# First-Principles Insights into the Relative Stability, Physical Properties, and Chemical Properties of $\mathrm{MoSe}_{2}$ 

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#### Abstract

A fascinating transition-metal dichalcogenide (TMDC) compound, $\mathrm{MoSe}_{2}$, has attracted a lot of interest in electrochemical, photocatalytic, and optoelectronic systems. However, detailed studies on the structural stability of the various $\mathrm{MoSe}_{2}$ polymorphs are still lacking. For the first time, the relative stability of 11 different $\mathrm{MoSe}_{2}$ polymorphs $\left(1 \mathrm{H}, 2 \mathrm{H}, 3 \mathrm{H}_{\mathrm{a}}, 3 \mathrm{H}_{\mathrm{b}}, 2 \mathrm{~T}\right.$, $4 \mathrm{~T}, 2 \mathrm{R}_{1}, 1 \mathrm{~T}_{1}, 1 \mathrm{~T}_{2}, 3 \mathrm{~T}$, and $2 \mathrm{R}_{2}$ ) is proposed, and a detailed analysis of these polymorphs is carried out by employing the firstprinciples calculations based on density functional theory (DFT). We computed the physical properties of the polymorphs such as band structure, phonon, and elastic constants to examine the viability for real-world applications. The electronic properties of  the involved polymorphs were calculated by employing the hybrid functional of Heyd, Scuseria, and Ernzerhof (HSE06). The energy band gap of the polymorphs ( $1 \mathrm{H}, 2 \mathrm{H}, 3 \mathrm{H}_{a}, 3 \mathrm{H}_{\mathrm{b}}, 2 \mathrm{~T}, 4 \mathrm{~T}$, and 2 R ) is in the range of $1.6-1.8 \mathrm{eV}$, coinciding with the experimental value for the polymorph 2 H . The covalent bonding nature of MoSe ${ }_{2}$ is analyzed from the charge density, charge transfer, and electron localization function. Among the 11 polymorphs, $1 \mathrm{H}, 2 \mathrm{H}, 2 \mathrm{~T}$, and $3 \mathrm{H}_{\mathrm{b}}$ polymorphs are predicted as stable polymorphs based on the calculation of the mechanical and dynamical properties. Even though the 4 T and $3 \mathrm{H}_{\mathrm{a}}$ polymorphs' phonons are stable, they are mechanically unstable; hence, they are considered to be under a metastable condition. Additionally, we computed the direction-dependent elastic moduli and isotropic factors for both mechanically and dynamically stable polymorphs. Stable polymorphs are analyzed spectroscopically using IR and Raman spectra. The thermal stability of the polymorphs is also studied.


## 1. INTRODUCTION

TMDCs are a novel luminaire building material that has recently gained much attention. ${ }^{1,2}$ A wide range of twodimensional and few-layered TMDCs have been created for a variety of applications including energy storage, catalysis, optoelectronics, and microelectronics. ${ }^{3}$ Especially, more than $90 \%$ of tumor cells were destroyed using phototherapy medications based on TMDC materials including $\mathrm{MoS}_{2}$, $\mathrm{WS}_{2}$, and $\mathrm{MoSe}_{2}$. Multiple polymorphs exist in TMDCs due to metal coordination and monolayer stacking order already reported by Donarelli et al. ${ }^{3,4}$ According to crystal symmetry, TMDCs naturally hold the T (tetragonal), H (hexagonal), and rare R (rhombohedral) phases. Layers of TMDCs have been adjusted according to several works in many different applications.

