The Conservation Multiplier

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Every government that controls an exhaustible resource must decide whether to exploit it or conserve it and thereby let the subsequent government decide whether to exploit or conserve. This paper develops a positive theory of this situation and shows when a small change in parameter values has a multiplier effect on exploitation. The multiplier strengthens the influence of a lobby paying for exploitation and of a donor compensating for conservation. A successful donor pays every period for each unit; a successful lobby pays once. This asymmetry causes inefficient exploitation. A normative analysis uncovers when compensations are optimally offered to the party in power, to the general public, or to the lobby.

I. Introduction

This paper presents a tractable dynamic game of resource exploitation between consecutive governments. The model is employed to illustrate how the conflicts between governments can be taken advantage of by a principal who prefers conservation or by a principal who prefers exploitation and the fundamental difference between the two.

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The model can be applied to several situations. For example, it is applicable to recent deforestation in the tropics. As I explain in section II, the deforestation rate in the Brazilian Amazon is pretty much determined by governmental policies. When the forest is cleared, the land is converted to agriculture. Thus, deforestation is valuable to the agricultural industry, which spends large resources on lobbying the government. On the other side, developed countries have offered payments in return for conservation through the United Nations program Reduced Emission from Deforestation and Forest Degradation (REDD+). Over time, the stakes have increased in the agricultural sector thanks to new trade agreements that enlarge the markets.1 Simultaneously, the threat of climate change, the emergence of global climate policies, and biodiversity losses have made the world community more willing to pay for conservation than before. Franklin and Pindyck (2018) estimate that the average marginal social cost of deforestation in the Brazilian Amazon increases from \$9,000 to \$35,000 per hectare when deforestation rates return to the high levels of the early 2000s (see also Strand et al. 2018). The estimates vastly exceed the cost of conservation (Stern 2008; Busch et al. 2012; IPCC 2014). Nevertheless, deforestation levels have increased in the past few years.²

These developments raise positive and normative questions. When can high exploitation rates be the outcome of the game between governments? What are the roles of polarization, political stability, institutions, and the policy makers' discretion? Are lobby groups taking advantage of the dynamic game between the governments, and why are they not outcompeted by stakeholders paying for conservation? How should compensations for conservation be designed to be effective?

To answer these questions, this paper starts by providing a positive theory of exploitation. In every period, there is a party in power deciding on how much to extract, and how much to conserve, of an exhaustible resource. The stock that is conserved is inherited by the next party in power.

It is beneficial to conserve as well as to exploit. The benefit of extraction is assumed to be larger when one is in power than when one is not in power, because some of the revenues can be controlled by the party in power. Since the party in power decides, it extracts more than the opposition would like. When today's government is uncertain about whether it will remain in power, it fears future overexploitation. This fear reduces the government's continuation value and its benefit from letting the next government manage the resource. The larger is the expected overexploitation, the less it is worthwhile to conserve today.

¹ Burgess, Costa, and Olken (2019, 8) observe a "growing political power of the agriculture producers."

² https://data.worldbank.org/indicator/AG.LND.FRST.K2?locations=BR.

This dynamic interlinkage generates a multiplier effect: a small increase in the value of extraction motivates larger extraction levels both directly and—because later governments will also extract more—indirectly. The indirect effect can be much larger than the direct effect.

The multiplier implies that external stakeholders can be very influential. If a donor provides compensations in return for conservation, the government becomes more likely to conserve. When the current government anticipates that the compensations will make conservation more likely also in the future, then conservation becomes even more sensible, and the government becomes willing to conserve. A lobby, benefiting from exploitation, pays favors to the party that exploits. When today's government anticipates that future governments are more likely to exploit because of the lobby, the government is more likely to exploit right away, even without (or with little) payments.

Both "principals" benefit from the multiplier, but they are fundamentally asymmetric: the lobby needs to pay only once for an extracted unit, whereas a donor must pay in every period to conserve it. The cost is thus higher for the proconservation principal. The future payments are not sufficiently valued by today's government if it fears being out of office later. The larger the political uncertainty is, the lower the influence of the proconservation donor is and the larger the influence of the proexploitation lobby is.

The positive theory is consistent with a number of empirical facts, as explained in section II. This consistency suggests that we should also consider the normative implications that are policy relevant, for example, regarding how compensation payments should be targeted. On the one hand, current payments may be most persuasive if the party in power has full discretion regarding how the funds are to be spent. On the other hand, if the compensation benefits the general public, and not only the ruling party, then future conservation becomes directly valuable to today's ruling party, even if it is not in power later. Specified conditions describe when earmarking the funds can be more effective. I also describe when the donor benefits from paying the lobby group to not lobby. Among the extensions, I consider resources that partly recover, parties that are heterogeneous, principals that differ in their abilities to lobby, and alternative ways in which the principals can influence the extraction rate.

Literature.—Dynamic games between successive governments have been studied extensively. It is well known that political turnover leads to less investment in state capacity (Besley and Persson 2009, 2010), more redistribution and depletion of capital (Tornell and Lane 1999), less stabilization (Alesina and Drazen 1991) and debt repayment (Amador 2003), or the accumulation of debt (Persson and Svensson 1989; Alesina and Tabellini 1990; Tabellini 1991; Battaglini and Coate 2008). In Harstad

(2020), I connect with the hyperbolic discounting literature and show that political rotation motivates investments in commitment technologies.

Similar results appear in resource economics. Extraction rates are shown to be larger if one fears nationalization (Long 1975) or future overexploitation (Kremer and Morcom 2000), if there are multiple dynasties (Nowak 2006), or if the resource fuels conflicts (van der Ploeg and Rohner 2012). More specifically, Robinson, Torvik, and Verdier (2006) show that an incumbent extracts more if he is unlikely to be reelected. Their two-period model is extended by Ryszka (2013) and van der Ploeg (2018), who investigate how a higher probability of being removed from office leads to more rapacious depletion.³

The model in this paper is especially tractable, and it uncovers the multiplier. Given the insight in the above-mentioned literature, however, the primary contribution of this paper is to employ this tractable model to study how multiple principals take advantage of the dynamic game between the governments. The multiplier implies that the returns to lobbying can be high and that the asymmetry between paying once for expropriation and paying always for conservation leads to a fundamental inefficiency. This inefficiency contrasts with the standard finding with menu auctions (Grossman and Helpman 1994; Dixit, Grossman, and Helpman 1997; Aidt 1998), vote buying (Dekel, Jackson, and Wolinsky 2008), and even informational lobbying (Battaglini 2002) that when all stakeholders lobby, the outcome is efficient. The inefficiency is not present in the dynamic lobbying models either.⁴

With this, I add a new political economy perspective to our understanding of deforestation and the design of compensations. Existing theories focus on contract-theoretic problems such as moral hazard (Kerr 2013; Gjertsen et al. 2020), private information (Mason and Plantinga 2013; Mason 2018), observability (Delacote and Simonet 2013), liquidity constraints (Jayachandran 2013), and additionality (Jack and Jayachandran 2019). Burgess et al. (2012) showed that deforestation increased in election years and after decentralization reforms in Indonesia (see Pailler 2018 for a more recent study of Brazil), and Harstad and Mideksa (2017)

³ There is a theoretical literature on dynamic contribution games (see Bagnoli and Lipman 1989; Marx and Matthews 2000; Battaglini, Nunnari, and Palfrey 2014; and subsequent papers), but the present game is different, since every player fears that later players will end the game (by exploiting the resource). In much of the contribution-games literature, in contrast, each player fears that subsequent players will not contribute, i.e., that the game will continue for a long time.

⁴ Levy and Razin (2013) study two principals influencing policy making in a dynamic game, but they focus on voting (among legislators) and assume that the principals can influence the choice of amendment, but not actual votes. Schopf and Voss (2019, 2021) analyze lobbying of a government extracting a resource, but the government (or planner) is long-lived. Neither the multiplier effect nor the inefficiency in the present paper arises in these papers.

provided a theoretical framework to explain these empirical findings and to investigate how conservation contracts should be designed when there are competing jurisdictions. These frameworks are static, however. When the game is dynamic, a time-inconsistency problem arises when a donor would like to postpone the payment for the "conservation good" (Harstad 2016).⁵ Harstad and Storesletten (2023) study the benefits of loans where repayments are requested only when the resource is exploited.

Outline.—For the interested reader, the next section discusses available empirical evidence and explains why the model is consistent with deforestation in the Brazilian Amazon. Section III presents the positive theory with rotations of political power and derives the multiplier. Section IV shows how the multiplier can be taken advantage of—not only by a donor paying for conservation but also by a lobby paying for exploitation. The normative analysis in section V shows when the donor achieves costeffective conservation with earmarks or by compensating the lobby instead of the party in power. Section VI presents extensions, and section VII concludes. The appendix contains all proofs not in the text.

II. Supporting and Motivating Evidence

A. Empirical Investigations

Among other things, my positive theory relies on the assumption that the party in power obtains an additional benefit (Δ) from extracting the resource, compared to the benefits obtained by the parties not in power. The theory predicts that (i) the larger this additional benefit is, the larger the equilibrium extraction rate is; (ii) the lower the probability of staying in power (p) is, the more one extracts; and (iii) the proexploitation lobby will be more influential than the proconservation donor.

The assumption is natural, given that governmental revenues can be used for party perks and not only for public goods that benefit everyone. The assumption is also in line with empirical evidence. Caselli and Michaels (2013, 230–31) find that "some of the revenues from oil [in Brazil] disappear before turning into the real goods and services they are supposed to be used for" and that "the evidence leads us to conclude that the missing money result is explained by a combination of patronage spending/rent sharing and embezzlement." More recently, Andersen et al. (2017, 857) estimate that "around 15% of the windfall gains accruing to petroleum-rich countries with autocratic rulers is diverted to secret accounts in havens." They continue, "This finding provides empirical

⁵ Harstad (2016) analyzed a dynamic game between a country that prefers to exploit and a donor who may buy or lease a resource for conservation. An inefficiency arises because the donor benefits from being expected to pay, so that the owner conserves in the meanwhile. That model did not permit rotation of political power, and thus the multiplier was not discussed. Also, that model did not permit multiple principals.

support for the theoretical argument that rulers and political elites in countries with weak political constraints and lack of competitive elections transform petroleum rents into political rents."

In the model, Δ can be large because of disagreements, weak institutions, or corruption. In line with prediction i, weaker institutions, and more corruption, seem to be associated with faster resource exploitation. Barbier, Damania, and Léonard (2005, 294) confirm that "corruption appears to be associated with cumulative land expansion in tropical developing economies." More specifically, they find, "the direct effect of greater control of corruption appears to be a reduction in cumulative agricultural land expansion of between 0.11% and 0.22%" (292).

There is more empirical evidence regarding prediction ii. Recently, Sanford (2021, 13) documents that "political competition may fuel exploitation of natural resource[s]." More specifically, he studies the effects on deforestation and finds that "competitive elections were associated with increased deforestation" (1). Sanford argues that the democratic transition (with more competition between parties) leads to a reduction in forest cover.

Oil is extracted by private companies, but policy makers may still prefer faster extraction if they do not expect to stay in power for long. Collier (2010, 1124) found that "ministers in the transitional government in the Democratic Republic of Congo (DRC) knew that they had only around three years in office. During this period many contracts were signed with resource extraction companies conceding very generous terms in return for signature bonuses that cashed in the value of the natural assets to the society."

More generally, Bohn and Deacon (2000, 543) compare different types of resources and find that "higher risk implies heavier discounting of future returns, tending to hasten production in the short run, but lowers the capital intensity of oil production, tending to slow production in the long run." That is, they find that "forest stocks are reduced by ownership risk" (547), but that a resource like oil, which requires up-front investment before it can be exploited, is not necessarily exploited faster.

Combined, predictions i and ii suggest that resources are better managed if p is large, while Δ is small. This finding is consistent with the empirical evidence of Collier and Hoeffler (2009, 305), who find that "electoral competition on the resource-rich societies appears to be particularly inappropriate unless, it is complemented by checks and balances." They also write "our results suggest that the form of democratic polity best-suited to resource-rich countries is one with checks and balances that are strong relative to electoral competition. This is indeed the form of democracy in the most striking exception to generally adverse combination of democracy and resource rents, namely Botswana. Electoral competition is in practice quite limited: The government has never been defeated at the polls. Yet, perhaps because the democracy has been continuous since independence, the legal and bureaucratic procedures that constitute checks and balances have been maintained."

