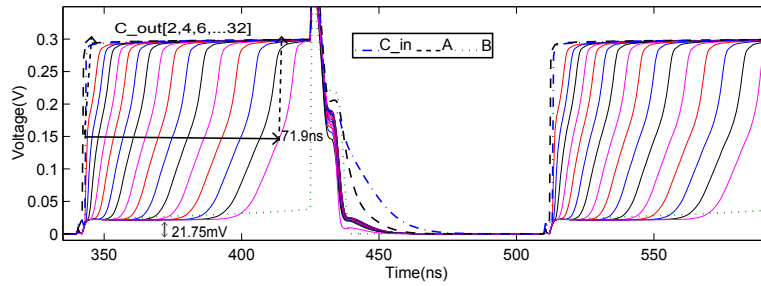


(b) Carry output nodes from N Type Carry gates.

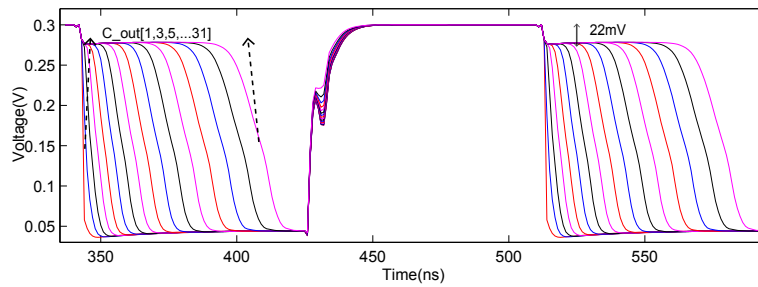
Figure 7.13: Simulation result of 32-bit carry chain implemented in Circuit 7.12 when only input bits B get transitions.

The graphs plotted in Figure 7.14 demonstrates the simulation results of the 32-bit carry chain 3, considering the worst case scenario where the transitions only arrive at the input nodes A in the evaluation phase while input nodes B remain at the precharged value. This turns on all the three evaluation transistors when transitions arrive at the carry input nodes. Considering N type Carry 3 gate, the contention current is increased as \bar{B} attempts to hold the output node to 1 through E_{N1} and E_{N2} while \bar{A} pulls the output node to 0 through E_{N3} . This decreases the speed performance significantly and the simulated propagation delay is 71.9ns for the presented scenario. Comparing with the previous simulation results, the proposed 32-bit carry chain 3 offers the least power consumption of only 405.5nW. The average deviation from the rails at the output nodes is only 22mV before the correct input transitions arrive. However, the main drawback is the significant degradation in the speed performance.

The proposed carry chain offers a great advantage in robustness with almost no deviation from the rails in the *Wait* mode. It only consumes a power of 4.85nW in the *Wait* mode.



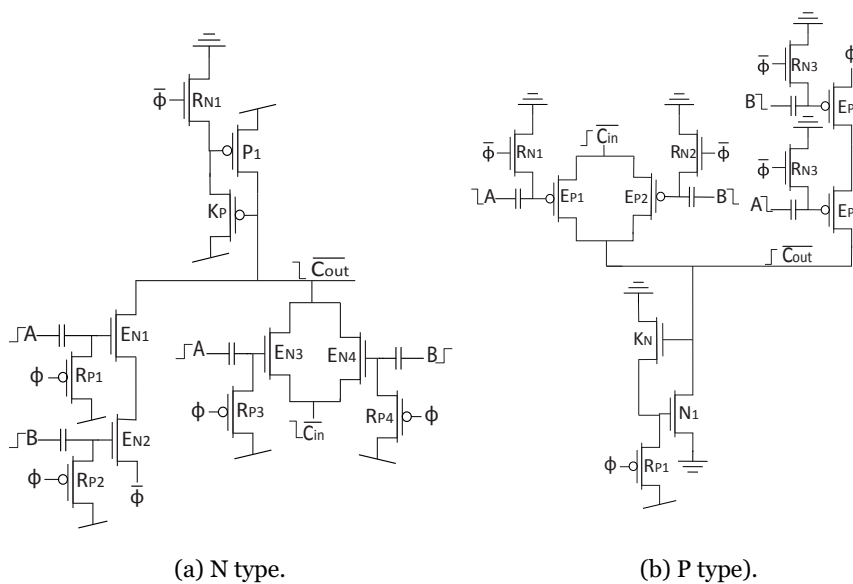
(a) Output nodes from P Type Carry gates and input signals.



(b) Output nodes from N Type Carry gates.

Figure 7.14: Simulation result of 32-bit carry chain implemented in Circuit 7.12 when only input bits A get transitions.

7.4 New implementations of 32-bit carry chain exploiting PTL



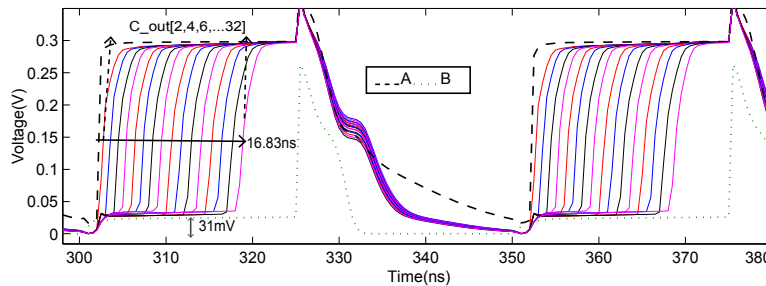
(a) N type.

(b) P type.

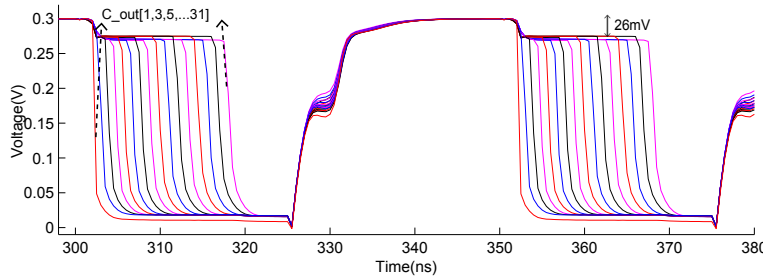
Figure 7.15: ULV domino Carry Gates using PTL (Carry 4).

The simulation results in the previous two sections utilizing PTL conclude that the propagation delay through the 32-bit carry chain 2 and 3 alters significantly in the worst case scenario when only input bits A switch instead of input bits B . The main cause of the speed degradation is the significant enhancement in the contention current, for example \bar{B} attempts to hold the output node to 1 through E_{N1} in N type Carry gates with PTL (implemented in Figure 6.6a on page 44 and 6.8a on page 46).

A new implementation of ULV NP domino Carry 4 gates is presented in Figure 7.15 to suppress the delay problem discussed in the above paragraph. Circuits in Figure 7.15a and 7.15b represents N and P type ULV domino Carry 4 gates respectively. Two serially connected evaluation transistors are proposed in Figure 7.15 instead of a single pass transistor in order to reduce the contention problem occurred in the ULV NP domino Carry 2 gates.



(a) Output nodes from P Type Carry gates and input signals.



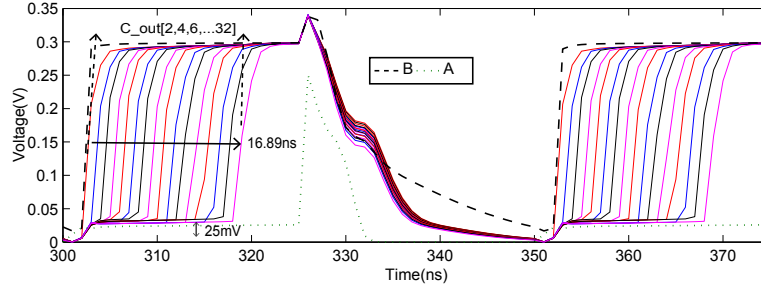
(b) Output nodes from N Type Carry gates.

Figure 7.16: Simulation result of 32-bit carry chain 4 implemented in Circuit 7.15 when only input bits A get transitions.

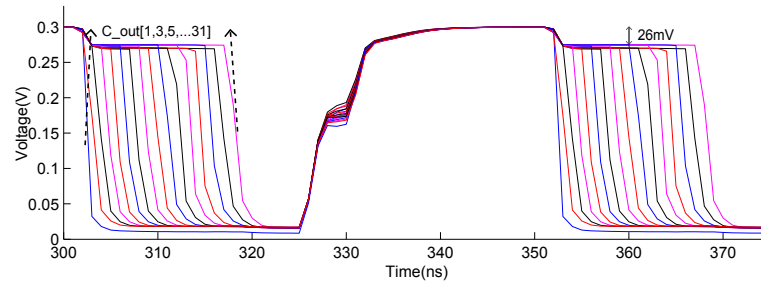
Simulation results shown in graphs in Figure 7.16 demonstrates the 32-bit carry chain 4 implemented by cascading the ULV NP domino Carry 4 gates. The worst case scenario is assumed where both input bits A and B get positive transitions in the first N type Carry 4 gate, while only input bits A get transitions on all other ULV NP domino Carry 4 gates in the chain. The propagation delay is only 16.8ns which is only 50% relative to the 32-bit propagation delay for the same scenario as shown in simulation results in Figure 7.11 on page 66.

The graphs shown in Figure 7.17 demonstrate the speed performance of the 32-bit carry chain 4. The simulations are considered for the worst case scenario, where both input bits A and B have positive transitions for the

first N type Carry 4 gate, while only input bits B switch in the rest of the NP domino Carry 4 gates in the chain.



(a) Output nodes from P Type Carry gates and input signals.



(b) Output nodes from N Type Carry gates.

Figure 7.17: Simulation result of 32-bit carry chain 4 implemented in Circuit 7.15 when only input bits B get transitions.

The simulation results presented in both Figure 7.16 and 7.17 conclude that the propagation delay is almost the same whether the transitions arrive at input nodes A or B . Thus the proposed Carry 4 gates provide a much better solution in terms of speed performance as compared to the 32-bit carry chain 2. However, the power consumption is increased to 1152nW. Relative to the conventional 32-bit carry chain, the delay and EDP is only 5.23% and 53% respectively.

However, the main drawback is the degradation in the power consumption and robustness when no transitions arrive at the input nodes and the output nodes hold the precharged value. The power consumption is 809nW with an average deviation of 16.5mV from the rails in the *Wait* mode.

An new implementation for ULV NP domino Carry 5 gates are proposed in Figure 7.18 in order to increase the speed performance by reducing the contention current, which is increased while only input bits A get transition in the worst case scenario in 32-bit ULV domino carry chain 3 (implemented in Figure 7.12 on page 66). The propagation delay is increased to 71.9ns as shown in simulation results in Figure 7.14 (page 68).

Two serially connected evaluation transistors are proposed in Figure 7.18 instead of a single pass transistor in order to reduce the contention problem occurred in the ULV NP domino Carry 3 gates.

The graphs in Figure 7.19 demonstrates the worst case scenario of 32-bit NP domino Carry 5 gates where only input bits A switch at the input nodes of every ULV NP domino Carry 5 gates in the chain. The propagation

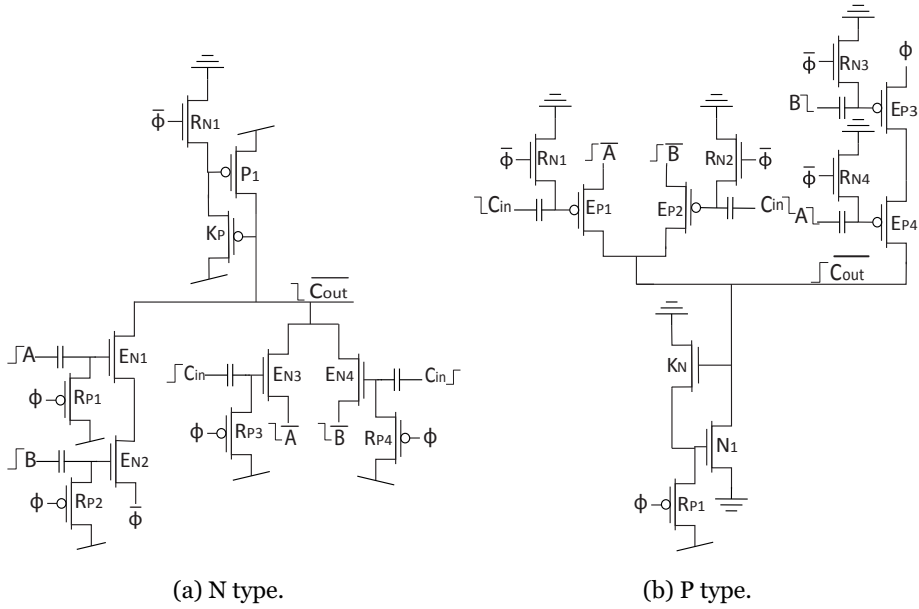
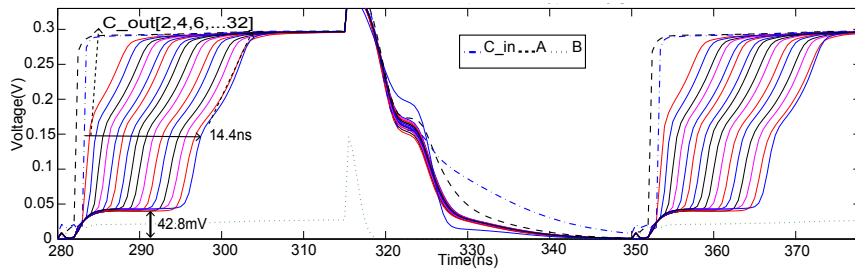
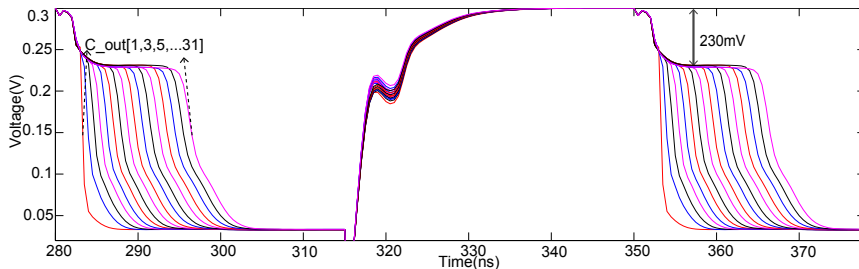


Figure 7.18: ULV domino Carry Gates using PTL (Carry 5).



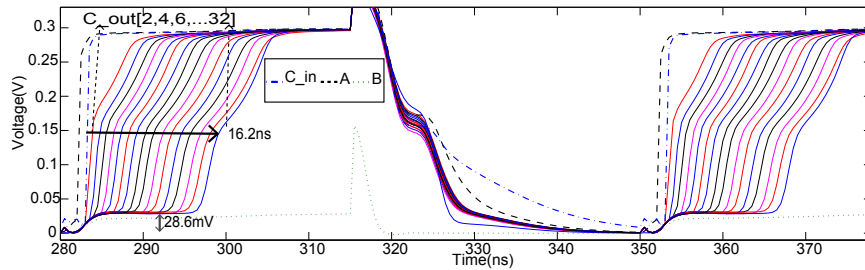
(a) Output nodes from P Type Carry gates and input signals.



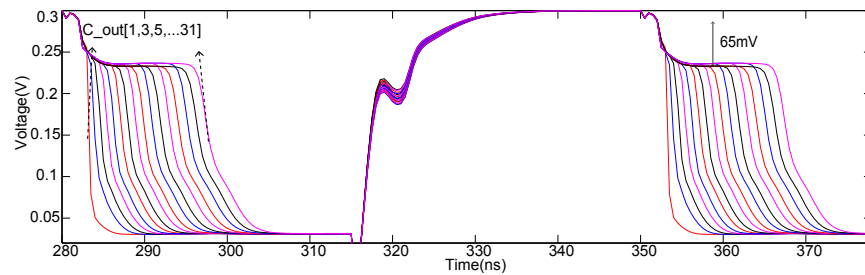
(b) Output nodes from N Type Carry gates.

Figure 7.19: Simulation result of 32-bit carry chain 5 implemented in Circuit 7.18 when only input bits *A* get transitions.

delay of 32-bit carry chain 5 is significantly decreased. The delay is only 20% relative to the delay shown in simulation results in Figure 7.14 (on page 68). Speed performance is improved at the cost of slightly increment in the power consumption. The 32-bit propagation delay and power consumption is 14.5ns and 644nW respectively. Relative to the conventional 32-bit carry chain, the delay and EDP is only 4.5% and 22.27% respectively. The deviation from the rails is 55mV at the output nodes before the correct input transitions arrive.



(a) Output nodes from P Type carry gates and input signals.



(b) Output nodes from N Type carry gates.

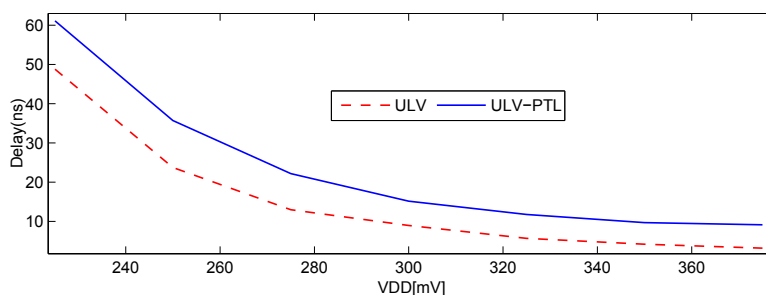
Figure 7.20: Simulation result of 32-bit carry chain 5 implemented in Circuit 7.18 when only input bits *B* get transitions.

The graphs shown in Figure 7.20 demonstrate the simulation results of 32-bit carry chain 5. The simulations are considered for the worst case scenario when the transitions only arrive at the input nodes *B* in all ULV NP domino Carry 5 gates. The circuit offers improvement in both speed and power consumption compared to the simulation results shown in Figure 7.13 (on page 67). The 32-bit propagation delay and power consumption is 16.2ns and 615.8nW respectively. Relative to the conventional 32-bit carry chain, the delay and EDP is only 5.05% and 26.5% respectively. The deviation from the rails is 46mV at the output nodes before the correct input transitions arrive.