Among the TMDC materials that have been described earlier, $\mathrm{MoSe}_{2}$ (molybdenum diselenite) is one of the finest materials. It has a greater electrical conductivity than $\mathrm{MoS}_{2}$ when compared. ${ }^{5,6}$ For the bilayer, $\mathrm{MoSe}_{2}$ exhibits a direct band gap, which switches to an indirect band gap as the layers rise. ${ }^{7}$ When subjected to NIR (near infrared) laser light, $\mathrm{MoSe}_{2}$ has been explored as a nonphotothermal agent. Photothermal experiments have just recently been documented by Yuwen et
al. ${ }^{6}$ The resultant monolayer $\mathrm{MoSe}_{2}$ is used as a biosensor for detecting VOCs (volatile organic compounds) in lung cancer, especially when Al is doped with $\mathrm{MoSe}_{2}\left(\mathrm{AlMoSe}_{2}\right)$, which have already been reported by Liu et al. ${ }^{8} \mathrm{MoSe}_{2}$ materials can be used in both photodetectors and switchable transistors. $\mathrm{MoSe}_{2}$ is a novel material that can absorb gas molecules on its surfaces, assisting in the charge transfer process. The $\mathrm{MoSe}_{2}$ nanosheet is one of the best gas sensors, detecting $\mathrm{NO}_{2}$ even at ambient temperature, as Chen et al. described before. ${ }^{9,10}$ As previously stated, single-layer $\mathrm{MoSe}_{2}$ based on ammonia is used as a gas sensor. ${ }^{11}$ In a recent article, the N -doped carbon at $\mathrm{MoSe}_{2}$ core/branch nanostructure displayed outstanding lithium storability reported by Morales et al. ${ }^{12}$ A covalent bond between atomic layers create the usual structure of $\mathrm{MoSe}_{2}$, with a single Mo atomic layer sandwiched between two Se

[^0]

(a)


(c)

(e)

(f)

Figure 1. (a) Basic building blocks and (b) the planar view of the Mo-Se trigonal prismatic phase. (c) Stacking sequences of MoSe ${ }_{2}$ hexagonal polymorphs. (d) The basic building blocks and (e) the planar view of the $\mathrm{MoSe}_{2}$ octahedral prismatic phase. (f) Stacking sequences of $\mathrm{MoSe}_{2}$ trigonal polymorphs.


Figure 2. Total energy vs volume curve for (a) group A and (b) group B. Calculated total energy as a function of the volume of the unit cell for the different $\mathrm{MoSe}_{2}$ polymorphs.
atomic layers. ${ }^{13}$ The stacking sequence and/or layer spacing can be changed to modify the $\mathrm{MoSe}_{2}$ structure. ${ }^{14}$ Depending on the structure, different $\mathrm{MoSe}_{2}$ polymorphs can be created, although not all of them will be stable. A stability study is required before using polymorphs for a variety of applications.
In this study, to find the stability impact, we conducted indepth theoretical assessments on features for 11 different $\mathrm{MoSe}_{2}$ polymorphs using DFT calculations for the first time. ${ }^{15,16}$ Stability investigation was carried out beforehand by finding the low energies of all polymorphs, as well as coordinate configurations were found for various layers of $\mathrm{MoSe}_{2}$ polymorphs. ${ }^{17}$ The electronic characteristics of $\mathrm{MoSe}_{2}$ polymorphs are examined. From the electronic properties, we observed that seven polymorphs are semiconductors in nature and four polymorphs are metallic in nature. ${ }^{18}$ To investigate how the polymorphs bind, the charge density, charge transfer, and electron localization function are also estimated. The
phonon and mechanical properties of all 11 polymorphs are extensively investigated to predict the stable nature of each polymorph. Six polymorphs are dynamically stable, and the remaining five polymorphs are dynamically unstable. The novel IR and Raman spectra are estimated for stable structures, which are used for vibrational study and to characterize the structure of polymorphs. In addition, the thermal stability of the polymorphs was examined by the thermal characteristics of the polymorphs. The primary purpose of this research was to analyze the structural, mechanical, dynamic, and thermal stability of different $\mathrm{MoSe}_{2}$ polymorphs. From this development, novel stable polymorphs are found, which might be used in quite a lot of applications like energy storage, catalysis, optoelectronics, and microelectronics for future purposes.

Table 1. Unit Cell Constants and Coordinates for the Investigated MoSe ${ }_{2}$ Polymorphs, Space Group, and Material Project IDs Are Mentioned Near the Polymorphs, in Parentheses