Future research must test other predictions of the model, including prediction iii, the stronger influence of proexploitation lobbies compared with proconservation stakeholders. Sure, lobby groups are active, as argued below. Harding et al. (2022) study lobby groups in Columbia and argue that "given the benefits to be had from forest clearance, campaign donations are used to buy regulatory non-enforcement of [conservation laws], as mayors choose not to sanction illegal deforestation in return for campaign contributions" (1). At the same time, we have more than a decade of experience with REDD+. Despite the large conservation benefits referred to in the Introduction, relative to the costs, IPBES (2019, 910) reports that "the literature is currently mixed on the success rates of forest carbon projects." Despite Brazil's being the largest recipient of REDD+ funds, its policy makers have tolerated deforestation levels that have increased.

B. Deforestation in the Amazon

Even though deforestation is influenced by many factors, it is mostly influenced by the government. Burgess, Costa, and Olken (2019, 3) analyze satellite data and conclude that they "demonstrate the remarkable reach of the Brazilian state to exploit or conserve its natural resources."⁶ The authors also find "concrete evidence that the Brazilian state [was] favoring exploitation over conservation" (2).

The high deforestation levels under President Jair Bolsonaro are consistent with the theory. After the election in 2018, *The Economist* wrote that "most analysts had thought that the right-winger would eventually lose to someone less divisive" and "his own Social Liberal Party, until now a tiny group, will have 52 seats in the 513-member lower house, up from eight in the outgoing congress."⁷ Low approval rates suggested that the probability of staying in power must have appeared limited.

Nevertheless, "Brazil's powerful farm lobby endorses far-right presidential candidate Bolsonaro"—according to Reuters.⁸ The agricultural sector has for decades supported, and lobbied for, a policy that permits

⁶ In particular, the high deforestation rates in the early 2000s were "associated with Brazilian policies to develop the Amazon," they write (2), but "this policy stance was sharply reversed in the 2006–2013 period with laws to protect the Amazon rainforest being introduced and enforced" (3).

⁷ https://www.economist.com/the-americas/2018/10/08/a-right-wing-populist-is-poised -to-become-brazils-next-president.

⁸ https://www.reuters.com/article/us-brazil-election-agriculture-idUSKCN1MC21M.

extensive deforestation.⁹ Transparency International reported that the Brazilian agriculture business "donated close to US\$100 million to politicians in the 2014 elections".¹⁰ Some paid illegal bribes, and the police had "crack[ed] down on an alleged massive land grab by an agribusiness collective in western Bahia, one of Brazil's largest soy producing regions."¹¹

Evidently, the proexploitation lobby does not attempt to earmark the donations for public goods.

Proconservation donors, in contrast, may benefit from earmarking the compensation for public goods, according to my theory. In the period 2005–12, the Brazilian government proved that deforestation can be reduced dramatically when there is a political will. Norway, the biggest contributor to the REDD+ program, paid Brazil \$1.2 billion in return. The REDD+ funds are, in part, earmarked, but the debate regarding earmarks is intense. In 2019, the governments of Brazil and Norway disagreed on how much discretion the Brazilian government should have and, as a result, the funding was suspended.¹² The conflict nurtured a debate regarding alternative targets. Angelsen et al. (2018) found that a donor might benefit from cooperating with farmers and agricultural associations instead of with governments, exactly as my theory predicts.

III. The Dynamics of Conservation and Extraction

A. An Extraction Game

Consider a natural resource that is being depleted over time. The resource can be a standard exhaustible resource, such as oil or coal. In practice, even a biodiverse tropical forest is exhaustible: once the forest is logged, and once the land is converted to agriculture, it will not return anytime soon. To fix ideas, I thus refer to the stock as tropical forests.

Time is discrete, and there is an infinite number of periods. At time *t*, the size of the stock is S_t . When the extracted fraction is $x_t \in [0, 1]$, $S_{t+1} = (1 - x_t)S_t$.

⁹ See Barbier, Damania, and Léonard (2005) and, more recently, *The Washington Post*: https://www.washingtonpost.com/world/the_americas/why-brazilian-farmers-are-burning -the-rainforest–and-why-its-difficult-for-bolsonaro-to-stop-them/2019/09/05/3be5fb92 -ca72-11e9-9615-8f1a32962e04_story.html.

¹⁰ https://www.jstor.org/stable/pdf/resrep24899.pdf (6).

¹¹ https://news.mongabay.com/2019/11/brazil-investigates-agribusiness-bribes-to-judges-for-favorable-land-rulings/.

¹² Reuters reported, "The aid that Brazil receives depends on the results of work to curb deforestation and for 2018 the funding would amount to about 300 million Norwegian crowns (\$33.27 million), but Norway will not proceed with the payment, a ministry spokes-woman confirmed to Reuters." In particular, "Norway has suspended donations supporting projects to curb deforestation in Brazil after the country's right-wing government blocked operations of a fund receiving the aid" (https://www.reuters.com/article/us-brazil-envi ronment-norway-idUSKCN1V52C9).

Players.—Variable x_t is decided on by the party in power at time t, P_t . This party may or may not be in power in the future. Let $p \in [0, 1]$ measure the probability that the party is in office in any later period. If p = 1, there is no rotation of political power. If there are n identical parties, we may have p = 1/n. For simplicity, I abstract from autocorrelation: whether P_t is in power at some time t' does not influence P_t 's chance of being in power later.¹³ For now, the parties are identical and p is exogenous, but section VI discusses how both assumptions can be relaxed.

Benefits.—The resource can be beneficial whether it is extracted or conserved. Deforestation implies land-use change so that agricultural products can be produced. If the per-period marginal agricultural value is lowercase a_1 , the present-discounted value of each extracted unit is uppercase $A_1 = a_1/(1 - \delta)$, where δ the discount factor. I let the present-discounted value of the timber (or of the oil or coal, if the model is applied to fossil fuel extraction).

To allow for a conflict of interest, $A_1 > 0$ is the extraction benefit for the party in power, while $A_0 \ge 0$ is the benefit for a party not in power. I assume that $\Delta \equiv A_1 - A_0 \ge 0$, meaning that any P_t benefits more if it exploits the resource than if another party exploits the resource. This assumption is natural, since the party in power can spend (parts of) the revenues on perks (see sec. II). With this interpretation, it seems reasonable that Δ is correlated with the amount of corruption in the country. In other applications, as when each government would prefer to postpone the repayment of debt, $\Delta < 0$ can be natural.

There may also be a benefit from conservation. The per-period benefit from each conserved unit is lowercase b > 0. Thus, the benefit from conserving a unit indefinitely is uppercase $B = b/(1 - \delta)$. For the most part, it will be assumed that the optimal extraction level is strictly positive (i.e., $A_0 > B$). (The appendix permits disagreements over the conservation benefit.)

The extraction cost.—The extraction cost function is

$$\frac{c}{2}x_t^2 S_t.$$
 (1)

Intuitively, one view is that the extraction cost should increase in the fraction that is extracted, x_t and also with the total stock S_t , for a given x_t , because the effort associated with extracting the fraction x_t from an average unit must be repeated for the number of units. An alternative viewpoint is that it seems reasonable to let the extraction cost be increasing and convex in the extracted quantity (x_tS_t) but possibly decreasing in

¹³ With incumbency advantage, P_i 's probability of staying in office is higher at t + 1 than at t + 2, and so on. This autocorrelation leads to a time-inconsistency problem that is less tractable (Harstad 2020).

the size of the remaining stock (for a given extracted quantity), because a larger stock makes it possible to distribute the extraction intensity over multiple remaining units. The cost function (1) is in line with both views, because we can write $cx_t^2S_t/2 = c(x_tS_t)^2/2S_t$.

A microfoundation.—Because (1) is in line with both views discussed above, it is not difficult to provide a supporting microfoundation. Suppose that to successfully log a typical unit of S_b one must offer a payment $\omega \ge 0$ that is larger than the input cost, θ . For example, a local worker or supplier may have to be hired. When each local input cost is unknown and uniformly distributed as $\theta \sim U[0, \overline{\theta}]$, a take-it-or-leave-it offer ω implies that the unit is logged with probability $\omega/\overline{\theta}$ and that the fraction of units that is logged is $x = \omega/\overline{\theta}$. The total cost of this extraction is $\omega \cdot (\omega/\overline{\theta}) \cdot S_t$, written as (1) when $c \equiv 2\overline{\theta}$.¹⁴

B. Strategies and Equilibrium Concept

Given the large set of equilibria in dynamic games, it is common to restrict attention to stationary Markov-perfect equilibria (MPEs). A Markov strategy cannot depend on payoff-irrelevant aspects of the history. That is, if P_t does not strictly benefit from conditioning its strategy on the stock in a situation in which the other parties do not condition their strategies on the stock—then P_t 's Markov-perfect strategy does not depend on the stock.¹⁵ Here, a Markov-perfect x_t must be independent from S_t .

LEMMA 1. There is a unique MPE. The MPE requires x_t to be invariant in S_t . Continuation values are linear in S_t .

Proof. Suppose that every future x_r is independent of the stock and is measured by stationary x_s . Then, a player's expected continuation value, starting from t + 1, is

$$\sum_{\tau=t+1}^{\infty} \delta^{\tau-(t+1)} (1-x_{s})^{\tau-(t+1)} \left[S_{t+1} x_{s} A_{p} + S_{t+1} (1-x_{s}) b - S_{t+1} c x_{s}^{2} / 2 \right]$$

$$= v_{p}(x_{s}) S_{t+1}, \text{ where}$$

$$v_{p}(x_{s}) = \frac{x_{s} A_{p} + (1-x_{s}) b - x_{s}^{2} c / 2}{1 - \delta(1-x_{s})} \text{ and } A_{p} \equiv (1-p) A_{0} + p A_{1}.$$
(2)

Given the continuation value $v_p(x_s)S_{t+1}$, the optimal x_t is

¹⁴ If the local workers' surplus (which is expected to be $(\omega/2) \cdot (\omega/\dot{\theta}) \cdot S_t$) is internalized, the net extraction cost is (1) with $c \equiv \bar{\theta}$.

¹⁵ Or, as Maskin and Tirole (2001, 202) write, "Markov strategies are the simplest strategies (i.e., the strategies measurable with respect to the coarsest partition and hence dependent on the fewest variables) that are consistent with rationality in the sense that, if the other players make their strategies measurable with respect to some [even] coarser partition [of the history], it would *not* always be optimal for a player to make his or her choice between any two given continuation strategies measurable with respect to [that partition]."

$$\arg\max_{x} S_{t} x_{t} A_{1} + S_{t} (1 - x_{s}) b - S_{t} x_{s}^{2} c/2 + \delta (1 - x_{t}) v_{p} (x_{s}) S_{t}.$$
 (3)

There is a unique $x_t = x_s$ solving (3). This solution is clearly independent of S_t . QED

The lemma follows because, given x_t , all benefits and costs are proportional to S_t . With alternative functional forms, x_t may decline or increase with S_t , but these changes would make the results emphasized in this paper less transparent, and the analysis would also be less tractable.

C. The First Best

Let A_* be the social planner's value of each extracted unit (e.g., A_* may be a weighted average of A_0 and A_1).