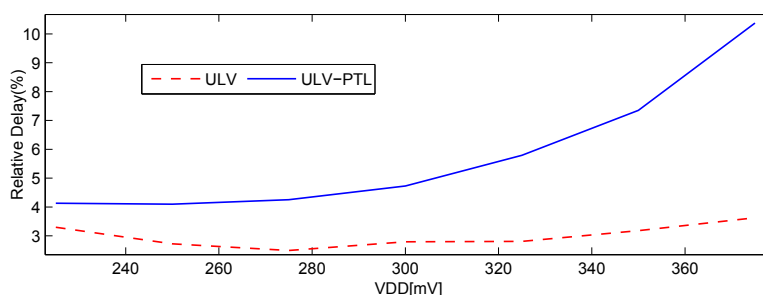
The simulation results conclude that 32-bit carry chain 5 offers the most fair performance in terms of power, robustness and speed compared to all previous 32-bit carry chain implementations, in both propagation and *Wait* mode. The power consumption is only 313nW with an average deviation of 11.5mV from the rails in the *Wait* mode.

7.5 Performance of ULV 32-bit carry chains at different supply voltages

Two configurations of proposed 32-bit NP domino carry chains are simulated at different supply voltages, and the performance is compared with conventional 32-bit carry chain with respect to speed, power and EDP.



(a) Delay in ns



(b) Delay (%) relative to conventional.

Figure 7.21: Delay for two ULV NP domino 32-bit carry chains compared with conventional 32-bit carry chain for different supply voltages.

The plots in Figure 7.21 demonstrate the propagation delay for two proposed ULV domino 32-bit carry chains in the worst case scenario. The dashed curve named *ULV* represents the speed performance for ULV domino 32-bit carry chain implemented in Figure 7.1 (on page 55) and the solid curve named *ULV-PTL* represents the speed performance for 32-bit ULV domino Carry 4 gates presented in Figure 7.15 (on page 68).

The subgraph in Figure 7.21a represents the propagation delay for proposed domino 32-bit carry chains. The simulation results conclude that *ULV* domino carry chain offers better speed performance than *ULV-PTL* carry chain. The propagation delay is under 65ns for the supply voltage of 200mV, and decreases to 15ns when the supply voltage rises to 400mV.

The propagation delay relative to the conventional CMOS 32-bit carry chain is presented in Figure 7.21b. The relative delay is less than 10% for the simulated ULV domino carry chains as the supply voltage varies from 200mV to 400mV. *ULV* carry chain offers the best speed performance at the supply voltage of 275mV, where the delay is only 1% relative to conventional CMOS carry chain.

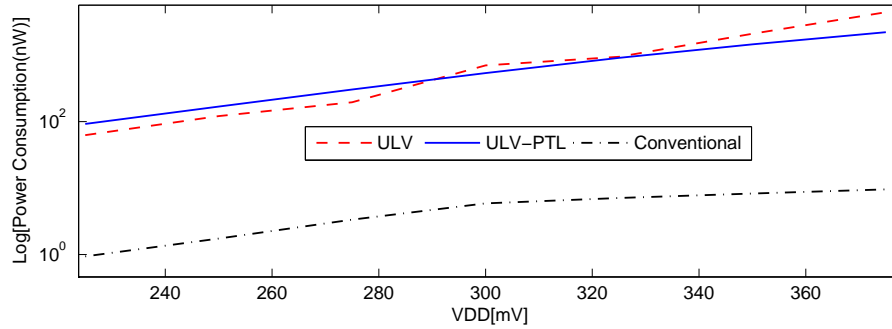
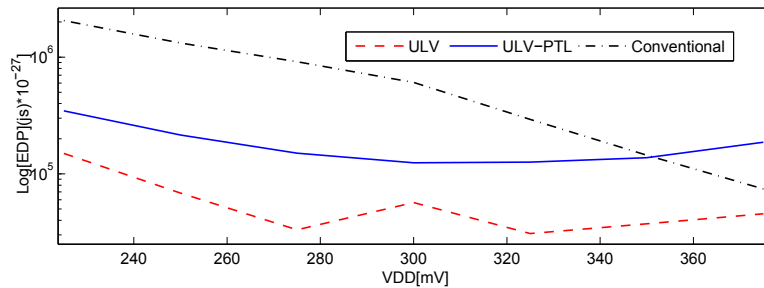
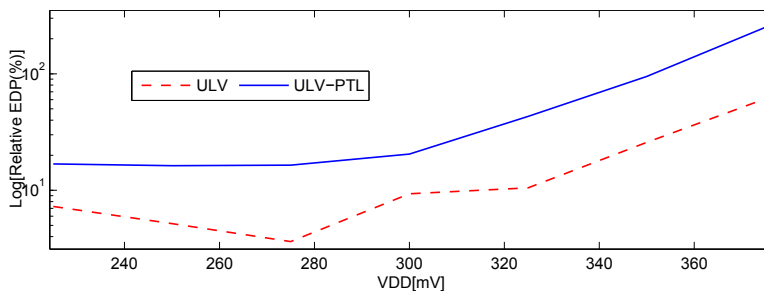


Figure 7.22: Power consumption of ULV domino 32-bit carry chain compared to conventional CMOS carry chain.

The graph in Figure 7.22 compares the power consumption of proposed ULV NP domino 32-bit carry chains and the conventional 32-bit carry chain in the worst case scenario. The graph concludes that the proposed domino carry chains consume more power than the conventional carry chain as expected, giving the advantage of superb speed performance. The graph also concludes that *ULV* consumes less power than *ULV-PTL* at low supply voltages, however when the supply voltage exceeds 290mV, *ULV* consumes more power than *ULV-PTL*. Although *ULV* consumes less power than *ULV-PTL*, it still results in better speed performance as mentioned earlier.



(a) EDP (Logarithmic scale)



(b) EDP (%) relative to conventional.

Figure 7.23: EDP for two ULV NP domino 32-bit carry chains compared with conventional 32-bit carry chain for different supply voltages.

Energy delay product (EDP) for the proposed 32-bit carry chain is compared with the conventional carry chain for different supply voltages.

The simulated results are implemented in graphs in Figure 7.23. Figure 7.23a presents the logarithmic y-axis which concludes that EDP for the proposed ULV domino carry chain is far lower than the conventional carry chain at ultra low supply voltages. The graph in Figure 7.23b proves that the relative EDP of *ULV* carry chain is less than 5% of the conventional carry chain at the supply voltage of 275mV.

7.6 Summary

A summary of various implementations of 32-bit carry chain together with the strength factor parameters of different kinds of transistors is shown in this section. In Table 7.2, the strength parameters for different kinds of transistors are given.

Simulation results	Transistor strength parameters(Sizing(nm))($\frac{W}{L}$) and biasing)			
Figure	R_M	$E R K$	P	N
7.2	$\frac{W_{min}}{L_{min}}$ L-thr <i>RBB</i>	$\frac{W_{min}}{L_{min}}$ L-thr <i>RBB</i>	$\frac{W_{min}}{L_{min}}$ L-thr <i>F</i>	$\frac{W_{min}}{L_{min}}$ L-thr <i>F</i>
7.3	$\frac{W_{min}}{L_{min}}$ L-thr <i>RBB</i>	$\frac{W_{min}}{L_{min}}$ L-thr <i>RBB</i>	$\frac{150}{300}$ L-thr <i>FBB</i>	$\frac{W_{min}}{L_{min}}$ L-thr <i>FBB</i>
7.4	$\frac{W_{min}}{L_{min}}$ L-thr <i>RBB</i>	$\frac{W_{min}}{L_{min}}$ L-thr <i>RBB</i>	$\frac{200}{300}$ L-thr <i>FBB</i>	$\frac{200}{200}$ L-thr <i>RBB</i>
7.6	$\frac{W_{min}}{L_{min}}$ H-thr <i>RBB</i>	$\frac{W_{min}}{L_{min}}$ L-thr <i>RBB</i>	$\frac{150}{300}$ L-thr <i>FBB</i>	$\frac{120}{100}$ L-thr <i>FBB</i>
7.7	$\frac{W_{min}}{L_{min}}$ L-thr <i>RBB</i>	$\frac{W_{min}}{L_{min}}$ L-thr <i>RBB</i>	$\frac{200}{300}$ L-thr <i>V</i>	$\frac{W_{min}}{L_{min}}$ L-thr <i>V</i>
7.8	$\frac{W_{min}}{L_{min}}$ H-thr <i>RBB</i>	$\frac{W_{min}}{L_{min}}$ L-thr <i>RBB</i>	$\frac{150}{200}$ L-thr <i>V</i>	$\frac{W_{min}}{L_{min}}$ L-thr <i>V</i>
7.10 and 7.11	$\frac{W_{min}}{L_{min}}$ L-thr <i>RBB</i>	$\frac{W_{min}}{L_{min}}$ L-thr <i>RBB</i>	$\frac{120}{200}$ L-thr <i>FBB</i>	$\frac{W_{min}}{L_{min}}$ L-thr <i>F</i>
7.13 and 7.14	$\frac{W_{min}}{L_{min}}$ L-thr <i>RBB</i>	$\frac{W_{min}}{L_{min}}$ L-thr <i>RBB</i>	$\frac{120}{200}$ L-thr <i>FBB</i>	$\frac{120}{200}$ L-thr <i>RBB</i>
7.16 and 7.17	$\frac{W_{min}}{L_{min}}$ L-thr <i>RBB</i>	$\frac{W_{min}}{L_{min}}$ L-thr <i>RBB</i>	$\frac{120}{200}$ L-thr <i>FBB</i>	$\frac{120}{100}$ L-thr <i>F</i>
7.19 and 7.20	$\frac{W_{min}}{L_{min}}$ L-thr <i>RBB</i>	$\frac{W_{min}}{L_{min}}$ L-thr <i>RBB</i>	$\frac{120}{200}$ L-thr <i>FBB</i>	$\frac{120}{175}$ L-thr <i>RBB</i>

Table 7.2: Strength parameters for different transistors in various configurations of 32-bit carry chains.

R_M represents the recharge transistors labeled R_P in the N type ULV domino Carry gates and R_N in all P type ULV domino Carry gates. K represents the keeper transistors labeled K_N in all the N type ULV domino Carry gates and K_P in all the P type ULV domino Carry gates. E represents all the evaluation transistors labeled E_N in all the N type ULV domino Carry gates and E_P in all the P type ULV domino Carry gates. R represents the recharge transistors labeled R_N in all the N type ULV domino Carry gates and R_P in all P type ULV domino Carry gates. P and N represents the evaluation transistors labeled P and N in all the P and N type ULV domino Carry gates.

The three most important strength tuning factors for all these different transistors are also given in Table 7.2. The first parameter represents the dimensions of the transistors. The second parameter represents the low threshold ($L - thr$), standard threshold ($S - thr$) and high threshold ($H - thr$] transistors. The third parameter represents the biasing scheme at the bulk terminals of the transistors. F represents floating bulk terminals. *RBB* represents the Reverse Body Biasing at the bulk terminals

by connecting the bulk terminals to V_{DD} for pMOS and GND for nMOS. *FBB* represents Forward Body Biasing at the bulk terminals by connecting the bulk terminals to V_{DD} for nMOS and GND for pMOS. V represents the variable threshold voltage for the transistors by connecting the bulk terminals of pMOS to $\bar{\phi}$ and nMOS to ϕ .

Table 7.3 summarizes the performance of different configurations of 32-bit carry chains simulated for the worst case scenario. The table represents the propagation delay T_D together with the power consumption, deviation from the rails (Dev) and other figure of merits (PDP and EDP). Besides this, the table also represents the T_D , PDP and EDP relative to a conventional 32-bit carry chain.

Figure	Simulation Results					Relative(%)		
	T_D (ns)	Power (nW)	Energy(fj)	EDP (yjs)	Dev(mV)	T_D	PDP	EDP
Conventional	320.7	5.91	1.89	607.8	0	100	100	100
7.2	5.2	1068	5.55	28.88	136	1.62	293.6	4.75
7.3	8.6	667	5.73	49.3	44	2.68	303.2	8.11
7.4	8.97	705.5	6.33	56.76	38	2.8	335	9.34
7.6	24.18	517	12.5	302.2	24	7.54	661	49.7
7.7	16	718	11.48	183.8	33.5	4.99	607	30.24
7.8	19.6	410.7	8.05	157.7	25	6.1	426	25.9
7.10	16.1	1067	17.1	276	27	5.02	904.7	45.4
7.11	34	973.6	33	1125	0	10.6	1746	185
7.13	16.6	795	13.2	219	55	5.17	698	36.03
7.14	71.9	405.5	29.1	2092	22	22.4	1539	344
7.16 and 7.17	16.8	1152	19.3	324	27	5.23	1021	53
7.19	14.5	644	9.38	135.4	55	4.5	496	22.27
7.20	16.2	615.8	9.97	161.6	46	5.05	527	26.5

Table 7.3: Performance of various configurations of 32-bit carry chains in the worst case scenario.

The simulation results conclude that the worst case speed scenario for a 32-bit carry chain is not probably worst case power consumption scenario for the proposed ULV domino logic style. The proposed ULV domino 32-bit carry chains consumes more power in the evaluation phase when the output nodes hold the precharged value and *Wait* for the correct transitions at the input nodes. The worst case power scenario occurs when the output nodes hold the precharged value during the whole evaluation phase.

Table 7.4 summarizes the power consumption in the *Wait* Mode I for different configurations of 32-bit carry chains. The carry chains are simulated assuming that both input bits at the first N type ULV domino Carry gates remain low in the whole evaluation phase, meanwhile one of the two input bits switch in all the further ULV domino Carry gates in the chain. The table also represents the average deviation between the output nodes of N and P type ULV domino Carry gates, i.e. deviation from 0 and 1 for P and N type ULV domino gates respectively.

Figure	Simulation Results	
	Power (nW)	Dev(mV)
7.3	1161	51.5
7.4	1163	48.5
7.6	1047	61
7.7	1086	35
7.8	963	43
7.10	1136	30
7.11	539.7	0.9
7.13	1022	72
7.14	475	21
7.16 and 7.17	1172	34
7.19	1072	55
7.20	908	50

Table 7.4: Power consumption and deviation of 32-bit carry chains in the *Wait Mode I*.

Table 7.5 summarizes the power consumption and deviation in the *Wait Mode II* for the various configurations of 32-bit ULV domino carry chains. The carry chains are simulated assuming that all the input bits remain 0 and 1 during the evaluation phase for all N and P type ULV domino Carry gates in the chain respectively. The output nodes hold the precharged value as no transitions arrive at the input nodes.

Figure	Simulation Results	
	Power (nW)	Dev(mV)
7.3	687	28
7.4	685	24
7.6	655.6	26
7.7	660.7	20.5
7.8	652.1	26.5
7.10 and 7.11	396.4	0
7.13 and 7.11	4.85	0
7.16 and 7.17	809	16.5
7.19 and 7.20	313	11.5

Table 7.5: Power consumption and deviation of 32-bit carry chains in the *Wait Mode II*.

The simulation results for different scenarios conclude that for high speed applications, the carry input signal utilizes only a delay of 8.2ns to propagate through a proposed ULV NP domino 32-bit carry chain. However the conventional 32-bit carry chain utilizes a propagation delay of 321ns to perform the same operation. The delay for the high speed carry chain is only 2.68% relative to conventional 32-bit carry chain. The high speed performance has an adverse affect on the power consumption. The high speed carry chain consumes a power of 1068nW whereas the conventional 32-bit carry gate only consumes a power of 5.91nW. However, EDP for the proposed high speed 32-bit carry chain is only 4.75% relative to the conventional carry chain due to the superb speed performance. Although

the 32-bit high speed offers a great advantage of speed improvement in the worst case scenario, the circuit also consumes a power of 687nW when no transitions arrive at the input nodes and the output nodes hold the precharged value. This is due to the leakage problem at ultra low supply voltages in the serially connected transistors.

Using the Multi threshold CMOS technique by implementing both high threshold and low threshold evaluation transistors, the 32-bit ULV domino carry chain consumes the least power consumption in the worst case scenario. The power consumption is only 517nW, offering a propagation delay of 24ns. The relative delay and EDP is only 7.54% and 49.7% respectively compared to the conventional 32-bit carry chain. Although the power consumption is least in the worst case scenario, it increases to 655nW when no input transitions arrive at the input nodes.

The lowest power consumption is obtained by ULV NP domino 32-bit carry gate which is utilized by pass transistor logic. The average propagation delay is 44ns in the worst case scenario for the low power 32-bit ULV domino carry chain. The delay for this low power 32-bit carry chain is only 13.7% relative to the conventional 32-bit chain. It consumes a power of 600nW for the 32-bit operation. It offers the least power consumption of only 4.85nW when no transitions arrive at the input nodes.

Chapter 8

Results - Overview of the papers

This chapter briefly summarizes all the three papers which are written throughout the master project. Each of the sections related to the papers states an outline including motivation, results and conclusion.

8.1 Paper I

High Speed and Ultra Low-voltage CMOS Domino Carry gates

Outline: The 1-bit full adder is the most fundamental arithmetical function in any kind of processor, and is the building block for many processing operations like Arithmetic Logic Unit (ALU), Floating Point Unit (FPU) and Application-Specific Integrated Circuit (ASIC). The overall worst case delay is obtained when the carry signal propagates through the full adder. This makes the carry propagation path the most critical and speed limiting factor for many high speed applications. Three novel configurations of ULV NP domino carry circuits (Carry 1, Carry 2 and Carry 3) are proposed in this paper in order to enhance the speed performance of the full adder.

Results: The proposed NP domino carry circuits are designed to operate at ultra low supply voltages. The performance for the proposed ULV NP domino carry gates and the conventional CMOS carry gate is compared with respect to speed, robustness and Energy Delay Product (EDP). The circuits are characterized at different supply voltages in the region of 200mV to 350mV. The simulation results conclude that the delay for all the proposed ULV carry gates is lower than 5% relative to the conventional CMOS carry gate as the supply voltage varies between 220mV to 300mV. Carry 2 gate offers the best speed performance at 250mV where the relative delay is only 2% compared to the conventional CMOS carry gate. The simulation results also conclude that the EDP is less than 1% for all the proposed ULV domino carry gates for the supply voltage less than 325mV relative to conventional CMOS carry gate. Carry 2 offers the EDP of only 0.02% relative to conventional CMOS carry gate at a supply voltage of 250mV.