| polymorph | unit cell constants ( $\AA$ ) | atom | site | $X$ | Y | Z |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $1 \mathrm{H}-\mathrm{MoSe}_{2}(P \overline{6} m 2 ; \mathrm{mp}-1023924)$ | $a=b=3.267, c=17.975$ | Mol | 1a | 0 | 0 | 0 |
|  |  | Sel | 2 i | 2/3 | 1/3 | 0.0920 |
| $2 \mathrm{H}-\mathrm{MoSe}_{2}\left(\mathrm{PG}_{3} / m m c ; \mathrm{mp}-1018809\right)$ | $a=b=3.269, c=13.857$ | Mol | 2b | 0 | 0 | 1/4 |
|  | $a=b=3.280, c=12.910^{22}$ | Sel | 4f | 2/3 | 1/3 | 0.3698 |
|  | $a=b=3.280, c=12.920^{24}$ |  |  |  |  |  |
|  | $a=b=3: 299, c=12.938{ }^{19}$ |  |  |  |  |  |
| $3 \mathrm{H}_{\mathrm{a}}-\mathrm{MoSe}_{2}(P \overline{6} m 2 ; \mathrm{mp}-1025874)$ | $a=b=3.267, c=36.342$ | Mo1 | 2 i | 2/3 | 1/3 | 0.7684 |
|  |  | Mo2 | 1c | 1/3 | $2 / 3$ | 0 |
|  |  | Sel | 2 i | 2/3 | 1/3 | 0.0458 |
|  |  | Se2 | 2h | 1/3 | 2/3 | 0.2773 |
|  |  | Se3 | 2h | 1/3 | 2/3 | 0.8139 |
| $3 \mathrm{H}_{\mathrm{b}}-\mathrm{MoSe}_{2}\left(\mathrm{P6}_{3} / m m c ; \mathrm{mp}-2815\right)$ | $a=b=3.268, c=13.425$ | Mol | 2d | 2/3 | 1/3 | 1/4 |
|  |  | Sel | 4f | 2/3 | 1/3 | 0.8737 |
| 2T-MoSe ${ }_{2}(P \overline{3} m 1 ; \mathrm{mp}$-1023939) | $a=b=3.268, c=22.471$ | Mol | 2b | 0 | 0 | 1/4 |
|  |  | Sel | 4f | 2/3 | 1/3 | 0.3698 |
| $4 \mathrm{~T}-\mathrm{MoSe}_{2}(P \overline{3} m 1 ; \mathrm{mp}-1027525)$ | $a=b=3.269, c=35.382$ | Mol | 2d | $2 / 3$ | 1/3 | 0.0935 |
|  |  | Mo2 | 2d | 2/3 | 1/3 | 0.7211 |
|  |  | Sel | 2d | 2/3 | $1 / 3$ | 0.3258 |
|  |  | Se 2 | 2d | 2/3 | 1/3 | 0.9535 |
|  |  | Se3 | 2d | 2/3 | 1/3 | 0.2317 |
|  |  | Se4 | 2d | 2/3 | 1/3 | 0.8590 |
| $2 \mathrm{R}_{1}-\mathrm{MoSe}_{2}(R \overline{3} m ;$ ICSD_31067; 1434) | $a=b=3.272, c=19.713$ | Mol | 1a | 0.9997 | 0.9997 | 0.9997 |
|  |  | Sel | 1a | 0.4175 | 0.4175 | 0.4175 |
|  |  | Se 2 | 1a | 0.2490 | 0.2490 | 0.2490 |
| $1 \mathrm{~T}_{1}-\mathrm{MoSe}_{2}(P \overline{3} m 1 ; \mathrm{mp}-147)$ | $a=b=3.326, c=15.451$ | Mol | 1a | 0 | 0 | 0 |
|  |  | Sel | 2d | 2/3 | 1/3 | 0.2667 |
| $1 \mathrm{~T}_{2}-\mathrm{MoSe}_{2}(P \overline{3} ; \mathrm{mp}-164)$ | $a=b=3.238, c=6.510$ | Mol | 1a |  | 0 | $0$ |
|  |  | Sel | 2d | 2/3 | 1/3 | $0.2652$ |
| $3 \mathrm{~T}-\mathrm{MoSe}_{2}(R \overline{3} m ; \mathrm{mp}-1558544)$ | $a=b=3.226, c=19.282$ | Mol | 1 b | 1/2 | 1/2 | 1/2 |
|  |  | Sel | 2c | 0.2561 | 0.2561 | 0.2561 |
| $2 \mathrm{R}_{2}-\mathrm{MoSe}_{2}(P 3 m 1 ; \mathrm{mp}-11238797)$ | $a=b=3.240, c=6.584$ | Mol | 1 b | 0 | 0 | 1/2 |
|  |  | Sel | 2d | 2/3 | 1/3 | 0.2383 |