Consider, first, a planner at *t*, taking as given $x_{\tau} = x_s$, $\tau > t$. The planner's continuation value at t + 1, $v_*(x_s)$, is given by equation (2) if we replace A_p with A_* . Given $v_*(x_s)$, the first-best x_t follows from (3) if A_* replaces A_1 :

$$x_{t} = \frac{A_{*} - b - \delta v_{*}(x_{s})}{c} = \frac{A_{*} - b}{c} - \frac{\delta}{c} \frac{x_{s}A_{*} + (1 - x_{s})b - x_{s}^{2}c/2}{1 - \delta(1 - x_{s})}.$$
 (4)

Because $v_*(x_s)$ is concave in x_s , x_t is convex in x_s . Because $v_*(\cdot)$ is maximized at

$$x_* = \operatorname{arg\,max} v_*(x)$$
$$= \max\left\{0, \sqrt{\left(\frac{1-\delta}{\delta}\right)^2 + 2\left(\frac{1-\delta}{\delta}\right)\frac{A_* - B}{c} - \frac{1-\delta}{\delta}\right\}}, \quad (5)$$

the optimal x_t , given x_s , is minimized when $x_s = x_*$. When $x_s = x_*$, the planner's preferred x_t maximizes the same continuation value as does x_s , so $x_t = x_*$.¹⁶

D. The Equilibrium Outcome

In general, P_t 's preferred x_t will depend on the expected future stationary x_s . To see how, note that P_t 's problem is given by (3), and the first-order condition (FOC) becomes

¹⁶ To ensure that $x_* \in (0, 1)$, assume

$$\sqrt{\left(\frac{1-\delta}{\delta}\right)^2 + 2\frac{A_*}{c}\left(\frac{1-\delta}{\delta}\right) - 2\frac{b}{c}} - \frac{1-\delta}{\delta} \in (0,1).$$

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$$x_t = \frac{A_1 - b - \delta v_p(x_s)}{c}.$$
 (6)

Analogously to the first best, because $v_p(x_s)$ is concave in x_s , x_t will be convex in x_s (see fig. 1). Because $v_p(x_s)$ is maximized at x_p , x_t is minimized at x_p , where

$$x_{p} \equiv \arg \max v_{p}(x)$$
$$= \max \left\{ 0, \sqrt{\left(\frac{1-\delta}{\delta}\right)^{2} + 2\left(\frac{1-\delta}{\delta}\right)\frac{A_{p}-B}{c}} - \frac{1-\delta}{\delta} \right\}.$$
(7)

In contrast to the first best, however, $x_i > x_p$, even if $x_s = x_p$, when $(1 - p)\Delta > 0$:

$$x_t = x_p + \frac{A_1 - A_p}{c} = x_p + \frac{(1 - p)\Delta}{c}$$

In equilibrium, we have that extraction is larger than x_p not only at time t but at all future dates. When extraction is larger, the resource will be exploited faster in the future, and the value of contemporary conservation is reduced. The lower continuation value motivates P_t to extract even more. This iterative domino process, illustrated in figure 1, converges to the fixed point $x_t = x_s = x_M$:



FIG. 1.—If Δ increases a little, x_M can increase by a lot—thanks to the multiplier.

$$x_{\rm M} = \frac{A_1 - b - \delta v_p(x_{\rm M})}{c} \Rightarrow$$
$$x_{\rm M} = \sqrt{\left[\frac{(1-p)\Delta}{c} - \frac{1-\delta}{\delta}\right]^2 + 2\left(\frac{1-\delta}{\delta}\right)\frac{A_1 - B}{c}} + \frac{(1-p)\Delta}{c} - \frac{1-\delta}{\delta}.$$
(8)

The Markov-perfect extraction level is stationary and increasing in $(1 - p)\Delta$, as shown in the appendix. Thus, x_M declines in p. In contrast, x_p increases in p. That is, when P_t is less likely to be in power later, P_t 's preferred future x_p is smaller, but P_t 's actual x_t is larger. For every p < 1, $x_M > x_1$, where $x_1 = \max_p x_p$.¹⁷

E. The Multiplier

To study comparative statics, equation (6) gives, for every parameter $I \in \{A_1, A_0, b, c, \delta, p\}$,

$$\frac{dx_t}{dI} = \frac{\partial x_t}{\partial I} + \frac{\partial x_t}{\partial x_s} \frac{dx_s}{dI} = \frac{\partial x_t}{\partial I} \left(1 + \frac{\partial x_t / \partial x_s}{1 - \partial x_t / \partial x_s} \right).$$

When $\Delta = 0$ or p = 1, $\partial x_t / \partial x_s = 0$, because every future extraction level is optimally chosen, from P_t 's point of view. This follows from applying the envelope theorem to equation (6).

But the larger $(1 - p)\Delta > 0$ is, the larger the future extraction level is compared to x_p , and the larger $\partial x_t / \partial x_s > 0$ is.

This logic implies that a larger $(1 - p)\Delta$ increases not only x_M but also the sensitivity of x_M to every parameter change.

PROPOSITION 1. When $(1 - p)\Delta > 0$ is larger, equilibrium $x_M > x_p$ is larger, $\partial x_t / \partial x_s > 0$ is larger, and the multiplier $\mu > 0$ is larger:

$$\frac{\partial x_t}{\partial x_{\rm s}} = \frac{\delta}{c} \frac{(1-p)\Delta}{1-\delta(1-x_{\rm s})} = \frac{\mu}{1+\mu}, \quad \text{and}
\frac{dx_t}{dI} = (1+\mu) \frac{\partial x_t}{\partial I}, \quad I \in \{A_1, A_0, b, c, \delta, p\}, \quad \text{where}$$

$$\mu \equiv \frac{\partial x_t/\partial x_{\rm s}}{1-\partial x_t/\partial x_{\rm s}} = \frac{\delta(1-p)\Delta}{c[1-\delta(1-x_{\rm s})]-\delta(1-p)\Delta}.$$
(9)

¹⁷ As before, I restrict attention to parameter values ensuring that x_{M} is in (0, 1), i.e.,

$$\sqrt{\left[\frac{\Delta(1-p)}{c} - \frac{1-\delta}{\delta}\right]^2} + 2\frac{(1-\delta)A_1 - b}{\delta c} + \frac{\Delta(1-p)}{c} - \frac{1-\delta}{\delta} \in (0,1).$$

We can also refer to μ as the *conservation multiplier*, because

$$\frac{d(1-x_t)}{dI} = -\frac{dx_t}{dI} = -(1+\mu)\frac{\partial x_t}{\partial I} = (1+\mu)\frac{\partial (1-x_t)}{\partial I}.$$

F. Calibration

A serious calibration is beyond the scope of this paper, but a very first attempt illustrates the potential. Suppose that $\Delta/A_0 = 1/3$, to reflect that the total gain from controlling the resource may be double the 15% that is diverted to secret accounts, documented by Andersen et al. (2017), because funds are also used for party perks and not only private consumption. With a 4% discount rate per year, $\delta \approx 0.85$ over a 4-year electoral period. Over the past 2 decades, deforestation rates in Brazil have been between 1% and 3% (per 4-year period), according to the World Bank.¹⁸ If we assume that this interval is supported by $p \in [0, 1/2]$, we can use equation (8) to calibrate the model and obtain $b/A_0 \approx 0.198$ and $c/A_0 \approx$ 2.12. If roughly 2% is deforested every 4-year period, on average, equation (8) requires $p \approx 1/7$. The estimated p does not appear unrealistic. With these numbers, the multiplier is estimated from equation (9):

$$\partial x_t / \partial x_s \approx 0.69$$
, so $\mu \approx 2.20$.

These numbers are interesting in themselves, and they can also help to study counterfactuals. If A_0 stays unchanged and we let *p* increase to 1, equation (8) verifies that x_M is reduced from 2% to 0.5%. If, instead, Δ is reduced to zero, x_M falls to zero.

The calibration can also help to shed light on the results in the subsequent sections.

IV. Payments and Lobbying for/against Conservation

The above dynamic game between consecutive governments can be taken advantage of by external stakeholders. This section considers multiple principals who influence the parties and uncovers a fundamental inefficiency that arises when one principal pays to maintain the status quo while the other pays for exploitation. For pedagogical reasons, I introduce one principal at a time.

¹⁸ https://data.worldbank.org/indicator/AG.LND.FRST.K2?locations=BR.

A. Compensating for Conservation

1. Effects of Compensations

Real-world REDD+ payment schemes are surprisingly simple. Here, I consider a compensation level k_i per unit of conserved resource at time t. As a start, assume that k_i benefits only the party in power and that it enters linearly and additively in P_i 's utility function.

The larger k_t is, for any fixed x_s , the more P_t will conserve. This decrease in x_t is the immediate and direct effect of the compensation. In addition, there is an indirect effect at play when k_s is expected to be offered to future parties that conserve, since a smaller future x_s also contributes to a smaller x_t at time t, as established by proposition 1. Thanks to the multiplier, the total effect of a given per-period payment k_s can be much larger than the effect of k_t in period t only. In other words, the presence and anticipation of future compensations help donor K to obtain what it seeks today, additional conservation.

2. Optimal Compensation

Let *K* be the long-lived donor or contributor. If f > 0 measures *K*'s perperiod value from a unit of conserved resource, $F \equiv f/(1 - \delta)$ is *K*'s present-discounted value from conserving a forest unit for all time. Equivalently, *K* faces the present-discounted cost x_tS_tF when x_tS_t is extracted. Thus, *K*'s continuation payoff can be represented as

$$V^{K}(S_{t}) = -x_{t}S_{t}F - (1 - x_{t})S_{t}k_{t} + \delta V^{K}(S_{t+1}).$$

Because *K*'s per-period payoff is linear in S_t (conditional on x_t and k_t), the logic in section III.B continues to imply that a Markov-perfect k_t must be stationary and independent of S_t . The appendix derives the Markov-perfect k_M and, for comparison, also the compensation level if *K* could commit to a fixed k_c for every future period.

LEMMA 2. The Markov-perfect compensation level, k_{M} , increases in f:

$$k_{\rm M} = \max\{0, (1-\delta)F - (1-x_{\rm M})[1-\delta(1-x_{\rm M})]c\}.$$
(10)

By comparison, if *K* could commit to a stationary k_c , the FOC for k_c would be

$$k_{c} = \max\left\{0, (1-\delta)F - (1-x_{s})(1-\delta(1-x_{s}))c\left\{\frac{1-\partial x_{t}/\partial x_{s}}{1+\delta p(1-x_{s})/[1-\delta(1-x_{s})]}\right\}\right\}, (11)$$

where
$$\frac{\partial x_{t}}{\partial x_{s}} = \frac{\delta}{c}\frac{(1-p)(\Delta-k_{c})}{1-\delta(1-x_{s})}.$$
(12)

Naturally, the compensation is larger if conserving another period is valuable (i.e., if $f = (1 - \delta)F$ is large). When $x_M \rightarrow 1$, $k_M \rightarrow f$, because every conserved unit is additional and due to the compensation.

There are two reasons for why $k_c > k_M$, as reflected by the numerator and the denominator in equation (11). First, if p is small and Δ is large, we know from proposition 1 that P_t is willing to conserve more if future extraction levels are expected to be lower. Future extraction levels will be lower indeed, if future compensation levels are higher. Thus, if *K* could commit to or build a reputation for a large k_c , she could take advantage of the multiplier. Harstad (2016) emphasizes the inefficiency that arises when *K* prefers to postpone the payment for the "conservation good."

Second, even if p is large or $\Delta = 0$, $k_c > k_M$ if p > 0. Intuitively, if P_t is likely to remain in power also in the future, P_t conserves more at time t if P_t expects to enjoy larger future compensations, as a result.

Regardless of how k_s is set, equation (12) shows that a larger k_s lowers $\partial x_t / \partial x_s$, and thus the multiplier. Intuitively, when the party in power, inclined to extract excessively, receives compensations in return for conservation, then the party in power and the opposition are more aligned. If $k_c \rightarrow \Delta$, the multiplier converges to zero.

B. Lobbying for Exploitation

1. Effects of Lobbying

Assume that the lobby contribution l_t to P_b conditional on each unit of exploitation at time t, benefits only the party in power and that it enters linearly and additively in P_t 's utility function. If the equilibrium l_t is stationary and equal to l_s , a larger l_s has the same effect as a larger A_1 and Δ , while A_0 is unchanged. The equations for x_t continue to hold if just l_s is added to A_1 and to Δ .

In addition, when P_t anticipates that future lobbying will increase x_s , then P_t becomes more willing to exploit at time t because of the larger future x_s as well as because of the possibility of obtaining l_t right now. Thanks to the multiplier, the total effect of a given per-period payment l_s on x_t can be much larger than the effect of l_t , in period t only, on x_t . In other words, the presence and anticipation of future lobbying help the lobby to obtain what it seeks.

Therefore, for any given future x_s , x_t increases in l_t . In addition, when P_t anticipates that future lobbying will increase x_s , then P_t becomes more willing to exploit at time t because of the larger future x_s as well as because of the possibility of obtaining l_t right now. Thanks to the multiplier, the total effect of a given per-period payment l_s on x_t can be much larger than the effect of l_t , in period t only, on x_t . In other words, the presence and anticipation of future lobbying help the lobby to obtain what it seeks.

2. Optimal Lobbying

Suppose that the lobby, *L*, is long-lived. Also, *L*'s present-discounted gain from each extracted unit is represented by *G*. For example, *L* may gain

g > 0 per period from the grains produced on a unit of land, where $G = g/(1 - \delta)$. Of course, G can also capture L's value of the extracted units (e.g., the timber).

At the start of every period t, L offers l_t to P_t for every extracted unit. Thereafter, P_t decides on x_t and receives $l_t x_t S_t$ in return from L, added to P_t 's payoff. Thus, L's continuation value is

$$V^{L}(S_{t}) = (G - l_{t})x_{t}S_{t} + \delta V^{L}(S_{t+t}).$$

As before, the payoff's linearity in S_t implies that a Markov-perfect compensation level, l_M , will be independent from S_t .