Conclusion: The proposed ULV domino carry gates offer superb speed performance, i.e. the delay and EDP relative to conventional CMOS carry gate is less than 5% and 1% respectively at a supply voltage of 325mV. The presented ULV domino carry gates are proposed for low voltage and high speed full adders. Due to superb speed performance, the present ULV domino gates can be a possible substitution for parallel design to enhance the speed performance of the full adders. This may reduce the area and complexity of the system.

8.2 Paper II

Static NP Domino Carry gates for Ultra Low Voltage and High Speed Full Adders

Outline: Paper II[30] resulted in an invitation to submit a journal paper. A more detailed description for the ULV NP domino carry gates proposed in [30] is given in this paper. Furthermore, the proposed circuits are analyzed and simulated in more details in order to obtain the Minimum Energy Point (MEP).

Results: All the circuits are simulated for the worst case scenario where the carry signal propagates through the circuits. Relative to conventional CMOS carry gate, the propagation delay is less than 20% for all the proposed ULV domino carry gates when the supply voltage varies between 175mV and 375mV. The overall best relative delay is achieved by using ULV domino carry gate with pass transistor logic (PTL). The reason is because the input carry bit only needs to propagate through a single transistor to reach the output node. Compared to the conventional carry gate, the least average delay is achieved at the supply voltage of 275mV, where Carry 2 only utilizes a relative delay of 2.48%.

The power consumption per ULV domino carry gate is compared with conventional CMOS carry gate at different supply voltages. As expected the power consumption for the ULV domino carry gates exceeds the power consumption of the conventional CMOS carry gate, offering the advantage of fast switching speed. Carry 2 and Carry 3 are utilized with PTL which contribute minimum power consumption than Carry 1.

Further, the energy of the ULV domino carry gates is compared with the conventional CMOS carry gate for different supply voltages. PDP for each of the proposed ULV carry gates is lower than the conventional carry gate for the supply voltage between 175mV and 350mV. This is mainly caused due to significant improvement in the speed performance for the proposed carry gates relative to the conventional carry gate. All the proposed ULV domino carry gates have the minimum relative PDP of lower than 25% at the supply voltage of 250mV, which makes it the Minimum Energy Point (MEP). Carry 2 is the most efficient solution as it only contributes 15.65% PDP relative to conventional Carry gate at MEP.

The relative EDP for all the proposed ULV domino carry gates is less than 30% for the supply voltage between 175mV and 375mV. At MEP (250mV), the EDP for all the proposed ULV carry gates is lower than 1.5%

relative to a conventional carry gate. However, Carry 2 is characterized by least relative EDP with a value closer to 0.527% at 275mV.

Conclusion: In this paper, different configurations of static ULV NP domino carry gates are presented using precharge and pass transistor logic. The proposed ULV domino carry gates are aimed for high speed serial adders in ultra low-voltage applications. In terms of frequency, speed, PDP and EDP, the ULV carry gates offers significant improvement compared to conventional CMOS carry gate. Both complexity and area may be saved if proposed ULV domino carry gates are implemented instead of applying carry look ahead techniques or parallel structures in order to enhance the speed performance for the full adders.

8.3 Paper III

Ultra-Low Voltage and High Speed NP Domino Carry Propagation chain

Outline: All the ULV domino carry gates implemented in [30] add only 2 single bits. If the arithmetic operation of more than 2-bits is desired, the proposed ULV domino carry gates are cascaded in a serial chain. In this paper, we exploit the performance of one of the proposed ULV NP domino carry gates in a 32-bit chain. Further, we compare the performance of proposed ULV NP domino 32-bit carry chain with the conventional 32-bit carry chain with respect to speed and Energy Delay Product (EDP).

Results: The proposed ULV domino 32-bit carry chain is simulated for worst case scenario, when the carry signal ripples through the whole chain. Both the conventional ULV domino carry chain and the conventional carry chain are simulated at a supply voltage of 300mV. A transient simulation is shown in the paper where the output waveforms of all ULV NP domino carry gates are shown. As expected, the propagation delay of the proposed carry chain is far lower than the conventional CMOS carry chain. Conventional carry chain has a propagation delay of approximately 321ns whereas the proposed ULV domino requires only 8.6ns to propagate from 1 to 32 bit. The simulated response also demonstrates that the logic levels of output waveforms are very close to the rails, resulting in a robust design with better noise margin.

Conclusion: In this paper we have presented a novel 32 bit ULV NP domino carry chain. The proposed ULV carry gates are used to achieve a very fast carry computation, offering a superb speed feature, i.e. the delay compared to the conventional CMOS carry chain is only 2.68% for a supply voltage of 300mV with almost no degradation in the noise margin. The EDP for the proposed ULV domino carry chain is approximately 8% relative to the conventional CMOS carry chain at the same supply voltage. The clock signal necessitates only a period of 20ns to execute an addition of 32 bits. ULV NP domino carry gates may be used to save power and area compared

to parallel designed adders for ultra low voltage and high speed applications.

Chapter 9

Discussion

9.1 Power consumption in the idle mode

Although ULV NP domino logic gates implemented in this thesis offer significant improvement in the speed performance compared to the conventional CMOS logic gates, the proposed gates also consume more power than the conventional CMOS logic gates. Considering the example of the proposed ULV NP domino 32-bit carry chains. The chains have the enormous power consumption when no transitions arrive at the input nodes in the idle mode and the output nodes hold the precharged value.

9.2 Performance of ULV NP domino carry chains with Pass Transistor Logic

The proposed ULV NP domino Carry 2 gates with PTL is the most efficient solution in terms of speed, area and power consumption compared to other proposed ULV NP domino Carry gates when an addition of only 2 bit is desired. The performances degrade when cascading the proposed NP domino Carry 2 gates in a long chain. This is due to the inclusion of the ULV NP domino inverters at the output nodes in order to obtain the specific carry signal for the further Carry 2 gates in the chain.

Another major challenge while cascading the proposed ULV NP domino Carry gates with PTL in a 32-bit chain is the degradation in the speed performance when the chain is simulated for the worst case scenario. For example if the transitions only arrive at input nodes *A* instead of input nodes *B* for all the NP domino Carry gates in the chain, the contention current is increased which degrades the speed performance. However ULV NP domino carry chains with PTL offer better robustness performance. ULV NP domino carry chains with PTL offer minimum power consumption than other proposed ULV domino carry chains in the idle state. New hybrid solutions are proposed to increase the speed performance for the 32-bit ULV NP domino carry chains with PTL by suppressing the contention current. However this degrades the robustness performance and increases the power consumption due to the serially connected transistors.

9.3 Leakage at the output nodes

One other main challenge while cascading the proposed ULV NP domino logic gates in long chains is the leakage problem at the output nodes. If the evaluation transistors labeled P and N are not strong enough to hold the precharged value, the output nodes may have the false transitions before the correct transitions arrive at the input nodes. However, increasing the strength of these transistors suppress the leakage problem at the cost of degradation in the speed performance for the proposed ULV NP domino gates. Multi-Threshold CMOS (MTCMOS), Variable-Threshold CMOS (VTCMOS) and carry gates with PTL are utilized in the 32-bit ULV domino carry chain to suppress the leakage problem in the worst case scenario. This offers better robustness performance and minimizes the power consumption but degrades the speed performance.

The simulation results conclude that the proposed ULV NP domino gates are suitable for high speed applications at ultra low supply voltages. However the proposed gates may not offer the best solution for low power applications.

Chapter 10

Conclusion

10.1 Summary of the contributions

This section summarizes the results of different NP domino ULV logic gates proposed throughout this master project.

In Chapter 4, the working operation of ULV domino logic is described in detail. Further novel ULV NP domino inverters are proposed and the simulation results are compared with the conventional CMOS inverter with respect to speed and robustness performance. The simulated circuits are targeted to a supply voltage of 300mV. The simulation results conclude that the proposed ULV NP domino inverters degrade the robustness performance, however the delay, Power Delay Product (PDP) and Energy Delay Product (EDP) is improved significantly compared to conventional CMOS inverter. New approaches like pseudo ULV NP domino and ULV NP domino inverters with keeper are introduced to enhance the robustness performance for the proposed ULV NP domino inverters. These new approaches improve the performance for the ULV NP domino inverters in all aspects.

ULV NAND and NOR ULV logic gates are presented in Chapter 5 by utilizing NP domino floating gate transistors. Various novel configurations for ULV NP domino logic gates are proposed by using the conventional style and pass transistor logic (PTL) style. The proposed gates are compared with the conventional NAND and NOR logic gates with respect to speed performance. The simulation results have concluded that ULV NP domino gates with PTL offers better speed performance than other configurations due to the reduced number of transistors.

Various novel configurations of ULV NP domino Carry gates are implemented in Chapter 6 in order to enhance the speed performance of the 1-bit full adder. The performance for the proposed ULV NP domino Carry gates are compared with the conventional CMOS carry gate with respect to speed, power, robustness, PDP and EDP. The simulation results are characterized as the supply voltages varies between 100mV and 400mV. The simulation results conclude that the proposed ULV NP domino Carry gates offer a significant improvement in terms of speed, robustness, PDP and EDP relative to the conventional CMOS Carry gate.

Montecarlo simulations are also included with process and mismatch variations at different supply voltage in the range between 100mV and

400mV which showed better robustness for the proposed ULV NP domino Carry gates. The performance with montecarlo simulations for the domino Carry gates is not compared with the conventional CMOS Carry gate as the conventional CMOS carry gate is unable to operate at ultra low supply voltages with high operating frequencies.

Various configurations of 32-bit carry circuits are utilized in Chapter 7 with the help of proposed ULV NP domino Carry gates. The proposed ULV NP domino 32-bit carry circuits are compared with the conventional 32-bit carry circuit with respect to speed, power, robustness, PDP and EDP at a supply voltage of 300mV.

The simulation results conclude that the fastest 32-bit carry chain utilizes the propagation delay of only 8.2ns for the carry input signal to propagate through 32-bits full adder. However the chain also consumes a power of 687nW when no transitions occur at the input nodes and the output nodes hold the precharged value. On the other hand, the least power consumption is obtained by ULV NP domino 32-bit carry chain with PTL. The average propagation delay is 44ns in the worst case scenario for the low power 32-bit ULV domino carry chain. However it offers the least power consumption of only 4.85nW when no transitions arrive at the input nodes.

Both high speed and low power 32-bit ULV domino carry chains are simulated at the worst case scenario as the supply voltage varies between 225mV and 375mV and the performance is compared to conventional 32-bit carry chain with respect to speed, power and EDP. The high speed ULV NP domino carry chain offers the least relative delay and EDP at a supply voltage of 275mV.

10.2 Innovation throughout the project

There are several new innovations presented in this thesis. All the various approaches of ULV NP domino logic gates presented in Chapter 5, 6 and 7 are founded by the author of this thesis. The ULV NP domino Carry gates/chains presented in Chapter 6 and 7 are published/submitted to various conferences/journal. Some of the key logic gates utilizing NP domino floating gate transistors in this thesis are listed below:

- Various implementations of ULV NP domino NAND and NOR gates
- Various implementations of ULV NP domino Carry gates
- Various implementations of ULV NP domino 32-bit carry chains

10.3 Further work

This thesis has mostly concerned the speed improvement in the digital logic circuits by exploiting the floating gate techniques when the supply voltage scales down. Still, the potential for the further work is immense and some of the major interesting research topics are listed below:

- Different body biasing schemes are utilized in order to scale down the threshold voltage of the transistors. However Forward Body Biasing

and floating bulk terminals of nMOS transistors can be a challenging task in the layout stage. The transistors with various body biasing schemes should be designed at the layout stage to verify the area consumption across different processes for the proposed ULV NP domino logic gates.

- Multi-Threshold CMOS (MTCMOS) and Variable-Threshold (VTC-MOS) techniques are applied to enhance the speed and to suppress the leakage power for the proposed ULV NP domino circuits. Layout should be implemented to discover the major challenges while utilizing these techniques and how these challenges impact on the performance of the circuits.
- The fastest 32-bit carry circuit consumes an amount of power that may be high for low power applications in the idle mode when no transitions arrive at the input nodes. New solutions should discover to suppress the power consumption in the idle mode without degrading the speed performance or increasing the complexity of the circuits.
- Other digital logic circuits, for example the summation circuit for the full adder can be constructed by utilizing the proposed ULV NP domino logic style. The full adders may be further used to implement CMOS multiplier functions utilizing the same logic style.
- All the simulation results shown throughout this thesis are only done at the schematic level. To obtain more realistic simulations, the physical layout parameters, for example the parasitic effects and the interconnect capacitance must be taken into consideration. The optimal goal would be to design the layout of all the proposed ULV NP domino circuits with various techniques and verify their performance with different aspects. A chip could be constructed for the ULV NP domino circuit which offers the best performance with respect to speed, power and area consumption. This was not in the scope of the master project due to the limited project time.

Appendix A

Truth Tables

A	B	\bar{A}	\bar{B}	$NAND$	AND	NOR	OR
0	0	1	1	1	0	1	0
0	1	1	0	1	0	0	1
1	0	0	1	1	0	0	1
1	1	0	0	0	1	0	1

Table A.1: Truth table of main logical functions

A	B	Sum	$Carry_out$
0	0	0	0
0	1	1	0
1	0	1	0
1	1	0	1

Table A.2: Truth table: Half Adder

C_in	A	B	Sum	$Carry_out$
0	0	0	0	0
0	0	1	1	0
0	1	0	1	0
0	1	1	0	1
1	0	0	1	0
1	0	1	0	1
1	1	0	0	1
1	1	1	1	1

Table A.3: Truth table: Full Adder

Appendix B

Publications

Paper I

High Speed and Ultra Low-voltage CMOS Domino Carry gates

*Published at 12th International Conference on Electronics, Hardware,
Wireless and Optical Communications (EHAC'13), pp. 52-57, Cambridge,
UK, February 20-22, 2013.*

High Speed and Ultra Low-voltage CMOS Domino Carry gates

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Abstract: In this paper we present ultra low-voltage and high speed CMOS domino Carry gates. For supply voltages below $325mV$ the delay for the proposed ultra low-voltage Carry gates are approximately 5% relative to a complementary CMOS Carry gate. Furthermore, the Energy Delay Product is less than 1% relative to complementary CMOS Carry gate at the same supply voltage. Different domino Carry gates are presented using pass transistor logic. The proposed ultra-low-voltage domino carry gates are going to be used in low-voltage and high speed adders.

Key-Words: Low-Voltage, High-Speed, Carry gate, Domino Logic, Precharge, CMOS.

I Introduction

In recent years, the power problem has emerged as one of the fundamental limits facing the future of CMOS integrated circuit design. The aggressive scaling of device dimensions to achieve greater transistor density and circuit speed results in substantial subthreshold and gate oxide tunneling leakage currents. Energy-efficiency is one of the most required features for modern electronic systems designed for high-performance and/or portable applications. In one hand, the ever increasing market segment of portable electronic devices demands the availability of low-power building blocks that enable the implementation of long-lasting battery-operated systems. On the other hand, the general trend of increasing operating frequencies and circuit complexity, in order to cope with the throughput needed in modern high-performance processing applications, requires the design of very high-speed circuits.

Depending upon the application, there are numerous methods that can be used to reduce the power consumption of VLSI circuits, these can range from low-level measures based upon fundamental physics, such as using a lower power supply voltage or using high threshold voltage transistors; to high-level measures such as clock-gating or power-down modes. The power consumption in digital circuits, which mostly use complementary metal-oxide semiconductor (CMOS) devices, is proportional to the square of the power supply voltage; therefore, voltage scaling is one of the important methods used to reduce power consumption. To achieve a high transistor drive cur-

rent and thereby improve the circuit performance, the transistor threshold voltage must be scaled down in proportion to the supply voltage. However, scaling down of the transistor threshold voltage V_t results in significant increase in the subthreshold leakage current.

Figure 1[12] shows a four bit full adder. Four full adders are cascaded in a chain, each of them has its C_{out} connected to C_{in} of the following one. The Carry signal propagates through the whole chain. The Full adder performs in the propagation mode when the input signals $X \neq Y$ which makes $C_{out} = C_{in}$. The overall worst case delay is obtained when all the Full Adders operate in the propagation mode in a chain, and the carry signal has to propagate from the first to the last full adder in the chain. Thus Carry propagation path is the most critical path when an addition of more than two bits is desired, which makes it a speed limiting factor for many high speed applications.

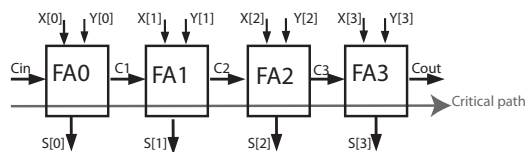


Figure 1: Four Bits Full Adder.

Floating-Gate (FG) gates have been proposed for Ultra-Low-Voltage (ULV) and Low-Power (LP)

logic [3]. However, in modern CMOS technologies there are significant gate leakages which undermine non-volatile FG circuits. FG gates implemented in a modern CMOS process require frequent initialization to avoid significant leakage. By using floating capacitances, either poly-poly, MOS or metal-metal, to the transistor gate terminals, the semi-floating-gate (SFG) nodes can have a different DC level than provided by the supply voltage headroom [3]. There are several approaches to FG CMOS logic [4, 5]. The gates proposed in this paper are influenced by ULV non-volatile FG circuits [6].

In this paper, we are focused on implementing Ultra-Low-Voltage (ULV) and high speed NP Domino carry gates. In Section II, an extended description of the NP Domino ULV inverter [8] is given. Conventional ULV carry gates are presented in Section III. In Section IV, different implementations of ULV carry gates are presented using pass transistor logic [10]. Simulation results are given in Section V and a conclusion is given in Section VI.