## 2. RESULTS AND DISCUSSION

2.1. Structure and the Stability of $\mathrm{MoSe}_{2}$ Polymorphs. The Mo atom is sandwiched between two Se atoms ( $\mathrm{Se}-\mathrm{Mo}-\mathrm{Se}$ ) creating the $\mathrm{MoSe}_{2}$ structure. The intralayer of the $\mathrm{MoSe}_{2}$ structure will be two-dimensionally covalently bonded, whereas the interlayer will be weakly coupled due to the weak van der Waals-type forces. ${ }^{19} \mathrm{MoSe}_{2}$ featured many polymorphs depending on the layer stacks. ${ }^{20} \mathrm{~A}$ single layer of $\mathrm{MoSe}_{2}$ will have a trigonal prismatic phase with a hexagonal structure and an octahedral prismatic phase with a trigonal structure (Figure 1). In the octahedral prismatic phase, the metal atoms are octahedrally coordinated by six nearby Se atoms. In the trigonally prismatic phase, the metal atoms are trigonally coordinated by two nearby Se atoms. Variations in the stacking order and registry of succeeding $\mathrm{Se}-\mathrm{Mo}-\mathrm{Se}$ sandwiches of the hexagonal and trigonal structure along the $c$ axis give rise to several crystal polymorphs or polytypes in three dimensions (Figure 1). ${ }^{20}$ In this work, based on the trigonal prismatic phase and octahedral prismatic phase, 11 different polymorphs are formed $\left(1 \mathrm{H}-\mathrm{MoSe}_{2}, 2 \mathrm{H}-\mathrm{MoSe}_{2}, 1 \mathrm{H}_{\mathrm{a}}-\right.$ $\mathrm{MoSe}_{2}, 1 \mathrm{H}_{\mathrm{b}}-\mathrm{MoSe}_{2}, 2 \mathrm{~T}-\mathrm{MoSe}_{2}, 4 \mathrm{~T}-\mathrm{MoSe}_{2}, 2 \mathrm{R}_{1}-\mathrm{MoSe}_{2}, 1 \mathrm{~T}_{1^{-}}$ $\mathrm{MoSe}_{2}, 1 \mathrm{~T}_{2}-\mathrm{MoSe}_{2}, 3 \mathrm{~T}-\mathrm{MoSe}_{2}$, and $2 \mathrm{R}_{2}-\mathrm{MoSe}_{2}$ ). In this architecture, the integer defines the number of layers per unit cell along the $c$-axis. Trigonal, hexagonal, and rhombohedral structural symmetries are denoted by the letters T, H, and R, respectively. ${ }^{20-22}$

In this work, polymorphs are separated into two groups (group A and group B) based on the energies of the polymorphs. In group A, we observe that two polymorphs are trigonal, one polymorph is rhombohedral and the other four are hexagonal ( $1 \mathrm{H}-\mathrm{MoSe}_{2}, 2 \mathrm{H}-\mathrm{MoSe}_{2}, 1 \mathrm{H}_{\mathrm{a}}-\mathrm{MoSe}_{2}, 1 \mathrm{H}_{\mathrm{b}}-$ $\mathrm{MoSe}_{2}, 2 \mathrm{~T}-\mathrm{MoSe}_{2}, 4 \mathrm{~T}-\mathrm{MoSe}_{2}$, and $2 \mathrm{R}_{1}-\mathrm{MoSe}_{2}$ ). ${ }^{23}$ In group B , one of the polymorphs is rhombohedral, while three are trigonal structures $\left(1 \mathrm{~T}_{1}-\mathrm{MoSe}_{2}, 1 \mathrm{~T}_{2}-\mathrm{MoSe}_{2}, 3 \mathrm{~T}-\mathrm{MoSe}_{2}\right.$, and $\left.2 \mathrm{R}_{2}-\mathrm{MoSe}_{2}\right)$. The bonding length of $\mathrm{Mo}-\mathrm{Se}$ and the structure formation of all of the polymorphs are given in the Supporting Information on Page S2.