LEMMA 3. The Markov-perfect level of lobbying, l_M , increases in G:

$$l_{\rm M} = \max\left\{0, \, G - \frac{1 - \delta(1 - x_{\rm M})}{1 - \delta} \, c x_{\rm M}\right\}.$$
(13)

By comparison, if L could commit to a stationary l_c , the FOC for l_c would be

$$l_{\rm c} = \max\left\{0, G - \frac{1 - \delta(1 - x_{\rm s})}{1 - \delta} cx_{\rm s} \left[\frac{1 - \partial x_t / \partial x_{\rm s}}{1 - \delta p x_{\rm s} / (1 - \delta + \delta x_{\rm s})}\right]\right\}, \text{ where } (14)$$

$$\frac{\partial x_i}{\partial x_s} = \frac{\delta}{c} \frac{(1-p)(\Delta+l_s)}{1-\delta(1-x_s)}.$$
(15)

Naturally, the equilibrium lobbying level increases in *G*. When l_M increases, x_M increases, and equation (13) shows that the larger x_M weakens the effect of *G* on l_M somewhat. Equilibrium l_M decreases in x_M , because a large x_M implies that *L*'s payment $x_M l_M S_t$ is large relative to the obtained additional exploitation. When $x_M \to 0$, $l_M \to G$, because every exploited unit is additional.

By comparison, l_M can be smaller or larger than l_c . There are two forces at play, and the first is reflected by the term $1 - \partial x_t / \partial x_s$ in the numerator. If P_t is likely to be out of office later and Δ is large, then $\partial x_t / \partial x_s$ is large. In this case, P_t extracts more when future parties are expected to extract more. To exploit the multiplier, *L* would prefer to commit or build a reputation for lobbying even more than l_M .

In contrast, if P_t is likely to remain in office, then a larger anticipated lobbying level implies that P_t expects that resource extraction will be rewarded (by *L*) also in the future, making it less important to extract right away. The lower importance of extracting right away is harmful for *L* in this situation, so *L* would prefer to commit to a smaller l_c . As reflected by the denominator in the square brackets in equation (14), a larger *p* will reduce the optimal l_c .

Regardless of how l_s is set, equation (15) shows that a larger l_s has the same positive effect on $\partial x_l / \partial x_s$, and on the multiplier, as an increase in

 Δ does. Intuitively, a larger l_s increases the party in power's gain from extraction but not the opposition's gain. Therefore, x_t is more sensitive to variations in expectations and parameter changes if the level of lobbying is high.

C. Paying Forever to Conserve versus Once to Exploit

If we henceforth consider the case in which both k_M and l_M are strictly positive, it is straightforward to combine the two principals in the dynamic game between ruling parties. At the beginning of every period t, K sets the compensation k_t for every conserved unit, at the same time as L sets the lobbying level l_t . Then, P_t sets x_t and collects $k_t(1 - x_t)S_t$ from K and $l_tx_tS_t$ from L. Otherwise, the payoffs are as before.

After including the principals in the game, it seems reasonable to redefine the first best so that the social marginal value from exploitation is $A_* + G$, while B + F is the social value from conserving a forest unit indefinitely. From equation (5),

$$x_* = \arg \max v_*(x)$$

= $\max \left\{ 0, \sqrt{\left(\frac{1-\delta}{\delta}\right)^2 + 2\left(\frac{1-\delta}{\delta}\right)\frac{A_* + G - B - F}{c}} - \frac{1-\delta}{\delta} \right\}.$

If *F* and *G* increase by the same amount, the two changes cancel, and the first-best x_* remains unchanged. The Markov-perfect x_M , in contrast, turns out to increase.

PROPOSITION 2. The first-best x_* decreases in *F* and increases in *G* according to

$$-\frac{\partial x_*/\partial G}{\partial x_*/\partial F} = 1,$$

but in the MPE, the impact of *G* is larger than that of *F*:

$$\begin{aligned} -\frac{\partial x_{\mathrm{M}}/\partial G}{\partial x_{\mathrm{M}}/\partial F} &= 1 + \delta \frac{1-p}{1-\delta} \frac{1-\delta(1-x_{\mathrm{M}})}{1-\delta(1-x_{\mathrm{M}})(1-p)} \in \left[1, \frac{1}{1-\delta}\right] \\ & \longrightarrow \frac{1}{1-\delta(1-p)} \text{ if } x_{\mathrm{M}} \to 0. \end{aligned}$$

If p = 1, the impacts of *F* and *G* on x_M are equal, exactly as in the first best and in the earlier literature (Grossman and Helpman 1994; Dixit, Grossman, and Helpman 1997; Aidt 1998). In this case, P_t is certain to stay in power and values how conservation at *t* allows for compensation to continue in the future.

How $-(\partial x_{\rm M}/\partial G)/(\partial x_{\rm M}/\partial F)$ Varies with p						
	p = 0	p = 1/7	p = 1/2	<i>p</i> = 1		
$-(\partial x_{\rm M}/\partial G)/(\partial x_{\rm M}/\partial F)$	6.7	3.7	1.7	1		

TADLE 1

NOTE.—The smaller is p, the larger is the influence of G, relative to F, on x_{M} .

When p < 1, however, the impact of F is larger. The intuition is that political rotation and instability make the ruling party impatient, and this impatience implies that K has less political influence than does L. After all, *K* must pay for a conserved unit in every future period, and thus K's willingness to pay reflects K's value of conserving a unit one additional period, as reflected by $f = (1 - \delta)F$. The future payments are costly for K but not sufficiently valued by the current party in power. In contrast, L must pay only once for a unit that is extracted, and thus L's willingness to pay reflects L's entire present-discounted value from exploitation, as measured by G. The smaller p is, the smaller is P_t 's weight on the future k_s , and thus on F, compared to P_t 's weight on l_t , and thus on G. If $p \to 0, -(\partial x_M/\partial G)/(\partial x_M/\partial F) \to 1/(1-\delta)$. In this case, P_t does not value the direct impact of compensations to future parties that conserve. In this case, P_t is equally influenced by k_s and by l_s and is equally influenced by $(1 - \delta)F = f$ and by *G*.

Table 1 illustrates how $-(\partial x_{\rm M}/\partial G)/(\partial x_{\rm M}/\partial F)$ varies with p. To derive the numbers, I draw on section III.F, where I argued that it is reasonable with $\delta = 0.85$ and where I estimated that $p \approx 1/7$. I let $x_{\rm M} \rightarrow 0$ to make the numbers comparable with table 2.19

As an example, let $F = \phi \underline{F}$, $G = \phi \underline{G}$, and

$$\underline{F}/\underline{G} \in \left(1, 1+\delta \frac{1-p}{1-\delta} \frac{1-\delta(1-x_{\mathrm{M}})}{1-\delta[1-x_{\mathrm{M}}(1-p)]}\right).$$

Here, $\phi > 0$ measures the importance of the principals' stakes. It is easy to check that if ϕ increases, the first-best x_* declines, but the equilibrium $x_{\rm M}$ increases.

This asymmetry holds whether or not the two principals can commit to or build a reputation for future payment levels. The proofs in the appendix allow the two principals to have heterogenous contribution costs

¹⁹ The numbers are very similar with $x_{\rm M} = 0.02$, argued for in sec. III.F. With $x_{\rm M} = 0.02$, the table becomes

	p = 0	p = 1/7	p = 1/2	p = 1
$-(\partial x_{\rm M}/\partial G)/(\partial x_{\rm M}/\partial F)$	6.7	3.8	1.8	1

	$(x_{ m D}, x_{ m R})$			
	$p_{\rm R} = 1/7$	$p_{\rm R} = 1/2$	$p_{\rm R} = 6/7$	
$x_{\rm R,*} = .10$	(.01, .12)	(.01, .11)	(.02, .10)	
$x_{R,*} = .20$	(.02, .26)	(.04, .22)	(.05, .20)	
$x_{\rm R,*} = .30$	(.05, .40)	(.08, .33)	(.09, .31)	

TABLE 2 How Equilibrium Extraction Rates Vary with $x_{\rm R,*}$ and $p_{\rm R}$

NOTE.—The equilibrium extraction rates in percentages, $(x_{\rm b}, x_{\rm R})$ are larger than the parties' bliss points, $(0, x_{\rm R})$, especially if the disagreement is large and especially for the party that is unlikely to be in power later.

and impacts. The effect of this heterogeneity is orthogonal to the asymmetry emphasized above, and the two are empirically distinguishable. (For example, the effect of heterogenous costs or impacts will be important no matter the level of p.)

So far, the analysis has been positive. The basic predictions are consistent with the facts discussed in section II. This consistency makes the following normative analysis meaningful.

V. Cost-Effective Conservation

The fundamental inefficiency uncovered by proposition 2 suggests that paying the party in power may not necessarily be the best way of achieving conservation. The party in power will not fully appreciate future payments, since the party may be out of power later.

A. Public Good Earmarks

If all payments are directed to fund the provision of a public good, benefiting everyone, P_t benefits directly from future conservation payments, whether or not P_t is in power. In this scenario, P_t is incentivized to conserve more. However, paying for public goods is less targeted toward the party in power, since the funds are tied to goods that may be of secondary importance to the party. With direct transfers, P_t can spend the money on public goods or on party perks, just as the party pleases.

To capture this trade-off, suppose that payments funding a public good provide the benefit $\gamma \in (0, 1)$ per dollar for the opposition as well as for the party in power. It is reasonable that $\gamma < 1$, since, otherwise, P_t (whose value of a dollar is normalized to 1) would prefer to spend all of P_t 's own funds on the public good.

Let $k_t^B \ge 0$ measure *K*'s payments per unit of conserved forest, earmarked the public good, while $l_t^B \ge 0$ is *L*'s earmarked payment, per extracted unit. For any given k_t^B and l_t^B , γk_t^B adds to all parties' benefit of conservation, while γl_t^B adds to all parties' value of exploitation. The analysis in section III remains unchanged if just *b* is replaced with $b + \gamma k_G$, while A_0 and A_1 are replaced with $A_0 + \gamma l_t^B$ and $A_1 + \gamma l_t^B$, respectively.²⁰

If all payments are earmarked public goods provisions, the effects of F and G are symmetric, just as in the first best. Then P_t will value the future payments.

In the MPE, however, no payment will be earmarked for the public good when $\gamma < 1$.

PROPOSITION 3. i) If all payments are earmarked for public goods, then, as in the first best,

$$-\frac{\partial x_{\rm M}}{\partial x_{\rm M}} \frac{\partial G}{\partial F} = 1.$$
(16)

ii) In an MPE, neither K nor L earmarks any payment for the public good.

iii) Under commitment, L will never promise that payments will be earmarked for public goods, but K will if and only if

$$p < 1 - \frac{1 - \gamma}{\delta(1 - x_{\rm M})}.\tag{17}$$

In this case,

$$-\frac{\partial x_{\rm M}/\partial G}{\partial x_{\rm M}/\partial F} = \frac{1}{\gamma} \left[1 + \frac{\delta x_{\rm M}(1-p)}{1-\delta} \right]$$

$$\rightarrow \frac{1}{\gamma} \text{ if } x_{\rm M} \rightarrow 0.$$
(18)

The intuition for part i is already explained. Part ii follows because, from equation (6), $\partial x_i/\partial A_1 = -\partial x_t/\partial b = 1/c$ (fixing $v_p(x_s)$), which implies that the principals would be indifferent between earmarking and not earmarking at time *t* if $\gamma = 1$. When $\gamma < 1$, it will always be more efficient for a principal to pay the party in power at time *t*, rather than to subsidize something P_t values less.

Part iii of proposition 3 is nevertheless establishing that K might benefit from building a reputation for earmarking the payments for public good provision. A commitment to earmark future funds is more effective in reducing x_M than are payments to P_t if p is small while δ and γ are large. The intuition is that when p is small, P_t discounts the compensations to future parties in power, unless the compensations are valued even when

²⁰ For simplicity, it is assumed that the principals, including the domestic lobby, do not benefit directly from any of the transfers, even when they are earmarked for public good provision. After all, their values of land are likely to be much larger than their values of a (nother) public good.

 P_t is out of power. In contrast, a more stable political environment means that letting parties administer the funds can be more effective in reducing extraction. With $\delta = 0.85$ and $x_M \approx 0$, condition (17) requires $\gamma > 0.27$ when p = 1/7. If p = 1/2, condition (17) requires $\gamma > 0.58$.

In contrast, *L* would never want a reputation for such earmarks. If *L*'s payments were beneficial even when P_t is out of power, then P_t would value future exploitation more, and thus P_t would extract less at time *t*.

This preference of L's has two important implications. First, the efficient equilibrium outcome, in line with part i, cannot be expected, regardless of whether the principals can commit to earmark future payments. Second, K faces a time-inconsistency problem when K would like to commit to earmarks, because K is tempted to pay P_t directly at any given point in time (this follows from part ii). However, L faces no such time-inconsistency problem, because L prefers to pay the party in power directly, regardless of whether L can commit to earmark. This observation adds to the asymmetry between the two parties.