II High speed and Ultra-low-voltage Domino and semi-floating-gate NP domino Inverter

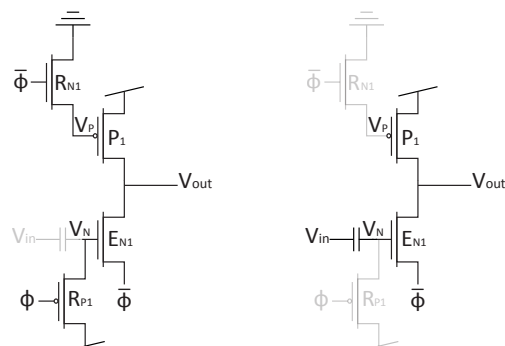
The ULV logic carry gates presented in this paper are related to the ULV domino logic style presented in [8], [9]. The main purpose of the ULV logic style is to increase the current level for low supply voltages without increasing the transistor widths. We may increase the current level compared to complementary CMOS using different initialization voltages to the gates and applying capacitive inputs. The extra load represented by the floating capacitors are less than extra load given by increased transistor widths. The capacitive inputs lower the delay through increased transconductance while increased transistor widths only reduce parasitic delay.

The High speed and ULV domino inverter represented in [8] is shown in Figure 2. The clock signals ϕ and $\bar{\phi}$ are used both as control signals for the recharge transistors R_{P1} and R_{N1} , and as reference signals for nMOS evaluation transistor E_{N1} . When ϕ switches from 1 to 0, the circuit is in precharge/recharge phase. During the precharge phase, R_{P1} turns on and recharges the gate of E_{N1} to 1. Meanwhile $\bar{\phi}$ switches from 0 to 1 which turns on R_{N1} and recharges the gate of pMOS transistor P_1 to 0. Thus both E_{N1} and P_1 turn on in the precharge phase and precharge the output node V_{out} to V_{dd} . Figure 2a is describing the precharge mode of this circuit. The gray shaded lines indicate the components which are not operating in

the precharge mode.

In the evaluation phase, clock signals ϕ and $\bar{\phi}$ switch from 0 to 1 and 1 to 0 respectively. Both recharge transistors R_{P1} and R_{N1} switch off which make the charge on nodes V_p and V_n to be floating as indicated by the gray shadow lines shown in Figure 2b. The output node V_{out} floats as well until we get a transition on the input node. The input signal V_{in} must be *monotonically rising* to ensure the correct operation for the N type type domino inverter. This can only be satisfied if

- input signal V_{in} is low at the beginning of the evaluation phase, and
- V_{in} only makes a single transition from 0 to 1 in the evaluation phase.



(a) Precharge Mode.

(b) Evaluate Mode.

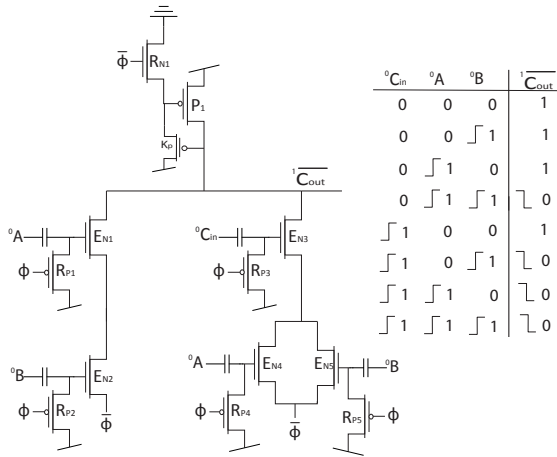
Figure 2: NP domino inverter in a) precharge phase and b) evaluate phase.

III Ultra-low-voltage and semi-floating-gate NP domino Carry circuit

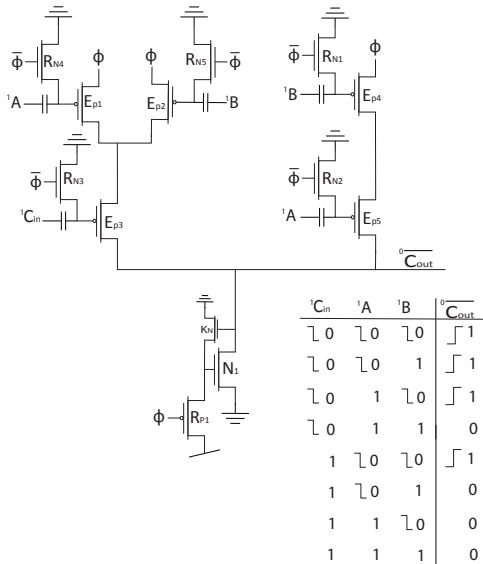
Different NP domino logical gates implemented in [9] operate at a very low supply voltage, and result in a really fast switching speed. Thus the *carry function* circuit can be implemented using the same logic style which can increase the propagation speed of the *carry bit* in a serial chain of cascaded full adders shown in Figure 1. C_{out} logic function of a Full Adder is shown in Equation 1 which concludes that C_{out} generates an *AND* functionality for the adding bits A and B as far

as C_{in} is 0. With the arrive of C_{in} bit, C_{out} generates an *OR* functionality for A and B .

$$C_{out} = A \cdot B + C_{in} \cdot (A + B) \quad (1)$$



(a) Precharge to 1 (N type).



(b) Precharge to 0 (P type).

Figure 3: ULV domino Carry Gates I (CARRY1).

Two ULV domino Carry gates are shown in Figure 3. The output node $\overline{C_{out}}$ in Figure 3a and 3b is precharged to 1 and 0 respectively. The CARRY gate has been implemented by combining ULV domino *Nand* and *Nor* gates implemented in [9] together

with a control signal C_{in} . C_{in} ascertains whether the output node gives a *Nand* or *Nor* functionality for the input bits A and B . A desired ULV domino inverter implemented in [8] should be connected at the output node of the implemented circuit to obtain C_{out} . This means that the output node $\overline{C_{out}}$ of a N type ULV domino carry gate should be connected to a P type ULV domino inverter to obtain a desired C_{out} .

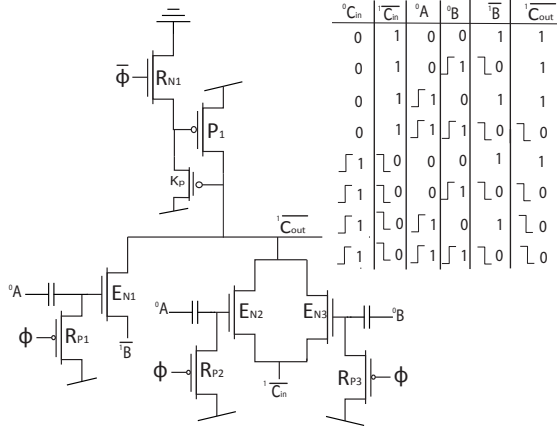
In order to retain the precharged value for the implemented Carry gates until the desired input bits arrive, the evaluation transistors P_1 to V_{DD} , or N_1 to GND should be made stronger than the other evaluation transistors. By applying an additional pMOS transistor K_P and nMOS transistor K_N in Figure 3a and 3b respectively, the gate of the evaluation transistors P_1 and N_1 will be pulled to V_{DD} and GND respectively when the output node $\overline{C_{out}}$ gets a transition in the evaluation phase which turns on the keeper transistors. This partially turns off the evaluation transistors P_1 and N_1 and let the output node $\overline{C_{out}}$ swings fully to V_{DD} and GND respectively. This helps to increase the noise margin and the robustness of the dynamic output node.

V_{DD}	CARRY1	CMOS	Deviation	Comment
300mV	54ps	4.72ns	4.2mV	Precharge to 1
300mV	153ps	3.7ns	7.6mV	Precharge to 0
300mV	103.5ps	4.21ns	11.8mV	Average

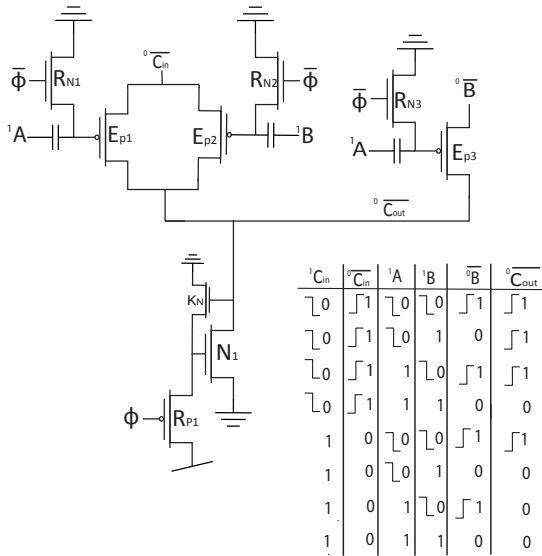
Table I: The speed and deviation for the Carry gate I compared to static CMOS Carry gate.

IV ULV NP domino Carry circuit using PTL

The same logic function can be obtained by using fewer number of transistors with the help of *Pass Transistor logic* (PTL) as compared to the conventional style, which reduces the overall delay of the system and saves the area on the chip. Circuits implemented in Figure 4 shows ULV NP domino Carry gates with the help of PTL. As compared to the carry gate implemented in Figure 3, the total number of evaluation transistors labelled E have been reduced from 5 to 3. The carry input bit needs only to pass through a single evaluation transistor before reaching the output node.



(a) Precharge to 1 (N type).



(b) Precharge to 0 (P type).

Figure 4: ULV domino Carry Gates using PTL II (CARRY2).

In Figure 4, the evaluation transistors labelled E can be described as pass transistors with an increased current level. If we consider the circuit in Figure 4a. As far as C_{in} is low, the output node $\overline{{}^1C_{out}}$ only switches from 1 to 0 when the evaluate transistor E_{N1} acts as a pass transistor for the input signal $\overline{{}^1B}$ when $\overline{{}^1B}$ switches from 1 to 0 and the other input 0A switches from 0 to 1 in the evaluation phase. When the C_{in} bit becomes high, only one of the two evaluation pass transistors E_{N2} or E_{N3} needs to turn on to

pull the output node $\overline{{}^1C_{out}}$ from 1 to 0. This implies that E_{N2} or E_{N3} acts as pass transistor for input $\overline{{}^1C_{in}}$ when $\overline{{}^1C_{in}}$ switches from 1 to 0 and at least one of the two other inputs 0A or 0B switches from 0 to 1.

V_{DD}	CARRY2	CMOS	Deviation	Comment
300mV	28.5ps	4.72ns	4.2mV	Precharge to 1
300mV	261ps	3.7ns	7.6mV	Precharge to 0
300mV	144.75ps	4.21ns	11.8mV	Average

Table II: The speed and deviation for the Carry gate II compared to static CMOS Carry gate.

Another alternative solution of ULV domino NP Carry gate using PTL is implemented in Figure 5. N type Carry gate in Figure 5a resembles the Carry gate implemented in Figure 4a. Both circuits perform entirely in the same sense as far as ${}^0C_{in}$ is logically 0. When ${}^0C_{in}$ switches from 0 to 1 in the evaluation phase, both parallel connected evaluation transistors E_{N2} or E_{N3} turn on and act as pass transistors for the inputs $\overline{{}^1A}$ and $\overline{{}^1B}$. Under this instance, only one of the two inputs $\overline{{}^1A}$ or $\overline{{}^1B}$ requires to switch from 1 to 0 to pull the output node $\overline{{}^1C_{out}}$ to 0.

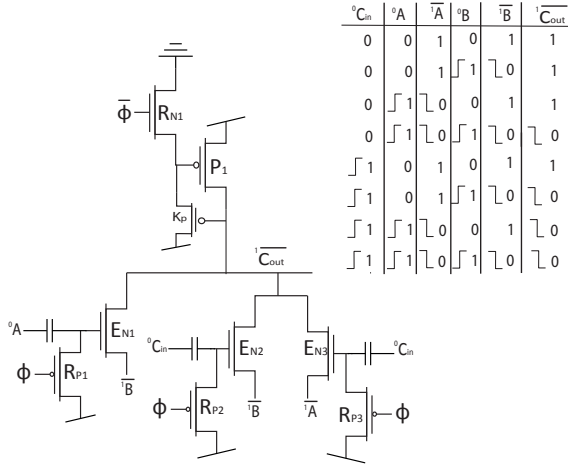
V_{DD}	CARRY3	CMOS	Deviation	Comment
300mV	99.4ps	4.72ns	10.65mV	Precharge to 1
300mV	411ps	3.7ns	30.5mV	Precharge to 0
300mV	255.2ps	4.21ns	20.5mV	Average

Table III: The speed and deviation for the Carry gate III compared to static CMOS Carry gate.

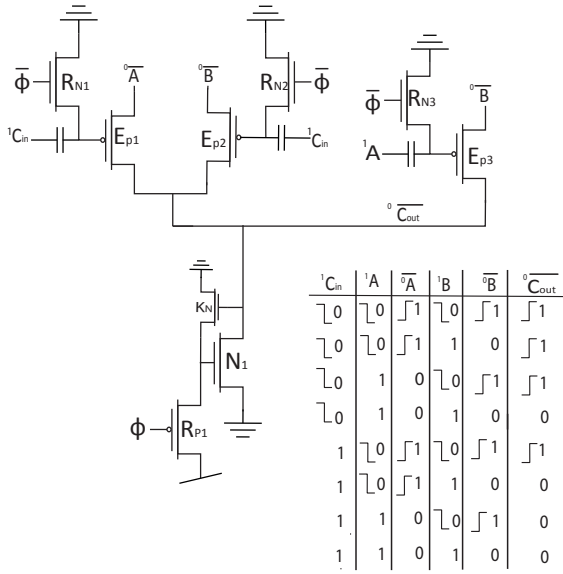
V Simulated Response

The data simulated is based on a 90nm TSMC CMOS process and the load applied is an identical gate for each logic style. The simulated response of different ULV carry gate circuits implemented in Figure 3, 4 and 5 are shown in Table I, II and III respectively. The implemented carry gates are directly target to a supply voltage of 300mV. The presented gates are compared to static CMOS carry gate at the same supply voltage. The Tables are showing both the delay and noise margin, for the implemented ULV carry gates compared to static CMOS Carry gate.

Table IV is showing a summary of the average relative delay of the presented ULV carry gates as compared to a static CMOS carry gates at a supply voltage of 300mV. CARRY1 is the fastest carry gate at a supply voltage of 300mV. Relative to the static CMOS carry gate in[11], the delay of the implemented ULV carry gates are between 2.45% and



(a) Precharge to 1 (N type).



(b) Precharge to 0 (P type).

Figure 5: ULV domino Carry Gates using PTL III (CARRY3).

	CARRY1	CARRY2	CARRY3
RelativeDelay(%)	2.45%	3.4%	6.06%

Table IV: The relative delay of ULV carry gates at a supply voltage of 300mV as compared to static CMOS carry gate.

6.06%. CARRY3 is slowest and less preferable due to low noise margin, as both parallel connected evaluation transistors E_{N2} or E_{N3} turn on in the worst case scenario, while only one of the two inputs 1A or ${}^1\bar{B}$ switches from 1 to 0. Thus both 0 and 1 is being transferred through the evaluation pass transistors, which makes the output transition slow and gives poor noise margin. However, it offers a more efficient solution in terms of area.

Plots in Figure 6 and 7 show the delay and Energy Delay Product (EDP) for the proposed carry gates relative to static CMOS carry gate presented in[11] respectively. The delay is lesser than 5% as compared to static CMOS carry gate for CARRY1 and CARRY2 for the supply voltages less than 325mV as shown in Figure 6. The CARRY2 gate gives the least relative delay of about 2% relative to static CMOS carry gate at the supply voltage of 250mV.

Average EDP of implemented ULV carry gates relative to static CMOS carry gate is shown in Figure 7. The simulation results conclude that the EDP is less than 1% for all presented ULV carry gates for the the supply voltage less than 325mV relative to static CMOS carry gate. CARRY2 gives the least average EDP relative to static CMOS carry gate with a value close to 0.02% at a supply voltage of 250mV.

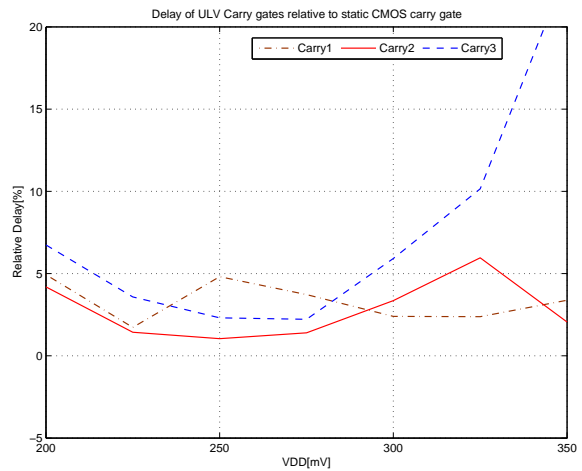


Figure 6: Delay of ULV carry gates relative to static CMOS carry gate.

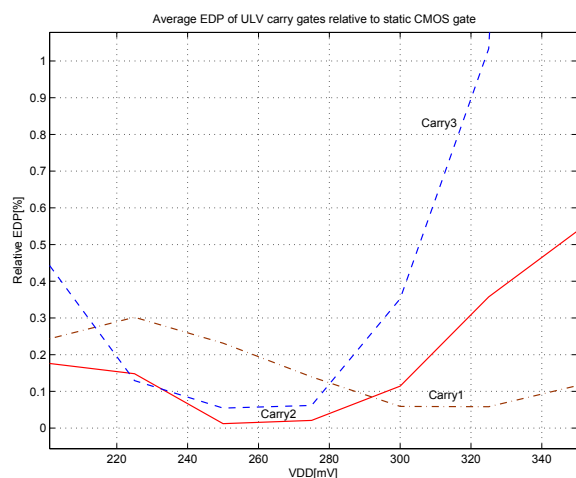


Figure 7: Average EDP of ULV carry gates relative to static CMOS carry gate.

VI Conclusion

Different ultra low-voltage NP domino Carry gates have been presented in this paper. The ULV domino carry gates are high speed, i.e. the delay compared to a static CMOS carry gate is less than 5% for a supply voltage equal to $325mV$. The energy delay product of the proposed ULV carry gates is less than 1% relative to the static CMOS carry gate when the circuits operate at a supply voltage below the threshold voltage of the transistors. The ULV carry gates can be used to design high speed and low voltage Full adders without applying parallel design which reduces both the power and the area.