The relative stability of the polymorphs is investigated after structural optimization. In our simulation, the total energy of all polymorphs as a function of volume with varying ranges is noticed. ${ }^{18}$ From Figure 2a, all of the polymorphs in group A show that the energies are very close for different volume ranges, which confirms that $\mathrm{MoSe}_{2}$ can easily be found in any of these variants. Figure 2b shows that group B polymorphs have low energy between -19.33 and $-19.44 \mathrm{eV} /$ f.u., which is lower than that of group A. The low energy of group A and group B are given in Table S1 of the Supporting Information. The formation energy of group A is in the range of -2.13 to $-2.17 \mathrm{eV} / \mathrm{f} . \mathrm{u}$. and group B obtained -1.43 to $-1.5 \mathrm{eV} / \mathrm{f} . \mathrm{u}$. range of formation energy. The volume, the minimum energy, and the formation energy of all of the polymorphs are given in Table S1 of the Supporting Information on Page S1.


Figure 3. HSE06 band structure for group A (a) $1 \mathrm{H}-\mathrm{MoSe}_{2}$ and (b) $3 \mathrm{H}_{\mathrm{a}}-\mathrm{MoSe}_{2}$ with a direct band gap and (c) $2 \mathrm{H}-\mathrm{MoSe} \mathrm{e}_{2}$ and (d) $2 \mathrm{~T}-\mathrm{MoSe} \mathrm{e}_{2}$ with indirect band gap. The band structure of other polymorphs in group A is given in the Supporting Information. The Fermi level is set at zero energy and marked as $E_{\mathrm{F}}$.

The calculated positional and lattice constants of different polymorphs are given in Table 1. Experimental results ( $a=b=$ $3.288 \AA, c=12.900 \AA$ ) well coincide with the $2 \mathrm{H}-\mathrm{MoSe}_{2}$ polymorph, which has already been reported by Brixner et al. ${ }^{22}$ The lattice constant of $2 \mathrm{H}-\mathrm{MoSe}_{2}(a=b=3.269 \AA, c=13.857$ $\AA$ ) well coincided with the previous result ( $a=b=3.28 \AA, c=$ 12.91 Å) given by Silvestrelli and Ambrosetti. ${ }^{19,24}$
2.2. Electronic Structure. A detailed investigation of the electronic computations is performed for all computed $\mathrm{MoSe}_{2}$ polymorphs. We used HSE06 for the electronic calculation in our study instead of GGA, which gave us improved accuracy. Materials with semiconducting qualities can absorb visible light, although metals can be employed as conductors. In this case, HSE06 band gap calculations allow us to understand the polymorphs in group A as semiconductors and the group B polymorphs as metals. ${ }^{25}$

The conduction band minimum and valence band maximum of $1 \mathrm{H}-\mathrm{MoSe}_{2}$ and $3 \mathrm{H}_{\mathrm{a}}-\mathrm{MoSe}_{2}$ polymorphs occur at the same symmetric point $k$ in Figure 3a,b, indicating a direct band gap with a band gap value of $2 \mathrm{eV}^{26,27}$ Because of all of the conduction band minima along the $K-\Gamma$ path and valence band maxima positioned at the $\Gamma$ point, the $2 \mathrm{H}-\mathrm{MoSe}_{2}, 2 \mathrm{~T}$ $\mathrm{MoSe}_{2}, 4 \mathrm{~T}-\mathrm{MoSe}_{2}, 3 \mathrm{H}_{\mathrm{b}}-\mathrm{MoSe}_{2}$, and $2 \mathrm{R}_{1}-\mathrm{MoSe}_{2}$ polymorphs in group A have an indirect band gap. Figure 3c,d shows $2 \mathrm{H}-$
$\mathrm{MoSe}_{2}$ and 2T-MoSe ${ }_{2}$ with an indirect band gap, and other polymorphs of group A are given in Figure S1 of the Supporting Information on Page S3. ${ }^{28}$ The band gap value of 1.6 eV of $4 \mathrm{~T}-\mathrm{MoSe}_{2}$ is the same as the band gap value of the $3 \mathrm{H}_{\mathrm{b}}-\mathrm{MoSe}_{2}$ polymorph. All group A polymorphs displayed similar band topologies, but the number of bands increased as the number of layers increased; this shows that all polymorphs could easily transition into one another. The band gap value and band gap type of group A are given in Table S2 of the Supporting Information on Page S4. All of the polymorphs have band degeneracy, but $4 \mathrm{~T}-\mathrm{MoSe}_{2}$ polymorphs have the highest, resulting in a larger effective density of state. 2 H $\mathrm{MoSe}_{2}$ polymorphs show a nearer value of the 1.58 eV band gap value, which is reported early by Tang et al. ${ }^{29}$ The band gap value of $2 \mathrm{H}-\mathrm{MoSe}_{2}$ is well suited to the theoretically determined band gap value of 1.88 eV reported by Gupta et al. ${ }^{13}$ Additionally, the experimental value of the band gap ( 1.48 eV ) is compared with our $2 \mathrm{H}-\mathrm{MoSe}_{2}$ polymorphs that are already reported by Mahatha Patel et al. ${ }^{30}$ The valence band maximum and conduction band minimum are formed due to the Mo-4d and Se-3p states. Group A's band gap range makes it appropriate for photovoltaic solar cells, photocatalysis, and water-splitting applications.