B. Paying the Lobby

Compensating short-lived presidents is expensive because K must compensate every one of them for not exploiting the resource. If the lobby is long-lived, then it can be less expensive to pay L to not lobby, since L appreciates that it can lobby or receive compensations also in the next period.

Let $q \in [0, 1]$ measure the probability that *L* will be the relevant lobby in any future period. With probability 1 - q, the current lobby is replaced by another identical group. To treat *L* and *K* more or less symmetrically, the reader is free to restrict attention to q = 1, as has been done so far. Alternatively, the lobby and the party in power will be more similar if q = p. If q > p, the lobby is more likely to be a player in the future than is the political party in power.

There are several ways of modeling transfers between the principals.²¹ Here, I consider the possibility that *K* pays *L* an amount $m_t \ge 0$ per unit that is actually conserved. Donor *K* sets m_t at the beginning of period *t*, before *K* and *L* simultaneously set k_t and l_t and before P_t sets x_t . With $m_t \ge 0$, *L*'s net value from exploitation is reduced, and thus *L* finds it optimal to reduce l_t . The reduced l_t allows *K* to reduce k_t without facing a larger x_t . Whether it is beneficial for *K* to pay *L*, instead of P_t , boils down to a comparison between *q* and *p*. After all, the value of conservation

²¹ Because both *K* and *L* pay P_t , the two principals can benefit from colluding and reducing both payments (without affecting x_t). To abstract for this trivial (and standard) collusion benefit, I consider the case in which *K*'s payment to *L* cannot be contingent on l_t (because, for instance, l_t is unverifiable).

includes the possibility of receiving compensations also in later periods. The extent to which the future compensations are valued hinges on the probability of being in power.

PROPOSITION 4. i) At any time *t*, *K* is indifferent between increasing m_t and increasing k_t .

ii) Suppose that $k_M > 0$ and $l_M > 0$. Then, *K* benefits from a commitment to compensate *L* rather than P_t for conservation if and only if

 $q \ge p$.

iii) Suppose that $k_M^B > 0$ and $l_M > 0$. Then, *K* benefits from a commitment to compensate *L* for conservation, rather than to earmark the payment for public goods, if and only if

$$q \ge 1 - \frac{1 - \{(1 - \delta)/[1 - \delta + \delta x_{\rm M}(1 - p)]\}\gamma}{\delta + \delta x_{\rm M}(\{\gamma/[1 - \delta + \delta x_{\rm M}(1 - p)]\} - 1)}$$

$$\rightarrow 1 - \frac{1 - \gamma}{\delta} \text{ when } x_{\rm M} \rightarrow 0.$$
(19)

iv) When $m_{\rm M} > 0$ and $l_{\rm M} > 0$,

$$-\frac{dx_{\rm M}/dG}{dx_{\rm M}/dF} = \frac{1-\delta(1-x_{\rm M})-\delta qx_{\rm M}}{[1-\delta(1-x_{\rm M})(1-q)](1-\delta)} \in \left[1,\frac{1}{1-\delta}\right]$$
$$\rightarrow \frac{1}{1-\delta(1-q)} \text{ when } x_{\rm M} \rightarrow 0, \quad \text{and}$$
$$-\frac{dx_{\rm M}/dG}{dx_{\rm M}/dF} \rightarrow 1 \text{ when } q \rightarrow 1.$$

Part i implies that the choice of m_t is not important to K in the short run, if K cannot commit. If K raises m_t by a marginal unit, l_t declines by a marginal unit, and K finds it optimal to reduce k_t by a marginal unit. Both x_t and K's payoff are unchanged. (However, L is better off, and P_t is worse off.)

Part ii considers the case where *K* prefers to commit to paying P_i rather than to earmark future payments for public good provision, that is, when condition (17) fails. If q > p, *K* strictly prefers to commit to paying *L* instead of P_i . As mentioned above, the intuition for this result is that the future compensations are appreciated the most by the party that is more likely to stay in power.

Part iii is relevant for the situation in which K would rather earmark the compensation for public good provision than pay P_t directly, that is, when condition (17) holds. Also in this case, a large q makes it preferable to compensate L, especially if γ is relatively small. Parts ii and iii of proposition 4 are illustrated in figure 2, together with condition (17), from proposition 3.

Part is shows that even when *K* pays *L*, the influence of *G* on x_M is larger than the influence of *F*, unless $q \rightarrow 1$.

VI. Extensions

A. Alternative Strategies for the Policy Maker

The party in power, P_b loses when future extraction levels are expected to be high. The future extraction levels depend on the parameters of the model. Although I have simplified by not considering changes in the parameters over time, it is straightforward to allow for parameters A_0 , A_1 , Δ , and b that are fixed in all future periods, even though they are different from the parameters that apply at time t. For any fixed A_p , P_t does not benefit directly from a future increase in A_0 or a decrease in A_1 or Δ , but P_t benefits indirectly because any of these changes will reduce the equilibrium x_M , according to equation (8). If the future b is larger, P_t benefits both directly and indirectly (i.e., because future extraction levels will be lower).

COROLLARY 1. Fix A_p . Then, P_t benefits if future Δ or A_1 decreases while A_0 or *b* increases.



FIG. 2.—It is most effective to pay P_i if p is large, pay L if q is large, and otherwise earmark the funds for public goods. The figure assumes that $x_{M} \approx 0$.

This corollary is important when P_t can influence future parameter values. In reality, powerful executives may have available several policy instruments.

For instance, if P_t signs a trade agreement, the payoff from extracting the resource can increase. The agreement may be desirable in a society where the additional value benefit everyone (as when A_0 increases). If the export revenues mostly benefit the party in power, however, the agreement will be undesirable because it will raise the multiplier and thus future extraction levels.

Traditional trade agreements are likely to raise equilibrium exploitation rates. If tariffs are contingent on forest cover, however, the agreement can be designed so as to motivate conservation (Harstad 2023a, 2023b). Such a contingent trade agreement will be especially desirable when the equilibrium extraction rates are high because of the multiplier, political instability, or corruption.

The party in power might also be able to raise the net benefit from conservation by investing in enforcement and monitoring technology, such as satellites. If the cost of conservation declines and the net conservation benefit increases, future parties will be induced to conserve more. The larger is the multiplier, the larger is the strategic incentive to invest in technologies that tie the hands of future policy makers.

When these investments are costly, the party in power may not be willing to pay very much. After all, when p < 1, it is tempting to postpone any expenditure to the next government. To mitigate this effect, and motivate P_{t+1} to invest more, P_t benefits from investing in an "upstream technology" that induces P_{t+1} to invest more in conservation technology. In Harstad (2020), I consider a hierarchy of technologies, where the cost of investing in one technology is influenced by another technology, farther upstream. The optimal investment subsidy depends on technological complementarities and the autocorrelation in the p's that arises with incumbency advantages.

B. Alternative Strategies for the Stakeholders

Stakeholders also influence politics in multiple ways. Even when the stakeholders do not pay parties directly, it is important to note that *K* benefits from a reduction in x_M and that *L* benefits from an increase in x_M . From equation (8), we learn that x_M increases in Δ and A_1 and decreases in A_0 , *b*, *c*, and *p*. These facts can be combined.

COROLLARY 2. Donor K loses, and L benefits, if Δ or A_1 increases while A_0 , b, c, or p decreases.

This simple observation can have important implications. As explained in section II, the difference $\Delta = A_1 - A_0$ may be related to the degree of polarization, since it can measure how valuable it is to spend

revenues on one's own party's perks, rather than on the opponent's perks. The ability to divert state revenues to perks can depend on the level of discretion, and corruption, in the country. The corollary implies that K, benefiting from conservation, prefers less polarization, discretion, and corruption. The proexploitation lobby, L, benefits from more polarization, discretion, and corruption. It is not implausible that certain stakeholders, such as an agricultural lobby, are able to work along with other forces that contribute to domestic polarization.

If *K* represents a foreign country, it may also be possible for *K* to reduce P_t 's export revenue by imposing boycotts or tariffs on forest-related products. These strategies of *K*'s may contribute to a lowered A_1 .

The corollary also states that K benefits from a stable political regime, in which p is large, while L benefits from the instability associated with a lower p. Once again, it may not be implausible that domestic groups can contribute to the relevant forces, also when it comes to influencing the stability of the political regime. Even foreign countries can take actions that affect the electoral outcomes in other countries, as analyzed by Antràs and Padró i Miquel (2011).

The benefit b may be associated with biodiversity and the extent to which the remaining forest is virgin or intact. A diminished quality of the forest induces the parties in power to conserve less. This situation is beneficial for L. The contributor K, in contrast, benefits from an increase in b. Parameter b may be larger if the rulers are more aware of the benefits associated with biodiversity. An information campaign, raising this awareness, can thus be beneficial for K.

C. Heterogeneous Political Parties

The above analysis is simple thanks to the assumption that all parties extract the same fraction once in office. With heterogeneous parties, the main results are strengthened and additional insights emerge.

Suppose there are two parties, D and R. The two are endowed with partyspecific values of extraction (A_i) , conservation (B_i) , extraction cost (c_i) , discount factor (δ_i) , or probability of being in power later (p_i) .

To isolate and emphasize the effects of heterogeneity, start with the case in which $\Delta = 0$. With $\Delta = 0$, party $i \in \{D, R\}$ prefers the same stationary extraction level, whether or not *i* is in office:

$$x_{i,*} = \sqrt{\left(\frac{1-\delta_i}{\delta_i}\right)^2 + 2\frac{A_i - B_i}{c_i}\left(\frac{1-\delta_i}{\delta_i}\right) - \frac{1-\delta_i}{\delta_i}}.$$
 (20)

Party *i*'s preferred extraction level $x_{i,*}$ maximizes *i*'s continuation value. That is, *i* would extract $x_{i,*}$ if $p_i = 1$ or if the opponent were expected to extract $x_{i,*}$. However, when $p_i < 1$ and *i* anticipates that $x_{j,M} \neq x_{i,*}$,

 $j = \{D, R\} \setminus i$, then *i* expects *j* to mismanage the resource when *j* will be in power. Consequently, *i*'s continuation value declines, and *i*'s extraction level at time *t*, $x_{i,p}$ is larger.

Intuitively, this reasoning holds whether $x_{j,M} > x_{i,*}$ or $x_{j,M} < x_{i,*}$. In the former case, *i* expects that *j* will extract too much in the future, and thus *i* finds it less valuable to conserve when *i* is in power, exactly as in section III. In the latter case, when $x_{j,M} < x_{i,*}$, *i* expects that *j* will conserve too much. Also this type of mismanagement induces *i* to extract more.

PROPOSITION 5. i) For $i \in \{D, R\} \setminus j$, in power at t, $x_{i,t}$ is U-shaped in $x_{j,s}$ and minimized at $x_i = x_{i,*}$ when $x_{j,s} = x_{i,*}$.

ii) For each $i \in \{D, R\}$, $x_i > x_{i,*}$ if and only if $x_{i,*} \neq x_{i,*}$ and $p_i < 1$.

Part i is illustrated in figure 3: $x_{D,t}$ is drawn as a best-response function of $x_{R,s}$, and $x_{R,t}$ is drawn as a best-response function of $x_{D,s}$. The intersection between the two pins down the MPE.

Part ii confirms that every party extracts more than it would have done without political rotation. It is the concern about future mismanagement that motivates *i* to extract more than $x_{i,*}$.

Numerical illustration.—Table 2 illustrates how equilibrium extraction rates, (x_D, x_R) vary with $x_{R,*}$ and p_R , letting $x_{D,*} = 0$ and $p_D = 1 - p_R$. As justified in section III.F, $\delta = 0.85$. A party's equilibrium extraction rate,



FIG. 3.—When the parties are heterogeneous and the best-response curves cross, both extraction rates are higher than the parties' bliss points.

compared to its ideal point, is larger if it is less likely to stay in power in the future and if the two bliss points differ a lot. For example, if $x_{R,*} = 0.3$ and $p_R = 1/2$, D finds it optimal to extract 8% when in power; R finds it optimal to extract 33%. If p_R increases, D extracts more when D is in power, while R extracts less when R is in power.

A corollary to proposition 5 is that the multiplier is different for the two parties and that it can be negative. Suppose, without loss of generality, that $x_{D,*} < x_{R,*}$. If $x_{R,s} > x_{D,*}$ increases, $x_{D,M}$ increases. If $x_{D,*} < x_{R,*}$ increases, in contrast, $x_{R,*}$ decreases, because R's continuation value increases when D's extraction rate is closer to R's bliss point. Therefore, a given stationary compensation level to D, in return for conservation, can be counterproductive.

Even though the stationary compensation level to D (denoted $k_{D,s}$) and to R (denoted $k_{R,s}$) have both been assumed to be zero in this section, it is straightforward to consider a marginal increase in these levels.