References:

- [1] Chandrakasan A.P. Sheng S. Brodersen R.W.: "Low-power CMOS digital design", *IEEE Journal of Solid-State Circuits*, Volume 27, Issue 4, April 1992 Page(s):473 - 484
- [2] Verma N. Kwong J. Chandrakasan A.P.: "Nanometer MOSFET Variation in Minimum Energy Subthreshold Circuits", *IEEE Transactions on Electron Devices*, Vol. 55, NO. 1, January 2008 Page(s):163 - 174
- [3] Y. Berg, D. T. Wisland and T. S. Lande: "Ultra Low-Voltage/Low-Power Digital Floating-Gate Circuits", *IEEE Transactions on Circuits and Systems*, vol. 46, No. 7, pp. 930–936, July 1999.
- [4] K. Kotani, T. Shibata, M. Imai and T. Ohmi. "Clocked-Neuron-MOS Logic Circuits Employing Auto-Threshold-Adjustment", *In IEEE International Solid-State Circuits Conference (ISSCC)*, pp. 320-321,388, 1995.
- [5] T. Shibata and T. Ohmi. "A Functional MOS Transistor Featuring Gate-Level Weighted Sum and Threshold Operations", *In IEEE Transactions on Electron Devices*, vol 39, 1992.
- [6] Y. Berg, Tor S. Lande and Ø. Næss. "Programming Floating-Gate Circuits with UV-Activated Conductances", *IEEE Transactions on Circuits and Systems -II: Analog and Digital Signal Processing*, vol 48, no. 1, pp 12-19, 2001.
- [7] Y. Berg "Novel Ultra Low-Voltage and High Speed Domino CMOS Logic", *In proc. IEEE/IFIP International Conference on VLSI and system-on-Chip (VLSI-SoC)*, Madrid 27-29 september 2010.
- [8] Y. Berg and O.Mirmotahari "Ultra Low-Voltage and High Speed Dynamic and Static Precharge Logic", *In proc. of the 11th Edition of IEEE Faible Tension Faible Consommation*, June 6-8, 2012, Paris, France.
- [9] Y. Berg and O.Mirmotahari. "Novel High-Speed and Ultra-Low-Voltage CMOS NAND and NOR Domino Gates", *In proc. of the 5th international Conference on Advances in Circuits, Electronics and Micro-electronics*, August 19-24, 2012, Rome, Italy.
- [10] Y. Berg and M.Azadmehr. "Novel Ultra Low-Voltage and High-Speed CMOS Pass Transistor Logic", *In proc. of the 11th Edition of IEEE Faible Tension Faible Consommation*, June 6-8, 2012, Paris, France.
- [11] Neil H.E. and David Harris. "CMOS VLSI DESIGN, A circuit and Systems Perspective", *Third edition, Addison Wesley 2005*, p 640.
- [12] M.Alioto and G.Palumbo. "Very High-Speed Carry Computation based on Mixed Dynamic/Transmission-Gate Full Adders", *In proc. of the 18th European Conference on Circuit Theory and Design*, August 27-30, 2007, Sevilla, Spain.
- [13] Y. Berg "Ultra Low Voltage Static Carry Generate Circuit", *In Proc. IEEE International Symposium on Circuits and Systems (ISCAS)*, Paris, May 2010.
- [14] Y. Berg: "Static Ultra Low Voltage CMOS Logic", *In Proc. IEEE NORCHIP Conference*, Trondheim, NORWAY, November 2009.

Paper II

Static NP Domino Carry gates for Ultra Low Voltage and High Speed Full Adders

Submitted to International Journal of Circuits, Systems and Signal Processing: North Atlantic University Union (NAUN).

Static NP Domino Carry gates for Ultra Low Voltage and High Speed Full Adders

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Abstract—In this paper we present different configurations of static ULV NP domino carry gates using precharge and pass transistor logic. The proposed ULV domino carry gates are aimed for high speed serial adders in ultra low-voltage applications. In terms of frequency, speed, PDP and EDP, the ULV carry gates offers significant improvement compared to conventional CMOS carry gate. At Minimum Energy Point at $250mV$, the proposed carry gates have less than 5% of the delay than the conventional CMOS Carry gate. Furthermore, the Power and Energy Delay Product is less than 23% and 1% respectively relative to conventional CMOS Carry gate at the same supply voltage. The simulated data presented is obtained using a $90nm$ TSMC CMOS process.

Index Terms—Low-Voltage, High-Speed, Carry gate, NP Domino Logic, Precharge, CMOS, Digital, Pass Transistor Logic.

I. INTRODUCTION

In recent years, the power problem has emerged as one of the fundamental limits facing the future of CMOS integrated circuit design. The aggressive scaling of device dimensions to achieve greater transistor density and circuit speed results in substantial sub-threshold and gate oxide tunnelling leakage currents. Energy-efficiency is one of the most required features for modern electronic systems designed for high-performance and/or portable applications. In one hand, the ever increasing market segment of portable electronic devices demands the availability of low-power building blocks that enable the implementation of long-lasting battery-operated systems. On the other hand, the general trend of increasing operating frequencies and circuit complexity, in order to cope with the throughput needed in modern high-performance processing applications, requires the design of very high-speed circuits.

Depending upon the application, there are numerous methods that can be used to reduce the power consumption of VLSI circuits, these can range from low-level measures based upon fundamental physics, such as using a lower power supply voltage or using high threshold voltage transistors; to high-level measures such as clock-gating or power-down modes. The power consumption in digital circuits, which mostly use complementary metal-oxide semiconductor (CMOS) devices, is proportional to the square of the power supply voltage[1]; therefore, voltage scaling is one of the important methods used to reduce power consumption. To achieve a high transistor drive current

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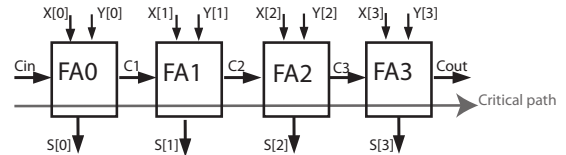


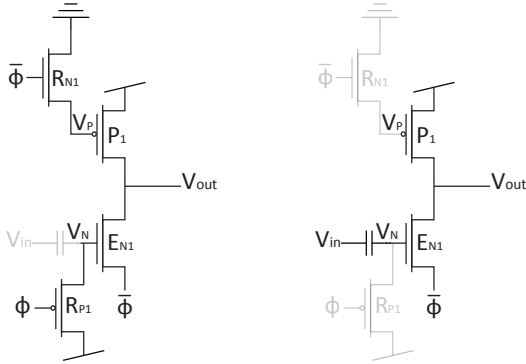
Fig. 1: Four Bits Full Adder.

and thereby improve the circuit performance, the transistor threshold voltage must be scaled down in proportion to the supply voltage. However, scaling down of the transistor threshold voltage V_t results in significant increase in the sub-threshold leakage current.

Figure 1[2] shows a four bit full adder. Four full adders are cascaded in a chain, each of them has its C_{out} connected to C_{in} of the following one. The Carry signal propagates through the whole chain. The Full adder performs in the propagation mode when the input signals $X \neq Y$ which makes $C_{out} = C_{in}$. The overall worst case delay is obtained when all the Full Adders operate in the propagation mode in a chain, and the carry signal has to propagate from the first to the last full adder in the chain. Thus Carry propagation path is the most critical path when an addition of more than two bits is desired, which makes it a speed limiting factor for many high speed applications. By using complex carry look ahead techniques or applying parallel structures, the delay can be reduced compared to a simple serial adder shown in Figure 1 at the cost of increased complexity, power consumption and chip area.[3]

Floating-Gate (FG) gates have been proposed for Ultra-Low-Voltage (ULV) and Low-Power (LP) logic [4]. However, in modern CMOS technologies there are significant gate leakages which undermine non-volatile FG circuits. FG gates implemented in a modern CMOS process require frequent initialization to avoid significant leakage. By using floating capacitances, either poly-poly, MOS or metal-metal, to the transistor gate terminals, the semi-floating-gate (SFG) nodes can have a different DC level than provided by the supply voltage headroom [4]. There are several approaches for both analog and digital applications using FG CMOS logic proposed in [5], [6], [7], [8]. The gates proposed in this paper are influenced by ULV non-volatile FG circuits [9].

In this paper, we are focused on implementing Ultra-



(a) Precharge Phase. (b) Evaluate Phase.

Fig. 2: NP domino inverter in a) precharge phase and b) evaluate phase.

Low-Voltage (ULV) and high speed NP Domino carry gates. In Section II, an extended description of the NP Domino ULV inverter [10] is given. Conventional ULV carry gates are presented in Section III. In Section IV, different implementations of ULV carry gates are presented using pass transistor logic [13]. Simulation results are given in Section V and a conclusion is given in Section VI.

II. HIGH SPEED AND ULTRA-LOW-VOLTAGE FLOATING-GATE NP DOMINO INVERTER

The ULV logic carry gates presented in this paper are related to the ULV domino logic style presented in [10], [11], [12]. The main purpose of the ULV logic style is to increase the current level for low supply voltages without increasing the transistor widths. We may increase the current level compared to complementary CMOS using different initialization voltages to the gates and applying capacitive inputs. The extra load represented by the floating capacitors are less than extra load given by increased transistor widths. The capacitive inputs lower the delay through increased transconductance while increased transistor widths only reduce parasitic delay. The proposed logic style may be used in critical high speed and low voltage sub circuits together with conventional CMOS logic.

The High speed and ULV N domino inverter represented in [10] is shown in Figure 2. The clock signals ϕ and $\bar{\phi}$ are used both as control signals for the recharge transistors R_{P1} and R_{N1} , and as reference signals for nMOS evaluation transistor E_{N1} . The recharge and the evaluation phase of the proposed logic style is characterized below:

A. Precharge/Recharge phase

When ϕ switches from 1 to 0, the circuit is in precharge/recharge phase. During this phase, R_{P1} turns on

and recharges the gate of E_{N1} to 1. Meanwhile $\bar{\phi}$ switches from 0 to 1 which turns on R_{N1} and recharges the gate of pMOS transistor P_1 to 0. Thus both E_{N1} and P_1 turn on in the precharge phase and precharge the output node V_{out} to V_{dd} . Figure 2a shows the precharge mode of this circuit. The gray shaded lines indicate the components which are not operating in the precharge mode.

B. Evaluation phase

In the evaluation phase, clock signals ϕ and $\bar{\phi}$ switch from 0 to 1 and 1 to 0 respectively. Both recharge transistors R_{P1} and R_{N1} switch off which make the charge on nodes V_p and V_n to be floating as indicated by the gray shadow lines shown in Figure 2b. The output node V_{out} floats as well until an input transition occurs. The input signal V_{in} must be *monotonically rising* to ensure the correct operation for the N domino inverter. This can only be satisfied if

- input signal V_{in} is low at the beginning of the evaluation phase, and
- V_{in} only makes a single transition from 0 to 1 in the evaluation phase.

As V_{in} makes a positive transition, the capacitance at the gate of E_{N1} charges and discharges. The charge at node V_N can be estimated by using Equation (1). We assume that the initial charge at the node is V_{dd} , V_{in} is charged upto V_{dd} as well. The capacitive division will be $\frac{1}{2}$ if C_{in} and $C_{parasitic}$ assume to be equal. This makes the voltage at the gate terminal V_N $1.5 \times$ higher than the voltage supplied by the supply voltage V_{dd} [4]. Thus evaluation transistor E_{N1} strongly biased which increases the current level of the transistor. Thus Pull Down Network (PDN) becomes much stronger than PUN and discharges the output node V_{out} to 0.

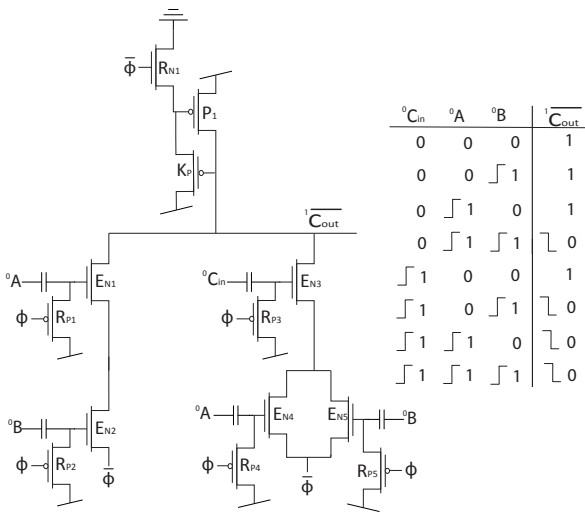
$$V_N = V_{init} + \Delta V_{in} * \frac{C_{in}}{C_{in} + C_{parasitic}} \quad (1)$$

III. ULTRA-LOW-VOLTAGE AND SEMI-FLOATING-GATE NP DOMINO CARRY CIRCUIT

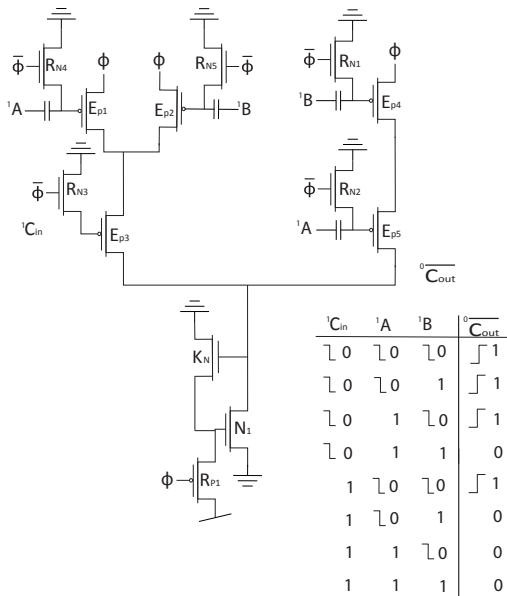
Different NP domino logical gates are presented in [11] which operate in the sub-threshold regime and result in a really fast switching speed. The CARRY circuit can be implemented using the same logic style which can increase the propagation speed of the *carry bit* in a serial chain of cascaded full adders shown in Figure 1. C_{out} logic function of a Full Adder is shown in Equation 2 which concludes that C_{out} generates an *AND* functionality for the adding bits A and B as far as C_{in} is 0. With the arrive of C_{in} bit, C_{out} generates an *OR* functionality for A and B .

$$C_{out} = A \cdot B + C_{in} \cdot (A + B) \quad (2)$$

Two ULV domino Carry gates are shown in Figure 3. The output node $\overline{C_{out}}$ in Figure 3a and 3b is precharged to 1 and 0 respectively. The CARRY gate has been implemented by combining ULV domino *Nand* and *Nor* gates implemented in [11] together with a control signal C_{in} . C_{in}



(a) Precharge to 1 (N type).



(b) Precharge to 0 (P type).

Fig. 3: ULV domino Carry Gates I (CARRY1).

ascertains whether the output node gives a *Nand* or *Nor* functionality for the input bits A and B . A desired ULV domino inverter implemented in [10] should be connected at the output node of the implemented circuit to obtain C_{out} . This means that the output node $\overline{C_{out}}$ of a N type ULV domino carry gate should be connected to a P type ULV domino inverter to obtain a desired C_{out} .

In order to retain the precharged value for the implemented Carry gates until the desired input bits arrive, the evaluation transistors P_1 to V_{DD} , or N_1 to GND should be made stronger than the other evaluation transistors. By applying an additional pMOS transistor K_P and nMOS transistor K_N in Figure 3a and 3b respectively, the gate

of the evaluation transistors P_1 and N_1 will be pulled to V_{DD} and GND respectively when the output node $\overline{C_{out}}$ gets a transition in the evaluation phase which turns on the keeper transistors. This partially turns off the evaluation transistors P_1 and N_1 and let the output node $\overline{C_{out}}$ swings fully to V_{DD} and GND respectively. This helps to reduce the static current which matches the OFF current I_{off} in the conventional CMOS inverter. The Noise Margin NM is defined in Equation 3.

$$NM = \frac{I_{on}}{I_{off}} \quad (3)$$

Thus, by adding keepers, improves both the noise margin and the power consumption of the proposed circuits.

IV. ULV NP DOMINO CARRY CIRCUIT USING PTL

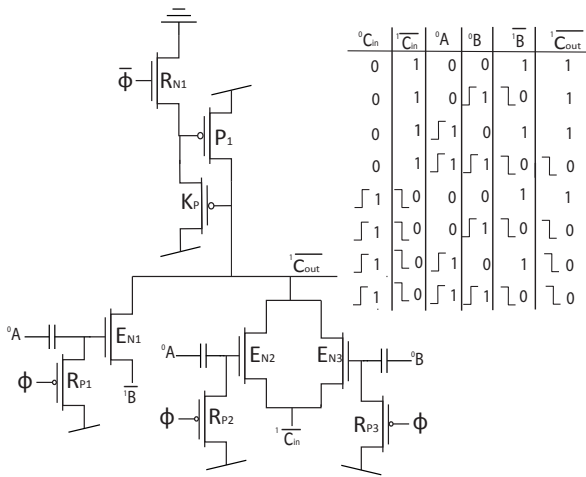
The same logic function can be obtained by using fewer number of transistors with the help of *Pass Transistor logic* (PTL) as compared to the conventional style, which reduces the overall delay of the system and saves the area on the chip. Circuits implemented in Figure 4 shows ULV NP domino Carry gates with the help of PTL. As compared to the carry gate implemented in Figure 3, the total number of evaluation transistors labelled E have been reduced from 5 to 3. The carry input bit needs only to pass through a single evaluation transistor before reaching the output node.