COROLLARY 3. If $k_{R,s}$ increases, both $x_{D,s}$ and $x_{R,s}$ decrease. If $k_{D,s}$ increases, $x_{D,s}$ decreases, but $x_{R,s}$ increases.

If the increase in compensation is substantial (rather than marginal), then, at some point, D will find that even R conserves too much, from D's point of view. In this situation, each party is paid by *K* to conserve and ends up conserving more than what the opponent would like it to do. (Even in sec. III, where parties were homogenous, eq. (12) showed that $\partial x_i/\partial x_s < 0$ when $k_c > \Delta$.)

If Δ is large, we return to the finding that each party extracts more than the other party would like it to do. With both $\Delta > 0$ and heterogeneous parties, the effects of payments for versus payments against resource extraction become more nuanced. The principals may want to build a reputation for supporting this or that party, depending on both Δ and the level of heterogeneity.

To complicate the situation further, it is reasonable that p_i is endogenous when the parties are heterogeneous. With homogenous parties, voters were indifferent at the election booth, and thus the probability of being in office was likely to depend on forces that are absent in the present model. With heterogeneous parties, voters will not be indifferent. The popularity of a specific party may also be influenced by actions and payments made by the stakeholders or by how an international treaty is designed (Battaglini and Harstad 2020). The interaction between heterogeneity, elections, and lobbying raises a host of new questions that may inspire new research.

VII. Concluding Remarks

This paper provides a positive theory for the game between consecutive governments when each of them decides whether to exploit or conserve a resource, such as a tropical forest. Because the current decision depends on expected future policies, parameter changes have a multiplier effect. The framework is employed to show how a lobby, eager to exploit, can take advantage of the multiplier. A donor, interested in conservation, can also benefit from the multiplier, but the asymmetry between paying once for exploitation and paying forever for conservation leads to an inefficient outcome.

The framework can be applied to alternative contexts. In particular, the predictions are consistent with recent developments in Brazil. Because of this consistency, the normative policy implications may be of relevance. First, payments contingent on conservation can have dramatically large effects because of the multiplier. Second, the anticipation of future payments, and the trust that they will continue to be offered, may have larger effects than the contemporary effects of current payments. It is thus essential to build credibility that payments will continue. Third, it is tempting for the donor to offer funds that can be used at the discretion of the president, but it may be more effective to build a reputation for earmarking the funds for public goods, beneficial also for parties no longer in power. Finally, if the lobby, willing to pay for exploitation, is more of a longrun player than is the current political party in power, then cost-effective conservation requires the donor to compensate the lobby rather than the government.

Throughout the paper, I have left behind several loose ends and open questions. The model is simple, the calibration preliminary, and the evidence scarce. My primary goal has been to inspire new research on this topic so that we can learn how the multiplier can be exploited to motivate conservation rather than depletion.

Appendix

Notation.—To facilitate the extensions, the proofs permit the per-period benefit from conservation to be b_1 for the party in power, b_0 for a party not in power, and $b_p \equiv (1 - p)b_0 + pb_1$. I also define $Z_p \equiv A_p - b_p$ and $\Delta \equiv Z_1 - Z_0$, so that $Z_1 - Z_p = Z_1 - [(1 - p)Z_0 + pZ_1] = (1 - p)\Delta$.

A. Proof of Proposition 1

With stationary x_n , P_t 's per-unit continuation value at any $\tau > t$ is similar to equation (2):

$$v_p(x_s) = \frac{x_s Z_p + b_p - x_s^2 c/2}{1 - \delta(1 - x_s)},$$
(A1)

and the FOC with respect to (w.r.t.) x_b following equation (3), becomes (similar to eq. [4]):

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$$x_{t} = \frac{Z_{1} - \delta v_{p}(x_{s})}{c} = \frac{1}{c} \left[Z_{1} - \delta \frac{b_{p} + Z_{p}x_{s} - x_{s}^{2}c/2}{1 - \delta(1 - x_{s})} \right].$$
 (A2)

Note that the second-order condition holds. Thus,

$$\frac{dx_{i}}{dx_{s}} = -\frac{\delta}{c} v'_{p}(x_{s}), \quad \text{where} \tag{A3}$$

$$v'_{p}(x_{s}) = \frac{\left(Z_{p} - cx_{s}\right)\left[1 - \delta(1 - x_{s})\right] - \delta\left(b_{p} + Z_{p}x_{s} - x_{s}^{2}c/2\right)}{\left[1 - \delta(1 - x_{s})\right]^{2}} \tag{A4}$$

$$= \frac{-\delta cx_{s}^{2}/2 - (1 - \delta)cx_{s} + Z_{p}\left[1 - \delta(1 - x_{s})\right] - \delta\left(b_{p} + Z_{p}x_{s}\right)}{\left[1 - \delta(1 - x_{s})\right]^{2}}.$$

With the fixed point $x_t = x_s$, equation (A2) gives

$$[1 - \delta(1 - x_s)]cx_s = Z_1[1 - \delta(1 - x_s)] - \delta(b_p + Z_p x_s - x_s^2 c/2) \Leftrightarrow$$

$$\delta c x_s^2/2 + [(1 - \delta)c - \delta(Z_1 - Z_p)]x_s + \delta b_p - (1 - \delta)Z_1 = 0 \Leftrightarrow$$

$$x_s = -\frac{(1 - \delta)c - \delta(1 - p)\Delta}{\delta c}$$
(A5)

$$\frac{\delta c}{\pm \frac{1}{\delta c}} \sqrt{\left[(1-\delta)c - \delta(1-p)\Delta\right]^2 - 4\frac{\delta c}{2}\left[\delta b_p - (1-\delta)Z_1\right]}$$

$$= \frac{(1-p)\Delta}{c} - \frac{1-\delta}{\delta} \pm \sqrt{\left(\frac{1-p}{c}\Delta - \frac{1-\delta}{\delta}\right)^2 + \frac{2}{c}\left(\frac{1-\delta}{\delta}Z_1 - b_p\right)}.$$
(A6)

The assumption that some extraction is optimal requires $[(1 - \delta)/\delta]Z_1 > b_p$. When we require $x_s \ge 0$, equation (A6) permits exactly one stationary MPE, equation (8).

Note that if $(1 - p)\Delta = 0$, then $x_M = x_1$, where $x_1 = x_p$, given by equation (7) when p = 1. However, $x_M > x_1$ if $(1 - p)\Delta > 0$, and x_M increases in $(1 - p)\Delta$, because

$$\frac{dx_{\rm M}}{d[(1-p)\Delta]} = \frac{1}{c} \left(1 - \frac{(1-\delta)/\delta - (1-p)\Delta/c}{\sqrt{[(1-\delta)/\delta - (1-p)\Delta/c]^2 + (2/c)\{[(1-\delta)/\delta]Z_1 - b_p\}}} \right),$$

which is strictly positive, given the assumption that $[(1 - \delta)/\delta]Z_1 > b_p$.

When equation (A5) is substituted into equations (A3)-(A4), we get

$$\frac{dx_{i}}{dx_{s}} = \frac{\delta}{c} \frac{\delta(Z_{1} - Z_{p})x_{s} - \delta b_{p} + (1 - \delta)Z_{1} - Z_{p}[1 - \delta(1 - x_{s})] + \delta(b_{p} + Z_{p}x_{s})}{[1 - \delta(1 - x_{s})]^{2}}
= \frac{\delta}{c} \frac{Z_{1} - Z_{p}}{1 - \delta(1 - x_{s})}
= \frac{\delta}{c} \frac{(1 - p)\Delta}{1 - \delta(1 - x_{s})}.$$
(A7)

For comparative statics, we get from equation (A2) that for any parameter $I \in \{A_1, A_2, b_1, b_2, c, p, \delta\}$,

$$\frac{dx_t}{dI} = \frac{\partial x_t}{\partial I} + \frac{\partial x_t}{\partial x_{\rm s}} \frac{dx_{\rm s}}{dI}.$$

So, when $x_t = x_s$,

$$\frac{dx_t}{dI} = \left(\frac{1}{1 - \partial x_t / \partial x_s}\right) \frac{\partial x_t}{\partial I} = \left(1 + \frac{\partial x_t / \partial x_s}{1 - \partial x_t / \partial x_s}\right) \frac{\partial x_t}{\partial I} \\ = \left[1 + \frac{(1 - p)\Delta}{(1 - \delta + \delta x_s)c/\delta - (1 - p)\Delta}\right] \frac{\partial x_t}{\partial I}.$$

QED

B. Proof of Lemma 2

The effect of compensation.—Donor *K* pays $(1 - x_t)S_tk_t$ to P_t at the end of period *t*. Let $\lambda_K > 0$ measure the party's valuation of each k_t . (In sec. III, $\lambda_K = 1$.) Now P_t 's per-unit continuation value can be written as

$$Z_{1}x_{t} + b_{1} + \lambda_{K}(1 - x_{t})k_{t} - cx_{t}^{2}/2 + (1 - x_{t})\delta v(x_{s}), \text{ where}$$
$$v(x_{s}) = \frac{Z_{p}x_{s} + b_{p} + \lambda_{K}p(1 - x_{s})k_{s} - x_{s}^{2}c/2}{1 - \delta(1 - x_{s})}.$$

The FOC w.r.t. x_t becomes

$$x_{t} = \frac{1}{c} \left[Z_{1} - \lambda_{K} k_{s} - \delta \frac{Z_{p} x_{s} + b_{p} + p \lambda_{K} (1 - x_{s}) k_{s} - x_{s}^{2} c/2}{1 - \delta (1 - x_{s})} \right].$$
 (A8)

The second-order condition holds, as before. Thus, the effect of k_t at time t is

$$\frac{dx_t}{dk_t} = -\frac{\lambda_K}{c}.$$
 (A9)

The effect of an anticipated increase in stationary $k_t = k_s$ is

$$\frac{dx_{t}}{dk_{s}} = \frac{\partial x_{t}}{\partial k_{s}} + \frac{\partial x_{t}}{\partial x_{s}} \frac{dx_{s}}{dk_{s}} = \frac{\partial x_{t}}{\partial k_{s}} \frac{1}{1 - \partial x_{t}/\partial x_{s}}, \quad \text{where}$$
(A10)
$$\frac{\partial x_{t}}{\partial k_{s}} = -\frac{\lambda_{K}}{c} \left[1 + \delta p \frac{1 - x_{s}}{1 - \delta(1 - x_{s})} \right] = -\frac{\lambda_{K}}{c} \frac{1 - \delta(1 - x_{s}) + \delta p - \delta p x_{s}}{1 - \delta(1 - x_{s})} = -\frac{\lambda_{K}}{c} \left[1 + \delta p \frac{1 - x_{s}}{1 - \delta(1 - x_{s})} \right].$$
(A10)

Regarding $\partial x_t / \partial x_s$, we can draw on equation (A7). With $k_s > 0$, equation (A8) can be written as equation (A2) if Z_1 and b_1 in equation (A2) are replaced by $\tilde{Z}_1 :=$ $Z_1 - \lambda_K k_s$ and $b_1^{-} := b_1 + \lambda_K k_s$ (and similarly for Z_p and b_p). With this, equation (A7) gives

$$\frac{\partial x_t}{\partial x_s} = \frac{\delta}{c} \frac{\tilde{Z}_1 - \tilde{Z}_p}{1 - \delta(1 - x_s)} = \frac{\delta}{c} \frac{(1 - p)(\tilde{Z}_1 - \tilde{Z}_0)}{1 - \delta(1 - x_s)} = \frac{\delta}{c} \frac{(1 - p)(\Delta - \lambda_K k_s)}{1 - \delta(1 - x_s)}.$$
 (A12)

K's problem.—Donor K's continuation value can be written as

$$V^{K}(S_{t}) = -fx_{t}S_{t} - \delta \frac{f}{1-\delta} x_{t}S_{t} - (1-x_{t})S_{t}k_{t} + \delta V^{K}(S_{t+1})$$

With future stationary k_s and x_s , we can write $V^K(S_t) = v^K S_t$, where the continuation value per unit of resource can be written as

$$v^{\kappa} = -Fx_{s} - k_{s}(1 - x_{s}) + (1 - x_{s})\delta v^{\kappa}, \text{ where}$$

$$v^{\kappa} = -\frac{Fx_{s} + k_{s}(1 - x_{s})}{1 - \delta(1 - x_{s})} \text{ and } F = \frac{f}{1 - \delta},$$
(A13)

where *F* is the present-discounted loss for each unit that is vanished for all time. At *t*, the FOC w.r.t. k_t becomes

$$-(1-x_t) + (F-k_t+\delta v^K) \left(-\frac{dx_t}{dk_t}\right) = 0.$$
(A14)

The second-order condition holds, given equation (A9) and given that x_t decreases in k_t .

With Markov-perfect $k_t = k_s = k_M$ and $x_t = x_s = x_M$, equation (A14) becomes

$$-(1 - x_{\rm M}) + \left[F - k_{\rm M} - \delta \frac{Fx_{\rm s} + k_{\rm M}(1 - x_{\rm M})}{1 - \delta(1 - x_{\rm M})}\right] \left(-\frac{dx_t}{dk_t}\right) = 0 \Leftrightarrow$$

$$k_{\rm M}[\delta + (1 - \delta)] = F(1 - \delta) - (1 - x_{\rm M})[1 - \delta(1 - x_{\rm M})] / \left(-\frac{dx_t}{dk_t}\right).$$
(A15)

With equation (A9), $\lambda_{\kappa} = 1$, and the nonnegativity constraint, equation (A15), can be written as equation (10) in lemma 2.

With commitment.—Donor K prefers a stationary compensation level k_c that maximizes v^{K} , given by equation (A13) with $k_s = k_c$. The FOC w.r.t. k_c becomes

$$\frac{(F - k_{\rm c})[1 - \delta(1 - x_{\rm s})] - \delta[Fx_{\rm s} + k_{\rm c}(1 - x_{\rm s})]}{[1 - \delta(1 - x_{\rm s})]^2} \left(-\frac{dx_{\rm s}}{dk_{\rm c}}\right)$$
$$-\frac{1 - x_{\rm s}}{1 - \delta(1 - x_{\rm s})} = 0 \Leftrightarrow$$
$$k_{\rm c}[\delta + (1 - \delta)] = F(1 - \delta) - (1 - x_{\rm s})[1 - \delta(1 - x_{\rm s})] / \left(-\frac{dx_{\rm s}}{d_{\rm c}}\right)$$

With equations (A10)–(A12), $\lambda_{\kappa} = 1$, and nonnegativity constraints, we get equation (11). QED

C. Proof of Lemma 3

Let *G* measure *L*'s gain from each x_t , while l_t measures the payment to P_t , per unit of $x_t S_t$.

The effect of lobbying.—An anticipated stationary lobby contribution l_s to the party in power, in return for every unit of extraction, adds $\lambda_L l_s x_l S_t$ to P_t 's payoff, where $\lambda_L > 0$ measures the ruling party's marginal valuation of l_s paid per unit of extraction. (In sec. III, $\lambda_L = 1$.) Thus, a larger $\lambda_L l_s$ has the same effect as a larger A_1 .

The FOC w.r.t. x_t is thus given by equation (A2), as before, if just Z_1 and Z_p in equation (A2) are replaced by $\hat{Z}_1 \coloneqq Z_1 + \lambda_L l_s$ and $\hat{Z}_p \coloneqq Z_p + p \lambda_L^p l_s$. When this expression for x_t is differentiated, we get

$$\frac{dx_t}{dl_s} = \lambda_L \frac{dx_t}{dA_1} = \lambda_L \frac{\partial x_t / \partial A_1}{1 - \partial x_t / \partial x_s}, \quad \text{with}$$
(A16)

$$\frac{\partial x_i}{\partial A_1} = \frac{1}{c} \left[1 - \frac{\delta p x_s}{1 - \delta (1 - x_s)} \right] = \frac{1}{c} \frac{1 - \delta + \delta x_s (1 - p)}{1 - \delta + \delta x_s}.$$
(A17)

Here, $\partial x_t / \partial x_s$ follows from equation (A7) if just Z_1 and Z_p in equation (A2) are replaced by \hat{Z}_1 and \hat{Z}_p :

$$\frac{\partial x_i}{\partial x_{\rm s}} = \frac{\delta}{c} \frac{\hat{Z}_1 - \hat{Z}_p}{1 - \delta(1 - x_{\rm s})} = \frac{\delta}{c} \frac{(1 - p)(\Delta + \lambda_L l_{\rm s})}{1 - \delta(1 - x_{\rm s})}.$$

In contrast, an increase in only l_t , at t, does not influence future parameters or variables. So,

$$dx_t/dl_t = \partial x_t/\partial l_t = \lambda_L/c.$$
(A18)

L's problem.—Let $q \in [0, 1]$ be the probability that L at t is the relevant lobby also in any given later period. (Before sec. V.B, q = 1.) Anticipating stationary l_s and x_s in later periods, L's continuation value, per unit of S_p is

$$v^{L} = q(G - l_{s})x_{s} + \delta(1 - x_{s})v^{L}$$
, where $v^{L} = \frac{qx_{s}(G - l_{s})}{1 - \delta(1 - x_{s})}$. (A19)

At t, L's problem is

$$\max_{l_t} (G - l_t) x_t S_t + (1 - x_t) S_t \delta v_L.$$

With equation (A19), the FOC w.r.t. l_i is

$$-x_{t} + \left[G - l_{t} - \delta \frac{qx_{s}(G - l_{s})}{1 - \delta(1 - x_{s})}\right] \frac{dx_{t}}{dl_{t}} = 0.$$
(A20)

The second-order condition holds, given equation (A18).

With equations (A18) and (A20), the Markov-perfect $l_t = l_s = l_M$ satisfies

$$l_{\rm M} = G - \frac{1 - \delta(1 - x_{\rm M})}{1 - \delta[1 - x_{\rm M}(1 - q)]} x_{\rm M} / \frac{dx_t}{dl_t} = G - \frac{1 - \delta(1 - x_{\rm M})}{1 - \delta[1 - x_{\rm M}(1 - q)]} \frac{cx_{\rm M}}{\lambda_L}.$$
 (A21)

With $\lambda_L = 1$ and the nonnegativity constraint, we obtain equation (13).

With commitment. Let q = 1. (This part is relevant only in sec. IV, where q = 1.) Suppose that *L* sets a constant $l_s = l_c$ to maximize v^L , given by equation (A19). The FOC is

$$(G - l_{\rm c}) \frac{1 - \delta(1 - x_{\rm s}) - x_{\rm s}\delta}{\left[1 - \delta(1 - x_{\rm s})\right]^2} \frac{dx_{\rm s}}{dl_{\rm c}} - \frac{x_{\rm s}}{1 - \delta(1 - x_{\rm s})} = 0 \Leftrightarrow l_{\rm c}$$
$$= G - \frac{1 - \delta(1 - x_{\rm s})}{1 - \delta} \frac{x_{\rm s}}{dx_{\rm s}/dl_{\rm c}}.$$

With equations (A16)-(A17), we get equation (14). QED

D. Proof of Proposition 2

With both $k_s > 0$ and $l_s > 0$, P_t 's FOC is written as equation (A2) if Z_1 and b_1 in equation (A2) are replaced by $\tilde{Z}_1 \coloneqq Z_1 - \lambda_K k_s + \lambda_L l_s$ and $b_1 \simeq b_1 + \lambda_K k_s$. With $x_t = x_s$, the FOC can be written as $\Omega = 0$, where

$$\begin{split} \Omega &\coloneqq (cx_{\mathrm{s}} - Z_{\mathrm{l}} + \lambda_{\mathrm{K}}k_{\mathrm{s}} - \lambda_{\mathrm{L}}l_{\mathrm{s}})[1 - \delta(1 - x_{\mathrm{s}})] \\ &+ \delta(1 - p)b_{\mathrm{0}} + \delta p(b_{\mathrm{l}} + \lambda_{\mathrm{K}}k_{\mathrm{s}}) \\ &+ \delta(Z_{p} - p\lambda_{\mathrm{K}}^{P}k_{\mathrm{s}} + p\lambda_{\mathrm{L}}^{P}l_{\mathrm{s}})x_{\mathrm{s}} - \delta x_{\mathrm{s}}^{2}c/2. \end{split}$$

Furthermore, for k_s we use equation (A15), and for l_s we use equation (A21). With these substitutions, the FOC can be written as a function $\Omega(x_M, F, G) = 0$. We can derive

$$\begin{aligned} \frac{\partial\Omega}{\partial F}(x_{\rm M},F,G) &= \lambda_{\rm K}[1-\delta(1-x_{\rm M})+\delta p(1-x_{\rm M})]\frac{(1-\delta)}{\delta+(1-\delta)} \\ &= \lambda_{\rm K}(1-\delta)[1-\delta(1-x_{\rm M})(1-p)], \end{aligned} \tag{A22} \\ \frac{\partial\Omega}{\partial G}(x_{\rm M},F,G) &= -\lambda_{\rm L}[1-\delta(1-x_{\rm M})-\delta px_{\rm M}]. \end{aligned}$$

When we differentiate $\Omega(x_M, F, G) = 0$, we obtain

$$\frac{\partial \Omega(x_{\rm M}, F, G)}{\partial x_{\rm M}} dx_{\rm M} + \frac{\partial \Omega(x_{\rm M}, F, G)}{\partial F} dF = 0 \Leftrightarrow \frac{dx_{\rm M}}{dF} = -\frac{\partial \Omega(x_{\rm M}, F, G)/\partial F}{\partial \Omega(x_{\rm M}, F, G)/\partial x_{\rm M}},$$

$$\frac{\partial \Omega(x_{\rm M}, F, G)}{\partial x_{\rm M}} dx_{\rm M} + \frac{\partial \Omega(x_{\rm M}, F, G)}{\partial G} dG = 0 \Leftrightarrow \frac{dx_{\rm M}}{dG} = -\frac{\partial \Omega(x_{\rm M}, F, G)/\partial G}{\partial \Omega(x_{\rm M}, F, G)/\partial x_{\rm M}}, \text{ so (A23)}$$

$$\frac{dx_{\rm M}/dF}{dx_{\rm M}/dG} = \frac{\partial \Omega(x_{\rm M}, F, G)/\partial F}{\partial \Omega(x_{\rm M}, F, G)/\partial G}.$$

With equation (A22),

$$\begin{aligned} -\frac{\lambda_{K}}{\lambda_{L}}\frac{dx_{M}/dG}{dx_{M}/dF} &= \frac{1}{1-\delta}\frac{1-\delta(1-x_{M})-\delta px_{M}}{1-\delta(1-x_{M})(1-p)} \\ &= 1+\delta\frac{1-p}{1-\delta}\frac{1-\delta(1-x_{M})}{1-\delta(1-x_{M})+\delta p(1-x_{M})}. \end{aligned}$$

It is easy to check that this expression is between 1 and $1/(1 - \delta)$ and that it approaches $1/[1 - \delta(1 - p)]$ if $x_M \rightarrow 0$. QED

E. Proof of Proposition 3

Part i.—Suppose that *L*'s expense l_t^B adds $\gamma > 0$ to every party's marginal benefit from exploitation (e.g., by funding public good provision) and that *K*'s expense k_t^B adds γ to every party's marginal benefit from conservation. The FOCs for these expenses are, as before, given by equations (A21) and (A15), but the effects on $x_{\rm M}$ are different.

Here P_t 's FOC w.r.t. x_t is given by equation (A2), as before, if just every Z_p in equation (A2) is replaced by $\hat{Z}_p \coloneqq Z_p + \gamma(l_s^B - k_s^B)$, $p \in [0, 1]$, and b_p is replaced by $b + \gamma k_s^B$. With this, and $x_t = x_s$, the FOC can be written as $\Omega^B = 0$, where

$$\begin{split} \Omega^{\scriptscriptstyle B} &\equiv [cx_{\rm s} - Z_{\rm l} - \gamma(l_{\rm s}^{\scriptscriptstyle B} - k_{\rm s}^{\scriptscriptstyle B})][1 - \delta(1 - x_{\rm s})] \\ &+ \delta(b + \gamma k_{\rm s}^{\scriptscriptstyle B}) + \delta[Z_{\scriptscriptstyle p} + \gamma(l_{\rm s}^{\scriptscriptstyle B} - k_{\rm s}^{\scriptscriptstyle B})]x_{\rm s} - \delta x_{\rm s}^2 c/2. \end{split}$$

Furthermore, for k_s^B we substitute in with equation (A15), and for l_s^B we substitute in with equation (A21). With these substitutions, the FOC can be written as a function $\Omega^B(x_M, F, G) = 0$. We can derive

$$\frac{\partial \Omega^{B}}{\partial F}(x_{\rm M}, F, G) = \gamma [1 - \delta(1 - x_{\rm M}) + \delta - \delta x_{\rm M}](1 - \delta) = \gamma (1 - \delta),$$

$$\frac{\partial \Omega^{B}}{\partial G}(x_{\rm M}, F, G) = -\gamma [1 - \delta(1 - x_{\rm M}) - \delta x_{\rm M}] = -\gamma (1 - \delta).$$
(A24)

Because the derivation of equation (A23) holds as before, we obtain equation (16).