In Figure 4, the evaluation transistors labelled E can be described as pass transistors with an increased current level. If we consider the circuit in Figure 4a. As far as C_{in} is low, the output node $\overline{C_{out}}$ only switches from 1 to 0 when the evaluate transistor E_{N1} acts as a pass transistor for the input signal $\overline{1B}$ when $\overline{1B}$ switches from 1 to 0 and the other input 0A switches from 0 to 1 in the evaluation phase. When C_{in} bit becomes high, only one of the two evaluation pass transistors E_{N2} or E_{N3} needs to turn on to pull the output node $\overline{1C_{out}}$ from 1 to 0. This implies that E_{N2} or E_{N3} acts as pass transistor for input $\overline{1C_{in}}$ when $\overline{1C_{in}}$ switches from 1 to 0 and at least one of the two other inputs 0A or 0B switches from 0 to 1.

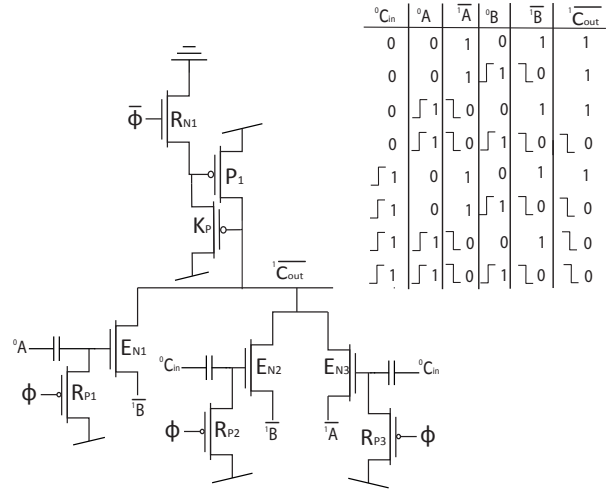
Another alternative solution of ULV domino NP Carry gate using PTL is implemented in Figure 5. N type Carry gate in Figure 5a resembles the Carry gate implemented in Figure 4a. Both circuits perform entirely in the same sense as far as ${}^0C_{in}$ is logically 0. When ${}^0C_{in}$ switches from 0 to 1 in the evaluation phase, both parallel connected evaluation transistors E_{N2} or E_{N3} turn on and act as pass transistors for the inputs $\overline{1A}$ and $\overline{1B}$. Under this instance, only one of the two inputs $\overline{1A}$ or $\overline{1B}$ requires to switch from 1 to 0 to pull the output node $\overline{1C_{out}}$ to 0.

V. SIMULATED RESPONSE

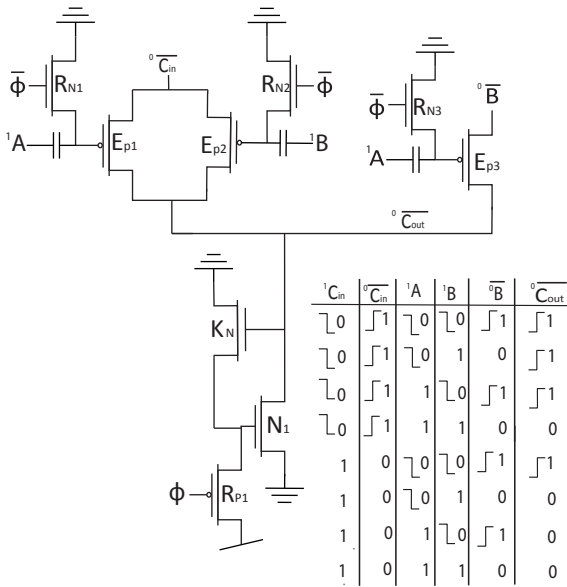
The data simulated is based on a 90nm TSMC CMOS process. To avoid underestimation of the implemented circuits and to obtain more realistic waveforms, clock signals have been made by inserting two symmetric conventional CMOS inverters between the ideal voltage sources and the clock signals. In the same way, input signals have been



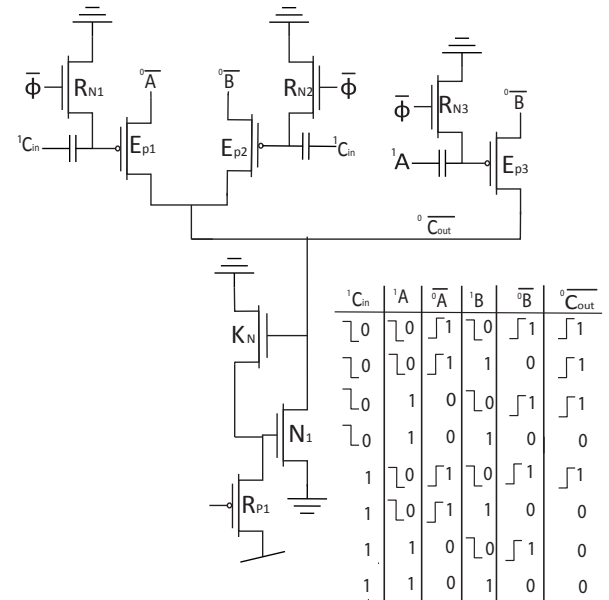
(a) Precharge to 1 (N type).



(a) Precharge to 1 (N type).



(b) Precharge to 0 (P type).



(b) Precharge to 0 (P type).

Fig. 4: ULV domino Carry Gates using PTL II (CARRY2).

Fig. 5: ULV domino Carry Gates using PTL III (CARRY3).

made by inserting ULV domino inverters implemented in [10] between the voltage sources and the input nodes. An identical gate for each logic style is applied as load at the output nodes of all circuits. The proposed ULV domino carry gates are simulated for the worst case scenario where only one of the two input bits are high and the and the carry signal has to propagate through the full adder.

The performance of the proposed ULV domino carry gates implemented in Figure 3, 4 and 5 are shown in Table I. The implemented carry gates are directly target to operate in the sub-threshold regime. The presented gates are compared with the conventional CMOS carry gate[14] at the same supply voltages. Table I demonstrates speed performance, together with power consumption and other figure of merits

(PDP and EDP) in order to optimize the *Minimum Energy Point* MEP for the proposed ULV domino Carry gates comparable with conventional CMOS carry gate.

The power consumed by the clock drivers are not included and must be taken into consideration for each specific application. Besides this, the Table also presents the operating limits of clock frequency which changes rapidly as the supply voltage varies. In Table I, the style labelled *N Carry* and *P Carry* represents the proposed N and P type domino carry gates respectively. *Avg* represents the average delay or power between the proposed *N* and *P* type domino carry gates.

The average propagation delay between N and P type

Style	Comment	100mV	150mV	200mV	250mV	300mV	350mV	400mV
CLK	f_{clk} (MHz)	0.83	2.5	8.3	16.67	66.67	83.3	125
Conventional Carry	Delay (ns)	328	101	25.4	10.4	2.56	1.55	0.782
	Power (nW)	0.008145	0.055	0.34	1.12	6.83	10.35	23
	PDP (10^{-18} J)	2.672	5.55	8.64	11.65	17.48	16.04	17.97
	EDP (10^{-27} J/s)	876.4	560.5	219.5	121	44.75	24.9	14.05
N Carry 1 P Carry 1 Carry 1	Delay (ns)	53	18.74	2.49	0.318	0.162	0.05	0.022
	Delay (ns)	194	36.83	2.75	0.38	0.19	0.109	0.1086
	Avg.Delay (ns)	123.5	27.785	2.62	0.349	0.176	0.0795	0.0653
	Relative delay (%)	37.65	27.52	10.31	3.36	6.88	5.11	8.36
	Avg.Power (nW)	0.0358	0.3078	1.907	7.55	41.1	100.8	265
	Avg.PDP (10^{-18} J)	4.423	8.552	4.996	2.635	7.234	8.014	17.305
	Relative PDP (%)	165	154	57.8	22.6	41.4	50	96.3
	Avg.EDP (10^{-27} J/s)	546.4	237.6	13.1	0.919	1.273	0.637	1.13
N Carry 2 P Carry 2 Carry 2	Delay (ns)	141.5	25.38	3.07	0.4127	0.183	0.0725	0.04516
	Delay (ns)	92.06	11.72	1.26	0.2976	0.166	0.1375	0.333
	Avg.Delay (ns)	116.8	18.5	2.165	0.35	0.1745	0.105	0.189
	Relative delay (%)	35.61	18.32	8.52	3.36	6.82	6.77	24.18
	Avg.Power (nW)	0.01867	0.209	1.461	5.21	28.45	56.9	137
	Avg.PDP (10^{-18} J)	2.181	3.86	3.16	1.823	4.96	5.97	25.9
	Relative PDP (%)	81.6	69.55	36.57	15.65	28.37	37.22	144.13
	Avg.EDP (10^{-27} J/s)	254.7	71.41	6.84	0.638	0.865	0.627	4.897
N Carry 3 P Carry 3 Carry 3	Delay (ns)	141.5	22.5	3.35	0.475	0.22	0.092	0.0715
	Delay (ns)	265.7	31.1	2.75	0.504	0.248	0.182	0.883
	Avg.Delay (ns)	203.6	26.8	3.05	0.489	0.234	0.137	0.477
	Relative delay (%)	62.07	26.53	12	4.7	9.14	8.84	61
	Avg.Power (nW)	0.01948	0.245	1.572	5.47	30.75	71.15	176.5
	Avg.PDP (10^{-18} J)	3.96	6.58	4.79	2.68	7.19	9.747	84.235
	Relative PDP (%)	148.4	117.35	55.1	23.01	41.15	60.57	468
	Avg.EDP (10^{-27} J/s)	807.5	176.4	14.63	1.312	1.684	1.335	40.2
	Relative EDP (%)	92.1	31.14	6.62	1.08	3.76	5.34	286

TABLE I: Performance of ULV domino Carry gates compared to complementary CMOS Carry gate at different supply voltages.

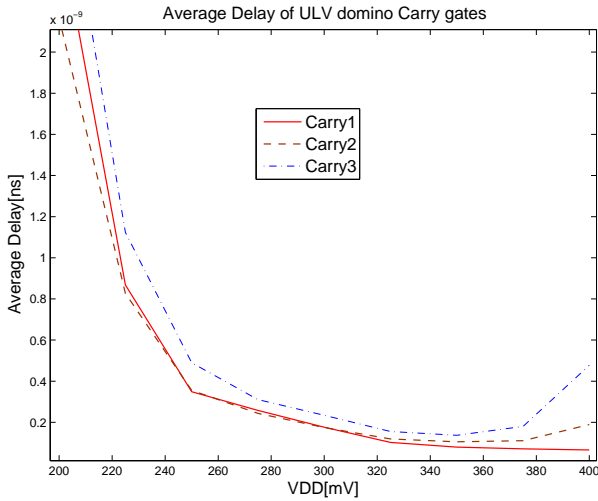


Fig. 6: Average Delay of ULV domino carry gates for different supply voltages.

Carry gates for the proposed ULV domino logic style is shown in Figure 6. The delay is in ns for the supply voltages under $225mV$ and decreases exponentially as the supply voltage increases. Beyond $300mV$, the propagation delay is only in the range of tens of ps . CARRY 1 and CARRY 2 contributes almost equal delay when the supply voltage is within $220mV$ and 320 . Under $220mV$, CARRY 2 provides

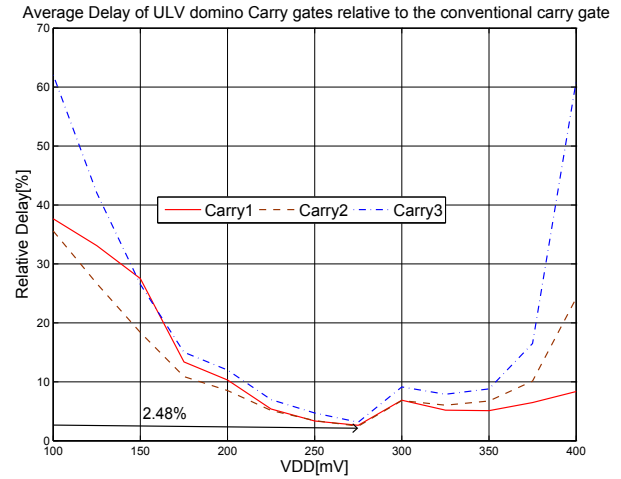


Fig. 7: Delay of ULV carry gates relative to conventional CMOS carry gate for different supply voltages.

minimum propagation delay. On the other hand, CARRY 1 gives minimum delay when the supply voltage exceeds over $320mV$.

CARRY 3 is the slowest and less preferable in high speed applications due to low noise margin, as both parallel connected evaluation transistors E_{N2} or E_{N3} turn on in the worst case scenario, while only one of the two inputs $\overline{1A}$ or $\overline{1B}$ switches from 1 to 0. Thus both $\overline{1A}$ and $\overline{1B}$

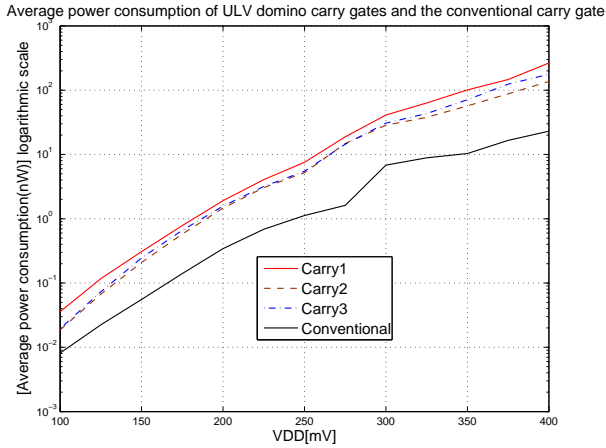


Fig. 8: Average power consumption per ULV carry gate compared to conventional CMOS carry gate.

simultaneously contends at the output node, which makes the output transition slow and gives poor noise margin. However, it offers a more efficient solution in terms of area and power consumption as compared to CARRY 1.

The average delay between N and P type Carry gates for the proposed ULV domino logic style is compared with the conventional CMOS Carry gate in Figure 7. The relative delay is lesser than 20% for all the proposed domino carry gates when the supply voltage varies between $175mV$ and $375mV$. The overall best relative delay is achieved by using ULV domino carry gate proposed in Figure 4 which is obtained by using pass transistor logic. The reason is because the input carry bit only needs to propagate through a single evaluation transistor to reach the output node. Compared to conventional carry gate, the least average delay is achieved at the supply voltage of $275mV$, where CARRY2 only utilizes a delay of 2.48%.

The average power consumption per ULV domino carry gate is compared with conventional CMOS carry gate in Figure 8. The total power consumption per gate increases with supply voltage. As expected the power consumption for the ULV domino carry gates exceeds the power consumption of the conventional CMOS carry gate, giving the advantage of really fast speed. As shown in Figure 8, ULV domino carry gates using pass transistor logic (PTL) contributes minimum power consumption than the domino carry gate implemented in Figure 3. This happens as the total number of evaluation transistors reduces from 5 to 3 by using PTL which consumes less power in the evaluation phase.

The average energy of the ULV domino carry gates relative to conventional CMOS carry gate for different supply voltages is shown in Figure 9. The *Power Delay Product* PDP for the proposed ULV carry gates is lower than the conventional carry gate for the supply voltage between $175mV$ and $350mV$. This is mainly caused due to very reduced delay for the proposed carry gates relative to the conventional carry gate.

Comparing the graphs in Figure 7 and 9 concludes that

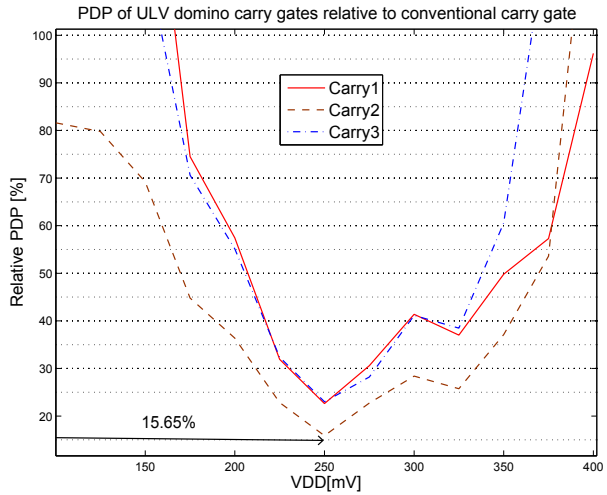


Fig. 9: Average relative energy of ULV domino carry gates.

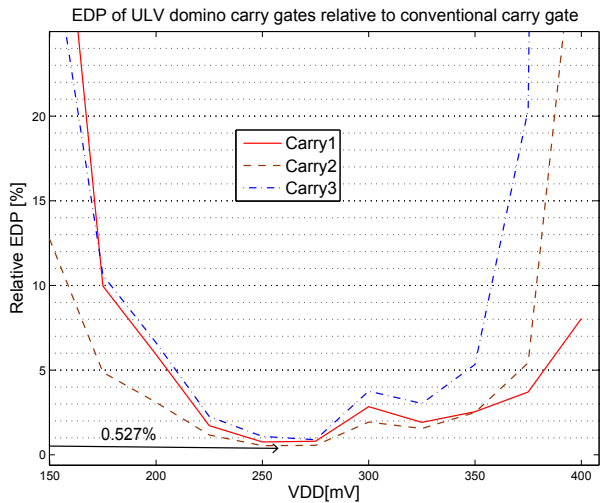


Fig. 10: Average relative energy delay product of ULV domino carry gates.

minimum relative PDP corresponds to the maximum relative speed for the proposed carry gates. All three proposed ULV domino carry gates have the minimum relative PDP of lower than 25% at the supply voltage of $250mV$, which makes it the Minimum Energy Point. CARRY 2 is the most efficient solution as it only contributes 15.65% PDP relative to conventional Carry gate. As the supply voltage reduces below $175mV$, the relative PDP for CARRY 1 and CARRY 3 exceeds 100% while the relative PDP of CARRY 2 is still beyond the PDP of conventional Carry gate. However, the relative PDP of CARRY 2 becomes worse than CARRY 1 as the supply voltage exceeds $375mV$.

The relative Energy Delay Product EDP for the ULV domino carry gates for different supply voltages is shown in Figure 10. The relative EDP for all the proposed ULV domino carry gates is lesser than 30% for the supply voltage between $175mV$ and $375mV$ which directly corresponds to the same supply voltage range where the PDP is minimum

	CARRY1	CARRY2	CARRY3
Relative Delay(%)	3.36	3.36	4.7
Relative PDP(%)	22.6	15.65	23.01
Relative EDP(%)	0.76	0.527	1.08

TABLE II: The delay, PDP and EDP of ULV domino carry gates at Minimum Energy Point (250mV) relative to conventional CMOS carry gate.

as shown in Figure 9.

At Minimum Energy point (250mV), the EDP of all proposed ULV carry gates is lower than 1.5% relative to a conventional carry gate. However, CARRY 2 is characterized by least relative EDP with a value closer to 0.527% at 275mV. The relative EDP of CARRY 2 is far better than the other solutions at the supply voltage under 175mV, but becomes worse than CARRY 1 as the supply voltage increases beyond 375mV.

Table II is showing a summary of delay, PDP and EDP of proposed ULV domino carry gates relative to conventional CMOS carry gate at Minimum Energy Point with a supply voltage of 250mV. CARRY 1 and CARRY 2 have the same relative delay of 3.36% thus both solutions are efficient for ultra low voltage and high speed applications. However for low power applications, CARRY 2 is the most efficient solution as it consumes less power than the other two ULV carry gates and results in lower PDP and EDP. CARRY 3 is the slowest and less preferable for high speed applications, but it offers a more efficient solution than CARRY 1 in terms of area and power.

VI. CONCLUSION

Different ultra low-voltage NP domino Carry gates have been presented in this paper. The ULV domino carry gates are high speed, i.e. the delay compared to conventional CMOS carry gate is less than 5% for a supply voltage equal to 250mV. The power and energy delay product of the proposed ULV carry gates is less than 23% and 1% relative to conventional CMOS carry gate respectively at minimum energy point. Both power and area can be saved if we can avoid using parallel adders by applying ULV domino carry gates when ultra low voltage solutions are preferable. In this manner we may take the advantage of the speed improvement and the reduction of power and area.

REFERENCES

- [1] Chandrakasan A.P. Sheng S. Brodersen R.W.: "Low-power CMOS digital design", *IEEE Journal of Solid-State Circuits*, Volume 27, Issue 4, April 1992 Page(s):473 - 484
- [2] M.Alioto and G.Palumbo. "Very High-Speed Carry Computation based on Mixed Dynamic/Transmission-Gate Full Adders", *In proc. of the 18th European Conference on Circuit Theory and Design*, August 27-30, 2007, Sevilla, Spain.
- [3] Y. Berg and O.Mirmotahari. "Static Differential Ultra Low-Voltage Domino CMOS logic for High Speed Applications.", *North atlantic university union: International Journal of Circuits, Systems and Signal Processing*. ISSN 1998-4464. 6(4), s 269- 274
- [4] Y. Berg, D. T. Wisland and T. S. Lande: "Ultra Low-Voltage/Low-Power Digital Floating-Gate Circuits", *IEEE Transactions on Circuits and Systems*, vol. 46, No. 7, pp. 930-936, July 1999.
- [5] K. Kotani, T. Shibata, M. Imai and T. Ohmi. "Clocked-Neuron-MOS Logic Circuits Employing Auto-Threshold-Adjustment", *In IEEE International Solid-State Circuits Conference (ISSCC)*, pp. 320-321, 388, 1995.
- [6] T. Shibata and T. Ohmi. "A Functional MOS Transistor Featuring Gate-Level Weighted Sum and Threshold Operations", *In IEEE Transactions on Electron Devices*, vol 39, 1992.
- [7] Y. Berg and M.Azadmehr. "A band-tunable auto-zeroing amplifier", *Proceedings of the WSEAS conferences*, ISSN 1790-5117. 3(CSCS 12), s 24- 28.
- [8] Y. Berg and M.Azadmehr. "A bi-directional auto-zeroing floating-gate amplifier.", *Proceedings of the 10th WSEAS conference*, ISBN 978-1-61804-062-6. s 70 - 75
- [9] Y. Berg, Tor S. Lande and Ø. Næss. "Programming Floating-Gate Circuits with UV-Activated Conductances", *IEEE Transactions on Circuits and Systems -II: Analog and Digital Signal Processing*, vol 48, no. 1, pp 12-19, 2001.
- [10] Y. Berg and O.Mirmotahari "Ultra Low-Voltage and High Speed Dynamic and Static Precharge Logic", *In proc. of the 11th Edition of IEEE Faible Tension Faible Consommation*, June 6-8, 2012, Paris, France.
- [11] Y. Berg and O.Mirmotahari. "Novel High-Speed and Ultra-Low-Voltage CMOS NAND and NOR Domino Gates", *In proc. of the 5th international Conference on Advances in Circuits, Electronics and Micro-electronics*, August 19-24, 2012, Rome, Italy.
- [12] Y. Berg and O.Mirmotahari. "Novel Static Ultra Low-Voltage and High Speed CMOS Boolean Gates", *North atlantic university union: International Journal of Circuits, Systems and Signal Processing*. ISSN 1998-4464. 6(4), s 249- 254.
- [13] Y. Berg and M.Azadmehr. "Novel Ultra Low-Voltage and High-Speed CMOS Pass Transistor Logic", *In proc. of the 11th Edition of IEEE Faible Tension Faible Consommation*, June 6-8, 2012, Paris, France.
- [14] Neil H.E. and David Harris. "CMOS VLSI DESIGN, A circuit and Systems Perspective", *Third edition, Addison Wesley 2005*, p 640.
- [15] Y. Berg "Ultra Low Voltage Static Carry Generate Circuit", *In Proc. IEEE International Symposium on Circuits and Systems (ISCAS)*, Paris, may 2010.
- [16] Y. Berg: "Static Ultra Low Voltage CMOS Logic", *In Proc. IEEE NORCHIP Conference*, Trondheim, NORWAY, november 2009.

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Paper III

Ultra-Low Voltage and High Speed NP Domino Carry Propagation chain

*Submitted at 2013 IEEE Faible Tension Faible Consommation (FTFC)
conference, Paris, France, June 20-21, 2013.*

Ultra-Low Voltage and High Speed NP Domino Carry Propagation chain

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Abstract—In this paper, an Ultra Low Voltage NP domino logic style is presented to perform a 32 bit computation in a carry propagation chain. The presented logic style is targeted to operate at the supply voltages in the sub-threshold regime. Simulated results of 32-bit proposed carry chain compared to the conventional carry chain show that the proposed approach offers a superb improvement in terms of speed and EDP. The proposed carry chain has a relative delay and EDP of only 2.68% and 8% respectively compared to the conventional carry chain. The 32-bit ULV NP domino carry chain using 90nm TSMC CMOS process technology with a supply voltage of 300mV could be operated on a clock frequency of 50MHz.

I. INTRODUCTION

In recent years, low voltage digital CMOS becomes more and more attractive, due to the general advances in process technology and due to the low power applications. The aggressive scaling of device dimensions and supply voltage in order to achieve greater transistor density and low power consumption results in degradation in the speed of the logic circuits due to reduced effective input voltage to the transistors. In one hand, the ever increasing market segment of portable electronic devices demands the availability of low-power building blocks that enable the implementation of long-lasting battery-operated systems. On the other hand, the general trend of increasing operating frequencies and circuit complexity, in order to cope with the throughput needed in modern high-performance processing applications, requires the design of very high-speed circuits.

Low voltage does not necessarily imply low power; the power consumed by a gate is proportional to the active current driving the output of the gate. Hence, delay and power consumption are both dependent on the current and the energy or power delay product (PDP) is not significantly dependent on the current. The energy required to toggle a bit is more dependent on the load and configuration of the gate. Energy delay product (EDP) is more dependent on speed than on power and will be improved by increasing the current for a specific supply voltage. The optimal supply voltage for CMOS logic in terms of EDP is close to the threshold voltage of the nMOS transistor V_{tn} for a specific process, assuming that the threshold voltage of the pMOS transistor V_{tp} is approximately equal to $-V_{tn}$ [1]. Several approaches to high speed and low voltage digital CMOS circuits have been presented [2].

A Full Adder is one of the most critical components of a processor as it is used in ALU, the floating point unit an address generation in case of cache or memory accesses[3]. Besides the addition task, it is also nucleus to many other arithmetic operations such as subtraction, multiplication, division etc. In a typical serial adder, the critical delay is affected by the carry propagation. The two bit Full adder operates in the propagation mode when only one of the the input signals is high and the *carry* signal has to propagate through the full adder. This makes the carry propagation path a speed limiting factor for many high speed applications. By using complex carry look ahead techniques or applying parallel structures, the delay can be reduced compared to a simple serial adder at the cost of increased complexity, power consumption and chip area. Thus improving the speed performance of serial adders at Ultra low supply voltages has been of a continuous interest.

Floating-Gate (FG) gates have been proposed for Ultra-Low-Voltage (ULV) and Low-Power (LP) logic [4]. FG logic implemented in a modern CMOS process require frequent initialization to avoid significant leakage. By using floating capacitances to the transistor gate terminals, the semi-floating-gate (SFG) nodes can have a different DC level than provided by the supply voltage headroom [4]. There are several approaches for both analog and digital applications using FG CMOS logic proposed in [5], [6], [7], [8]. The gates proposed in this paper are influenced by ULV non-volatile FG circuits [9].

A ULV and high speed serial carry chain has been presented [10] using a simple dynamic ULV logic. In In this paper, we exploit ULV and high speed NP Domino carry gates[11] in a 32-bit serial chain. In Section II, an extended description of the NP Domino ULV inverter [12] is given. An ULV NP domino 2 bit carry gate is presented in Section III. Simulation results are shown in Section IV and a conclusion is given in Section V.

II. HIGH SPEED AND ULTRA-LOW-VOLTAGE NP DOMINO INVERTER

The ULV domino carry gate presented in this paper is related to the ULV domino logic style presented in [12], [13], [14]. The main purpose of the ULV logic style is to increase the current level for the transistors at low

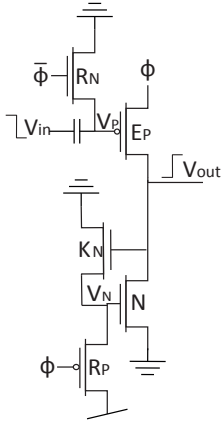


Fig. 1: ULV P type domino inverter (Precharge to 0).

supply voltages without increasing the transistor widths. We may increase the current level compared to complementary CMOS using different initialization voltages to the gates and applying capacitive inputs. The extra load represented by the floating capacitors is less than the extra load given by increased transistor widths. The capacitive inputs lower the delay through increased transconductance while increased transistor widths only reduce the parasitic delay. The proposed logic style may be used in critical high speed and low voltage full adders together with the conventional CMOS logic.

The High speed and ULV P type domino inverter represented in [12] is shown in Figure 1. The clock signals ϕ and $\bar{\phi}$ are used both as control signals for the recharge transistors R_P and R_N , and as reference signals for pMOS evaluation transistor E_P . The recharge/precharge and the evaluation phase for the proposed logic style is characterized below:

A. Precharge/Recharge phase

When ϕ switches from 1 to 0, the circuit becomes in the precharge/recharge phase. During this phase, R_P turns on and recharges the gate of N transistor to 0. Meanwhile $\bar{\phi}$ switches from 0 to 1 which turns on R_N and recharges the gate of E_P to 0. Thus both evaluation transistors N and E_P turn on and precharge the output node V_{out} to gnd . The keeper transistor K_N is inactive during this phase as the output node is precharged to 0.

B. Evaluation phase

In the evaluation phase, clock signals ϕ and $\bar{\phi}$ switch from 0 to 1 and 1 to 0 respectively. Both recharge transistors R_P and R_N switch off which make the charge on gate terminals V_p and V_n floating. The output node V_{out} floats as well until an input transition occurs. The input signal V_{in} must be *monotonically falling* to ensure the correct operation for the P type domino inverter. This can only be satisfied if

- input signal V_{in} is high at the beginning of the evaluation phase, and
- V_{in} only makes a single transition from 1 to 0 in the evaluation phase.

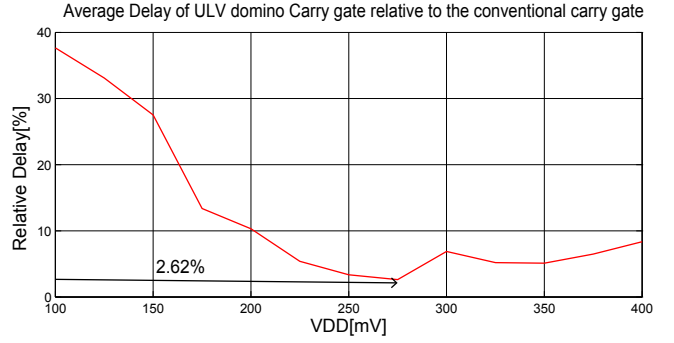


Fig. 2: Delay of ULV NP domino carry gate relative to standard CMOS carry gate.

K_N turns on when the output node gets a positive transition in the evaluation phase. This partially turns off the evaluation transistor N and let the output node swings fully to gnd . This helps to reduce the static current which directly impacts on the noise margin and the power consumption for the proposed logic.

III. TWO BIT ULV NP DOMINO CARRY GATE

Different implementations of ULV NP domino Carry gates are presented in [11] which operate in the sub-threshold regime and result in a really superb speed performance. The proposed NP domino carry gates offer an average propagation delay below 5% relative to the conventional CMOS carry gate[15] at a supply voltage of $275mV$. A two bit ULV NP domino carry gate shown in Figure 3 is based on one of the NP domino carry gates presented in [11]. The propagation average speed for the proposed ULV carry gate compared to standard CMOS carry gate[15] for different supply voltages is shown in Figure 2. The average maximum speed is achieved at a supply voltage of $275mV$ where the delay is only 2.62% relative to conventional CMOS carry gate.

Table I demonstrates speed performance, together with power consumption and other figure of merits (PDP and EDP) in order to optimize the *Minimum Energy Point* MEP for the proposed ULV domino carry gate comparable with conventional CMOS carry gate at different supply voltages.

The left carry gate (N type) in Figure 3 resembles an N type ULV domino inverter presented in [12]. The output nodes $\overline{C_{out}[0]}$ and $\overline{C_{out}[1]}$ precharges to 1 and 0 respectively in the precharge phase. In the evaluation phase, the output nodes remain floating holding the precharged value until the accurate inputs arrive. In order to retain the precharged value, the evaluation transistors P to V_{DD} , or N to gnd should be made stronger than the other evaluation transistors. Different techniques have been suggested in [16] to increase the strength of MOS transistors in the subthreshold regime. The circuit response to different configurations in the evaluation phase is described below:

- 1) If the inputs signal A and B gets a positive transition prior to C_{in} in the N type carry gate, the evaluation

Style	Comment	200mV	225mV	250mV	275mV	300mV	325mV	350mV	375mV	400mV
CLK	f_{clk} (MHz)	8.3	12.5	16.67	33.33	66.67	71.4	83.3	100	125
Conventional Carry	Delay (ns)	25.4	16.1	10.4	9.83	2.56	1.97	1.55	1.09	0.782
	Power (nW)	0.34	0.69	1.12	1.61	6.83	8.88	10.35	16.56	23
	PDP (10^{-18} j)	8.64	11.12	11.65	15.83	17.48	17.49	16.04	18.05	17.97
	EDP (10^{-27} js)	219.5	179	121	155.6	44.75	34.4	24.9	19.7	14.05
N type Carry	Delay (ns)	2.49	0.827	0.318	0.245	0.162	0.075	0.05	0.035	0.022
P type Carry	Delay (ns)	2.75	0.909	0.38	0.271	0.19	0.129	0.109	0.106	0.1086
NP Carry	Avg.Delay (ns)	2.62	0.868	0.349	0.258	0.176	0.102	0.0795	0.0707	0.0653
	Avg.Power (nW)	1.907	4.057	7.55	18.8	41.1	63.3	100.8	146.4	265
	Avg.PDP (10^{-18} j)	4.996	3.52	2.635	4.85	7.234	6.47	8.014	10.36	17.305
	Avg.EDP (10^{-27} js)	13.1	3.05	0.919	1.25	1.273	0.662	0.637	0.733	1.13
Relative (%)	Delay	10.31	5.40	3.36	2.62	6.88	5.19	5.11	6.48	8.36
	PDP	57.8	31.9	22.6	30.59	41.4	37	50	57.3	96.3
	EDP	5.97	1.72	0.76	0.8	2.84	1.92	2.56	3.71	8.04

TABLE I: Performance of ULV NP domino Carry gate compared to complementary CMOS Carry gate at different supply voltages.

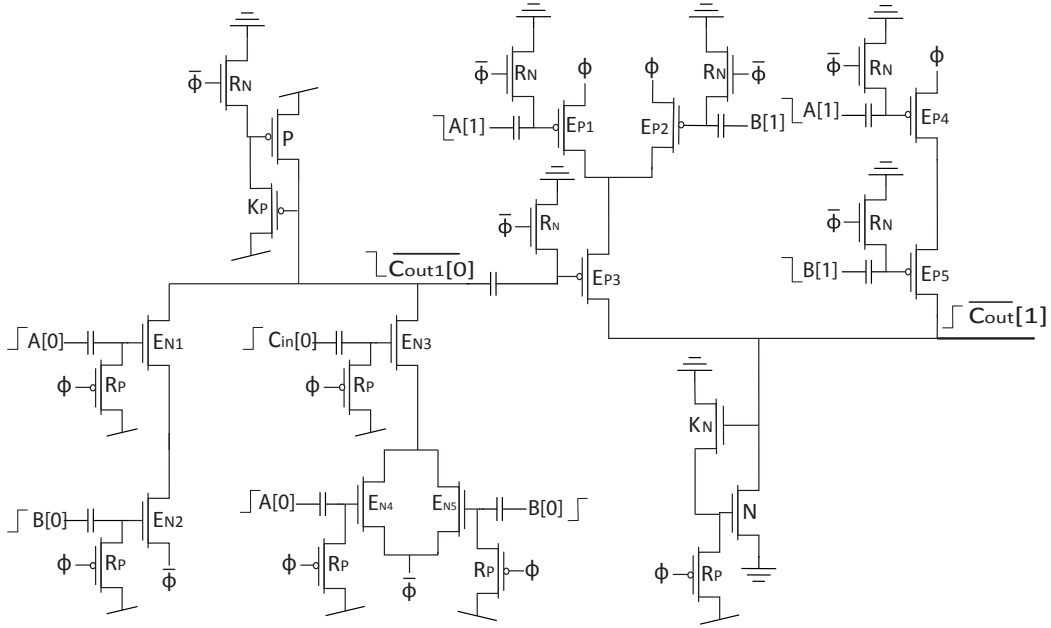


Fig. 3: A two bit ULV NP domino carry gate.

transistors E_{N1} and E_{N2} turn on as the active current is larger due to the boost of the evaluation transistors. Thus the output node pulls down to 0. The P type carry gate operates in the same way but the input signals get a negative transition. This is the best case scenario as the carry bit does not propagate in the domino chain and all the output nodes get a transition when both nput signals arrive prior to the carry signal.