Part ii.—A contribution at t only does not influence future parameters. So,

$$dx_t/dl_t^B = \gamma/c$$
 and $dx_t/dk_t^B = -\gamma/c$.

When we compare with equations (A9) and (A18) when $\lambda_K = \lambda_L = 1$, it follows that *K* and *L* always set $l_t^B = k_t^B = 0$ in the MPE if they can pay the party in power.

Part iii.—Suppose that k_s and l_s are stationary payments to the party in power, while k_s^B and l_s^B are stationary funds for the public good, valued by $\gamma > 0$. The above reasoning implies that P_t 's FOC w.r.t. x_b when $x_t = x_s$, can be written as $\Omega^{B^+} = 0$, where

$$\Omega^{B^+} \equiv [cx_{\mathrm{s}} - Z_1 + \lambda_K k_{\mathrm{s}} - \lambda_L l_{\mathrm{s}} - \gamma (l_{\mathrm{s}}^B - k_{\mathrm{s}}^B)][1 - \delta(1 - x_{\mathrm{s}})] + \delta(1 - p)b_0$$

+ $\delta p(b_1 + \lambda_K k_{\mathrm{s}}) + \delta \gamma k_{\mathrm{s}}^B + \delta [Z_p - p\lambda_K^P k_{\mathrm{s}} + p\lambda_L^P l_{\mathrm{s}} + \gamma (l_{\mathrm{s}}^B - k_{\mathrm{s}}^B)]x_{\mathrm{s}} - \delta x_{\mathrm{s}}^2 c/2.$
(A25)

Note that

$$\partial \Omega^{B^{+}} / \partial l_{s} = -\lambda_{L} [1 - \delta(1 - x_{s}) - \delta p x_{s}], \qquad (A26)$$

$$\partial \Omega^{B^{+}} / \partial l_{s}^{B} = -\gamma [1 - \delta(1 - x_{s}) - \delta x_{s}] = -\gamma (1 - \delta), \qquad (A27)$$

$$\partial \Omega^{B^{+}} / \partial k_{s} = \lambda_{L} [1 - \delta(1 - x_{s}) + \delta p (1 - x_{s})] = \lambda_{L} [1 - \delta(1 - x_{s})(1 - p)], \qquad (A27)$$

$$\partial \Omega^{B^{+}} / \partial k_{s}^{B} = \gamma [1 - \delta(1 - x_{s}) + \delta(1 - x_{s})] = \gamma. \qquad (A28)$$

So, analogously to equation (A23),

$$\frac{dx_{\rm M}/dl_{\rm s}}{dx_{\rm M}/dl_{\rm s}^{\rm B}} = \frac{\partial\Omega^{\rm B+}/\partial l_{\rm s}}{\partial\Omega^{\rm B+}/\partial l_{\rm s}^{\rm B}} = \frac{\lambda_{\rm L}}{\gamma} \frac{1-\delta(1-x_{\rm s})-\delta px_{\rm s}}{1-\delta} = \frac{\lambda_{\rm L}}{\gamma} \left[1+\frac{\delta x_{\rm s}(1-p)}{1-\delta}\right],$$

which is larger than 1 when $\gamma < \lambda_L$. However,

$$\frac{-dx_{\rm M}/dk_{\rm s}}{-dx_{\rm M}/dk_{\rm s}^{\rm B}} = \frac{\partial\Omega^{\rm B+}/\partial k_{\rm s}}{\partial\Omega^{\rm B+}/\partial k_{\rm s}^{\rm B}} = \frac{\lambda_{\rm K}}{\gamma} [1 - \delta(1 - x_{\rm M})(1 - p)]$$

which is larger than 1 when condition (17) holds and $\lambda_{K} = 1$.

In this case, K would prefer that the funds be earmarked for public goods, while L would always prefer to pay the party in power. With equations (A15) and (A24),

$$\partial \Omega^{B^+} / \partial F = \gamma (1 - \delta). \tag{A29}$$

Regarding the relative influence of F and G, employing (A23) with (A29), (A26), and (A21),

$$-\frac{dx_{\rm M}/dG}{dx_{\rm M}/dF} = \frac{\lambda_L}{\gamma} \frac{1-\delta[1-x_{\rm M}(1-p)]}{1-\delta},$$

which can be written as equation (18) when $\lambda_L = 1$. QED

F. Proof of Proposition 4

Part i.—Suppose now that *L* is in power with probability *q* in any future period. At *t*, the lobby in power receives $(1 - x_s)m_tS_t$ from *K*. Then *L*'s continuation value per unit of S_n starting at any later period (before realizing whether or not *L* is in power), is

$$v^{L} = q[x_{s}(G - l_{s}) + (1 - x_{s})m_{s}] + (1 - x_{s})\delta v^{L} = q \frac{x_{s}(G - l_{s} - m_{s}) + m_{s}}{1 - (1 - x_{s})\delta}$$

Anticipating this, *L* maximizes at *t*:

$$\begin{aligned} x_t(G - l_t - m_t) + m_t + (1 - x_t)\delta v^L, & \text{so} \\ - x_t + \left[G - l_t - m_t - \delta q \frac{x_s(G - l_s - m_s) + m_s}{1 - (1 - x_s)\delta} \right] \frac{\partial x_t}{\partial l_t} &= 0. \end{aligned}$$

The second-order condition holds. Thus, if the one-period m_t increases by one unit, l_t decreases by one unit, and so does *K*'s optimal k_t (which follows from the FOC [A15] if just $F(1 - \delta)$ is replaced with $F(1 - \delta) - m_t$); *K*'s payoff and x_t stay unchanged. This implies that if *K* cannot commit, *K* is indifferent between paying P_t and *L*.

Part ii.—In a stationary equilibrium,

$$(G - l_{s} - m_{s}) \left[1 - \frac{\delta q x_{s}}{1 - (1 - x_{s})\delta} \right] = x_{s} \frac{c}{\lambda_{L}} + \frac{\delta q m_{s}}{1 - (1 - x_{s})\delta} \Leftrightarrow l_{s} = G - m_{s} - \frac{\delta q m_{s} + [1 - (1 - x_{s})\delta]x_{s}c/\lambda_{L}}{1 - [1 - x_{s}(1 - q)]\delta} \Rightarrow \frac{\partial l_{s}}{\partial m_{s}} = -1 - \frac{\delta q}{1 - [1 - x_{s}(1 - q)]\delta} = -\frac{1 - \delta(1 - x_{s})(1 - q)}{1 - \delta(1 - x_{s}) - \delta q x_{s}}.$$

When l_s is a function of m_s , Ω^{B+} , in equation (A25), can be written as a function of m_s . When $\partial \Omega^{B+} / \partial m_s = (\partial \Omega^{B+} / \partial l_s)(\partial l_s / \partial m_s)$,

$$\frac{\partial \Omega^{B+}}{\partial m_{s}} = \lambda_{L} [1 - \delta(1 - x_{s}) - \delta p x_{s}] \frac{1 - \delta(1 - x_{s})(1 - q)}{1 - \delta(1 - x_{s}) - \delta q x_{s}}$$

When we compare with equation (A27), $\partial \Omega^{B+} / \partial m_{s} \geq \partial \Omega^{B+} / \partial k_{s}$ when

$$[1 - \delta(1 - x_{s}) - \delta p x_{s}] \frac{1 - \delta(1 - x_{s})(1 - q)}{1 - \delta(1 - x_{s}) - \delta q x_{s}} \ge [1 - \delta(1 - x_{s})(1 - p)],$$

which holds with equality if p = q and strictly if p < q.

When we compare with equation (A28), $\partial \Omega^{B^+} / \partial m_s \geq \partial \Omega^{B^+} / \partial k_s^B$ when

$$[1-\delta(1-x_s)-\delta px_s]\frac{1-\delta(1-x_s)(1-q)}{1-\delta(1-x_s)-\delta qx_s}\geq \gamma,$$

which can be written as condition (19). If $x_s = 0$, this inequality simplifies to

$$1 - \delta(1 - q) \ge \gamma \Leftrightarrow q \ge 1 - (1 - \gamma)/\delta.$$

Part iv.-Moreover,

$$-\frac{dx_{\rm M}/dG}{dx_{\rm M}/dF} = \frac{(\partial\Omega^{B+}/\partial l_{\rm s})(\partial l_{\rm s}/\partial G)}{(-\partial\Omega^{B+}/\partial l_{\rm s})(\partial l_{\rm s}/\partial m_{\rm s})(\partial m_{\rm s}/\partial F)} = \frac{1-\delta(1-x_{\rm M})-\delta qx_{\rm M}}{[1-\delta(1-x_{\rm M})(1-q)](1-\delta)},$$

which is strictly decreasing in q and approaches 1 when $q \rightarrow 1$. QED

G. Proof of Proposition 5

Party *i*'s continuation value in any later period is the natural modification of equation (A1):

$$v_i = \frac{b_i + p_i x_i Z_i + (1 - p_i) x_j Z_i - p_i x_i^2 c_i / 2 - (1 - p_i) x_j^2 c_i / 2}{1 - \delta_i [1 - p_i x_i - (1 - p_i) x_j]}.$$

The FOC w.r.t. $x_{i,i}$ is thus a function of the anticipated future stationary x_i and x_j (subscript *s* omitted for simplicity):

$$c_{i}x_{i,t} = Z_{i} - \delta_{i}v_{i} = Z_{i} - \delta_{i}\frac{b_{i} + Z_{i}p_{i}x_{i} + (1 - p_{i})Z_{i}x_{j} - p_{i}x_{i}^{2}c_{i}/2 - (1 - p_{i})x_{j}^{2}c_{i}/2}{1 - \delta_{i}\left[1 - p_{i}x_{i} - (1 - p_{i})x_{j}\right]},$$

$$= \frac{Z_{i}(1 - \delta_{i}) - \delta_{i}b_{i} + \delta_{i}p_{i}x_{i}^{2}c_{i}/2 + \delta_{i}(1 - p_{i})x_{j}^{2}c_{i}/2}{1 - \delta_{i}\left[1 - p_{i}x_{i} - (1 - p_{i})x_{j}\right]}.$$
 (A30)

With $x_{i,t} = x_i$, equation (A30), together with the analogous FOC for x_j , gives a unique MPE outcome (x_i, x_j) . With $x_{i,t} = x_i$, we can also use equation (A30) to write x_i as a function of the future stationary x_j , anticipated by \dot{x} .

$$c_{i}x_{i}\left\{1-\delta_{i}\left[1-p_{i}x_{i}-(1-p_{i})x_{j}\right]\right\} = Z_{i}(1-\delta_{i})-\delta_{i}b_{i}+\delta p_{i}x_{i}^{2}c_{i}/2$$

+ $\delta_{i}(1-p_{i})x_{j}^{2}c_{i}/2 \Leftrightarrow p_{i}x_{i}^{2}/2 + x_{i}\left\{1/\delta_{i}-\left[1-(1-p_{i})x_{j}\right]\right\}$ (A31)
+ $[b_{i}-Z_{i}(1/\delta_{i}-1)]/c_{i}-(1-p_{i})x_{j}^{2}/2 = 0.$

Consequently, if $p_i = 1$, $x_i = x_{i,*}$, where $x_{i,*}$ satisfies

$$x_{i,*}^2/2 + x_{i,*}(1/\delta_i - 1) + [b_i - Z_i(1/\delta_i - 1)]/c_i = 0.$$
 (A32)

This is analogous to equation (A5), with solution equation (20). When we substitute equation (A32) into equation (A31), we can derive

$$p_i (x_i - x_{i,*})^2 / 2 + (x_i - x_{i,*}) [1/\delta_i - 1 + (1 - p_i)(x_j - x_{i,*}) + x_{i,*}] - (1 - p_i)(x_j - x_{i,*})^2 / 2 = 0,$$

with solution

$$\begin{aligned} x_i - x_{i,*} &= \frac{1}{p_i} \sqrt{\left[1/\delta_i - 1 + (1 - p_i)(x_j - x_{i,*}) + x_{i,*}\right]^2 + p_i(1 - p_i)(x_j - x_{i,*})^2} \\ &- \frac{1/\delta_i - 1 + (1 - p_i)(x_j - x_{i,*}) + x_{i,*}}{p_i}. \end{aligned}$$

Clearly, the right-hand side is U-shaped in x_i and minimized when $x_j = x_{i,*}$. The difference between x_i and $x_{i,*}$ is vanishing when $p_i \rightarrow 1$.

With the similar equation for x_j , we can solve for x_i and x_j , given $x_{i,*}$, $x_{j,*}$, and $\delta_i = \delta$. QED

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