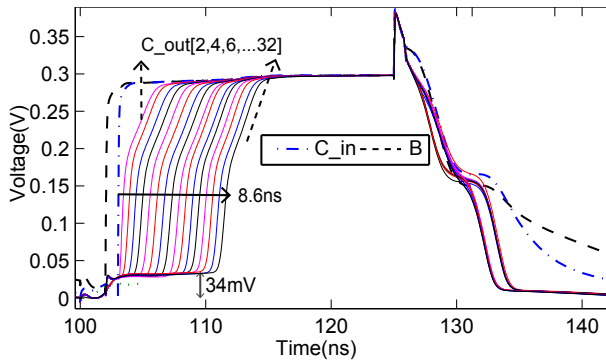
- Assuming the worst case scenario when only one of the two inputs get a transition which turn on one of the two parallel connected evaluation transistors E_{N4} or E_{N5} in N type, the output node will retain the precharged value until the carry input signal arrives. When the carry input signal arrives, E_{N3} turn on making the path from V_{DD} to gnd which pulls down the output node to 0. Furthermore, negative transition at $\overline{C_{out}[0]}$ turn on the

E_{P3} pulling the output node to 1 if one of the two input signals $A[1]$ or $B[1]$ get a negative transition. In this way, the carry signal propagates through the NP domino carry gates in the worst case scenario.

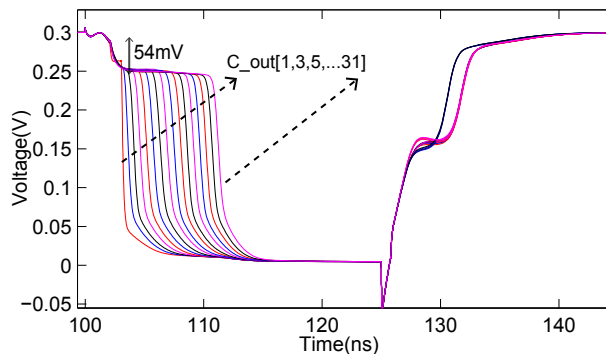
IV. SIMULATION RESULTS

The data simulated is based on a 90nm TSMC CMOS process. To avoid underestimation of the implemented circuits and to obtain more realistic waveforms, clock signals have been made by inserting two symmetric conventional CMOS inverters between the ideal voltage sources and the clock signals. In the same way, input signals for ULV domino carry gates have been made by inserting ULV domino inverters implemented in [12] between the voltage sources and the input nodes.

Graph in Figure 4 shows the simulated results of the 32 bit carry chain. 16 two bit NP domino carry gates implemented



(a) Output nodes from P Type carry gates.



(b) Output nodes from N Type carry gates.

Fig. 4: Simulated response of a 32-bit carry chain implemented in Figure 3.

in Figure 3 are cascaded together to make a 32 bit carry chain. The proposed ULV domino carry gates are simulated at the supply voltage of $300mV$ and by considering the worst case scenario where only one of the two input bits get a transition in every ULV domino carry gate and the carry input signal propagates through a 32 bit carry chain.

The propagation delay of the proposed carry chain is far less than the delay of the conventional CMOS carry gate[15]. Conventional carry gate has a propagation delay of approximately $321ns$ at the same supply voltage whereas the proposed ULV domino requires only $8.6ns$ to propagate from 1 to 32 bit. The simulated response also demonstrates that the logic level of different carry signals are very close to the rails after the transition, offering a robust design with a better noise margin. The floating output nodes of P and N type carry gates are pulled slightly towards 1 and 0 respectively before the carry input signal arrives. This problem can be eliminated by increasing the strength of the evaluation transistors labelled N and P offering a low static power consumption at the cost of slightly degradation in speed performance.

V. CONCLUSION

In this paper we have presented a 32 bit ULV NP domino carry chain which is simulated for the worst case scenario. The proposed ULV carry gates are used to achieve a very fast carry computation, offering a superb speed feature, i.e.

the delay compared to the conventional CMOS carry chain is only 2.68% for a supply voltage of $300mV$ with almost no degradation in the robustness and the area. The energy delay product *EDP* for the proposed ULV domino carry chain is approximately 8% relative to the conventional CMOS carry chain at the same supply voltage. The clock signal necessitates only a period of $20ns$ to execute an addition of 32 bits. ULV NP domino carry gates can be used to save power and area compared to parallel designed adders for ultra low voltage and high speed applications.

REFERENCES

- [1] Chandrakasan A.P. Sheng S. Brodersen R.W.: "Low-power CMOS digital design" , *IEEE Journal of Solid-State Circuits*, Volume 27, Issue 4, April 1992 Page(s):473 - 484
- [2] Verma N. Kwong J. Chandrakasan A.P.: "Nanometer MOSFET Variation in Minimum Energy Subthreshold Circuits" , *IEEE Transactions on Electron Devices*, Vol. 55, NO. 1, January 2008 Page(s):163 - 174
- [3] A. Wang, A.P. Chandrakasan, S.V. Kosonocky: "Optimal supply and threshold scaling for subthreshold CMOS circuits" , *Proc. of IEEE Computer Society Annual Symposium on VLSI*, 2002, pp. 5-9.
- [4] Y. Berg, D. T. Wisland and T. S. Lande: "Ultra Low-Voltage/Low-Power Digital Floating-Gate Circuits" , *IEEE Transactions on Circuits and Systems*, vol. 46, No. 7, pp. 930-936, July 1999.
- [5] K. Kotani, T. Shibata, M. Imai and T. Ohmi. "Clocked-Neuron-MOS Logic Circuits Employing Auto-Threshold-Adjustment" , *In IEEE International Solid-State Circuits Conference (ISSCC)*, pp. 320-321, 388, 1995.
- [6] T. Shibata and T. Ohmi. " A Functional MOS Transistor Featuring Gate-Level Weighted Sum and Threshold Operations" , *In IEEE Transactions on Electron Devices*, vol 39, 1992.
- [7] Y. Berg and M.Azadmehr. "A band-tunable auto-zeroing amplifier" , *Proceedings of the WSEAS conferences*, ISSN 1790-5117. 3(CSCS 12), s 24- 28.
- [8] Y. Berg and M.Azadmehr. "A bi-directional auto-zeroing floating-gate amplifier." , *Proceedings of the 10th WSEAS conference*, ISBN 978-1-61804-062-6. s 70 - 75
- [9] Y. Berg, Tor S. Lande and Ø. Næss. "Programming Floating-Gate Circuits with UV-Activated Conductances" , *IEEE Transactions on Circuits and Systems -II: Analog and Digital Signal Processing*, vol 48, no. 1, pp 12-19, 2001.
- [10] Y. Berg "Ultra Low Voltage Static Carry Generate Circuit" , *In Proc. IEEE International Symposium on Circuits and Systems (ISCAS)*, Paris, May 2010.
- [11] S.M. Mahmood and Y.Berg. "High Speed and Ultra Low-voltage CMOS Domino Carry gates" , *In proc. of the 12th WSEAS Conference on Electronics, Hardware, Wireless and Optical Communications*, ISBN 978-1-61804-164-7. s 52 - 57
- [12] Y. Berg and O.Mirmotahari "Ultra Low-Voltage and High Speed Dynamic and Static Precharge Logic" , *In proc. of the 11th Edition of IEEE Faible Tension Faible Consommation*, June 6-8, 2012, Paris, France.
- [13] Y. Berg and O.Mirmotahari. "Novel High-Speed and Ultra-Low-Voltage CMOS NAND and NOR Domino Gates" , *In proc. of the 5th international Conference on Advances in Circuits, Electronics and Micro-electronics*, August 19-24, 2012, Rome, Italy.
- [14] Y. Berg and O.Mirmotahari. "Novel Static Ultra Low-Voltage and High Speed CMOS Boolean Gates" , *North atlantic university union: International Journal of Circuits, Systems and Signal Processing*. ISSN 1998-4464. 6(4), s 249- 254.
- [15] Neil H.E. and David Harris. "CMOS VLSI DESIGN, A circuit and Systems Perspective" , *Third edition, Addison Wesley 2005*, p 640.
- [16] M. Alioto. "Impact of NMOS/PMOS imbalance in Ultra-Low Voltage CMOS standard cells" , *Circuit Theory and Design (ECCTD)*, 2011 20th European Conference on , vol., no., pp.536,539, 29-31 Aug. 2011

Bibliography

- [1] A.P. Chandrakasan, S. Sheng, and R.W. Brodersen. Low-power CMOS digital design. *Solid-State Circuits, IEEE Journal of*, 27(4):473–484, apr 1992. ISSN 0018–9200. doi: 10.1109/4.126534.
- [2] N. Verma, J. Kwong, and A.P. Chandrakasan. Nanometer MOSFET variation in Minimum Energy Subthreshold Circuits. *Electron Devices, IEEE Transactions on*, 55(1):163–174, 2008. ISSN 0018–9383. doi: 10.1109/TED.2007.911352.
- [3] Kimiyoshi Usami and Mark Horowitz. Clustered voltage scaling technique for low-power design. In *Proceedings of the 1995 international symposium on Low power design*, pages 3–8. ACM, 1995.
- [4] S. Mutoh, T. Douseki, Y. Matsuya, T. Aoki, S. Shigematsu, and J. Yamada. 1-V power supply high-speed digital circuit technology with multithreshold-voltage cmos. *Solid-State Circuits, IEEE Journal of*, 30(8):847–854, 1995. ISSN 0018–9200. doi: 10.1109/4.400426.
- [5] T. Shibata and T. Ohmi. A functional mos transistor featuring gate-level weighted sum and threshold operations. *Electron Devices, IEEE Transactions on*, 39(6):1444–1455, 1992. ISSN 0018–9383. doi: 10.1109/16.137325.
- [6] Paul Hasler, Chris Diorio, Bradley A Minch, and Carver Mead. Single transistor learning synapses. *Advances in neural information processing systems*, pages 817–826, 1995.
- [7] Bradley A Minch, Chris Diorio, Paul Hasler, and Carver A Mead. Translinear circuits using subthreshold floating-gate MOS transistors. *Analog Integrated Circuits and Signal Processing*, 9(2):167–179, 1996.
- [8] P. Hasler, B.A. Minch, and C. Diorio. Adaptive circuits using pFET floating-gate devices. In *Advanced Research in VLSI, 1999. Proceedings. 20th Anniversary Conference on*, pages 215–229, 1999. doi: 10.1109/ARVLSI.1999.756050.
- [9] Y. Berg, D.T. Wisland, and T.S. Lande. Ultra low-voltage/low-power digital floating-gate circuits. *Circuits and Systems II: Analog and Digital Signal Processing, IEEE Transactions on*, 46(7):930–936, jul 1999. ISSN 1057–7130. doi: 10.1109/82.775389.

- [10] Y. Berg, T.S. Lande, and O. Naess. Programming floating-gate circuits with UV-activated conductances. *Circuits and Systems II: Analog and Digital Signal Processing, IEEE Transactions on*, 48(1):12 –19, jan 2001. ISSN 1057 – 7130. doi: 10.1109/82.913182.
- [11] Y. Berg, S. Aunet, O. Minnotahari, and M. Hovin. Novel recharge semi-floating-gate CMOS logic for multiple-valued systems. In *Circuits and Systems, 2003. ISCAS '03. Proceedings of the 2003 International Symposium on*, volume 5, pages V–193–V–196 vol.5, 2003. doi: 10.1109/ISCAS.2003.1206229.
- [12] Y. Berg. Novel ultra low-voltage and high speed domino CMOS logic. In *VLSI System on Chip Conference (VLSI-SoC), 2010 18th IEEE/IFIP*, pages 225–228, 2010. doi: 10.1109/VLSISOC.2010.5642664.
- [13] K. Venkat, Liang Chen, I. Lin, P. Mistry, P. Madhani, and K. Sato. Timing verification of dynamic circuits. In *Custom Integrated Circuits Conference, 1995., Proceedings of the IEEE 1995*, pages 271 – –274, may 1995. doi: 10.1109/CICC.1995.518184.
- [14] P. Meher and K.K. Mahapatra. Ultra low-power and noise tolerant CMOS dynamic circuit technique. In *TENCON 2011 - 2011 IEEE Region 10th Conference*, pages 1175 –1179, nov. 2011. doi: 10.1109/TENCON.2011.6129297.
- [15] S. Mutoh, T. Douseki, Y. Matsuya, T. Aoki, and J. Yamada. 1V high-speed digital circuit technology with 0.5 μ m multi-threshold CMOS. In *ASIC Conference and Exhibit, 1993. Proceedings., Sixth Annual IEEE International*, pages 186–189, 1993. doi: 10.1109/ASIC.1993.410836.
- [16] T. Kuroda, T. Fujita, T. Nagamatu, S. Yoshioka, T. Sei, K. Matsuo, Y. Hamura, T. Mori, M. Murota, M. Kakumu, and T. Sakurai. A high-speed low-power 0.3 μ m cmos gate array with variable threshold voltage (VT) scheme. In *Custom Integrated Circuits Conference, 1996., Proceedings of the IEEE 1996*, pages 53–56, 1996. doi: 10.1109/CICC.1996.510510.
- [17] Neil H.E. and David Harris. *Integrated Circuit Design*, page 389. PEARSON, fourth edition, 2010.
- [18] M. Alioto. Ultra-Low Power VLSI Circuit Design Demystified and Explained: A Tutorial. *Circuits and Systems I: Regular Papers, IEEE Transactions on*, 59(1):3 –29, jan. 2012. ISSN 1549 – 8328. doi: 10.1109/TCSI.2011.2177004.
- [19] M. Anis, S. Areibi, and M. Elmasry. Design and optimization of multithreshold CMOS (MTCMOS) circuits. *Computer-Aided Design of Integrated Circuits and Systems, IEEE Transactions on*, 22(10): 1324–1342, 2003. ISSN 0278 – 0070. doi: 10.1109/TCAD.2003.818127.

- [20] M. Alioto. Impact of NMOS/PMOS imbalance in Ultra-Low Voltage CMOS standard cells. In *Circuit Theory and Design (ECCTD)*, 2011 20th European Conference on, pages 536 –539, aug. 2011. doi: 10.1109/ECCTD.2011.6043407.
- [21] Song Ye and Jun Li. The effects of a deep n-well junction on RF circuit performance. In *Junction Technology (IWJT)*, 2010 International Workshop on, pages 1 –4, may 2010. doi: 10.1109/IWJT.2010.5475012.
- [22] F. Assaderaghi, S. Parke, D. Sinitsky, J. Bokor, P.-K. Ko, and Chenming Hu. A dynamic threshold voltage MOSFET (DTMOS) for very low voltage operation. *Electron Device Letters, IEEE*, 15(12):510–512, 1994. ISSN 0741 – 3106. doi: 10.1109/55.338420.
- [23] P. Simonen, A. Heinonen, M. Kuulusa, and J. Nurmi. Comparison of bulk and SOI CMOS technologies in a DSP processor circuit implementation. In *Microelectronics*, 2001. ICM 2001 Proceedings. The 13th International Conference on, pages 107–110, 2001. doi: 10.1109/ICM.2001.997499.
- [24] P.F. Butzen and R.P. Ribas. Leakage Current in Sub-Micrometer CMOS Gates, http://www.inf.ufrgs.br/logics/docman/book_emicro_butzen.pdf.
- [25] H.J.M. Veendrick. Short-circuit dissipation of static CMOS circuitry and its impact on the design of buffer circuits. *Solid-State Circuits, IEEE Journal of*, 19(4):468 – 473, aug 1984. ISSN 0018 – 9200. doi: 10.1109/JSSC.1984.1052168.
- [26] X. Qi, S.C. Lo, A. Gyure, Y. Luo, M. Shahram, K. Singhal, and D.B. MacMillen. Efficient subthreshold leakage current optimization - Leakage current optimization and layout migration for 90- and 65- nm ASIC libraries. *Circuits and Devices Magazine, IEEE*, 22(5):39 –47, sept.-oct. 2006. ISSN 8755 – 3996. doi: 10.1109/MCD.2006.272999.
- [27] Neil H.E. and David Harris. *Integrated Circuit Design*, page 154. PEARSON, fourth edition, 2010.
- [28] M. Alioto and G. Palumbo. Very high-speed carry computation based on mixed dynamic/transmission-gate full adders. In *Circuit Theory and Design*, 2007. ECCTD 2007. 18th European Conference on, pages 799 –802, aug. 2007. doi: 10.1109/ECCTD.2007.4529717.
- [29] Y. Berg and M. Azadmehr. Novel ultra low-voltage and high-speed CMOS pass transistor logic. In *Faible Tension Faible Consommation (FTFC)*, 2012 IEEE, pages 1 –4, june 2012. doi: 10.1109/FTFC.2012.6231719.
- [30] S.M Mahmood and Y. Berg. High Speed and Ultra Low-voltage CMOS Domino Carry gates. In *12th WSEAS Conference on Electronics*,

Hardware, Wireless and Optical Communications, pages 52–57, 2013. doi: ISBN978-1-61804-164-7.

- [31] M. Alioto and G. Palumbo. Analysis and comparison on full adder block in submicron technology. *Very Large Scale Integration (VLSI) Systems, IEEE Transactions on*, 10(6):806 –823, dec. 2002. ISSN 1063 – 8210. doi: 10.1109/TVLSI.2002.808446.