Group B polymorphs have a metallic appearance due to the overlap of the conduction and valence bands in the band structure. ${ }^{27}$ Figure 4 shows the $3 \mathrm{~T}-\mathrm{MoSe}_{2}$ band structure, and


Figure 4. HSE06 band structure of $3 \mathrm{~T}-\mathrm{MoSe}_{2}$ showing a metallic appearance. The band structure of other polymorphs of group B is given in Figure S2 of the Supporting Information.
the other band structure of group B is given in Figure S2 of the Supporting Information on Page S4. Although all of the bands in group B had the same structure, the number of bands in 3T$\mathrm{MoSe}_{2}$ increased due to the increased layer thickness.

Surprisingly, all of the band structures in groups A and B have a flat band between $\Gamma$ and $A$. Because of the diminishing overlap between atomic wave functions, very confined orbitals or big unit cells with well-spaced atoms can readily give birth to common flat atomic bands (FABs). In multilayer and heavy
fermion systems, FABs are typical. The flatness of the band in the band structure is determined due to the interlayer spacing of the $\mathrm{MoSe}_{2}$. ${ }^{31-33}$
2.3. Bonding Nature. The projected valence-chargedensity distribution is used to describe bonding interactions in polymorphs. ${ }^{18,25}$ Because of the similar nature of all of the polymorphs, the charge density, charge transfer, and electron localization function (ELF) plots of the lowest energy of hexagonal and trigonal polymorphs are the same, as shown in Figure 5.

The $\mathrm{Se}-\mathrm{Mo}-\mathrm{Se}$ bonds are trigonally connected, as shown by the hexagonal polymorph's charge density in Figure 5a, demonstrating a normal covalent connection. Figure 5d shows a cross-shaped connection between the $\mathrm{Se}-\mathrm{Mo}-\mathrm{Se}$ trigonal polymorphs and conventional covalent bonding. ${ }^{34}$ The red color indicates that the cation-cation charge transfer is tightly constrained, whereas the yellow color indicates that the anion has a more diffuse location. ${ }^{35}$ These polymorphs have a covalent bond nature, as shown by the fact that both the cations and the anion share electrons (see Figure 5b,e).

Electron localization occurs between Se (like a cap) and Mo atoms in hexagonal and trigonal polymorph, as shown in Figure 5c,f, respectively, and is concentrated with an ELF value greater than 0.5 , implying the formation of covalent bonding between Mo and Se. ${ }^{36-38}$ Covalent bonding is apparent in all polymorphs.
2.4. Vibrational Study. The phonon is calculated for the investigated polymorphs to determine their dynamical stability, as well as the total PhDOS and phonon dispersion curves at the equilibrium volume, with the high symmetry direction of the Brillouin zone. ${ }^{39}$ Because of the increased forces in the polymorphs, an atom in the polymorphs is displaced from its equilibrium position, and evaluating the force associated with the system reveals the phonon frequency for a set of


Figure 5. (a, d) Charge density, (b, e) charge transfer, and (c, f) ELF for hexagonal (H) and trigonal polymorph (T), respectively.


Figure 6. Positive phonon dispersion and phonon density of states for (a) $1 \mathrm{H}-\mathrm{MoSe}_{2}$, (b) $2 \mathrm{H}-\mathrm{MoSe}_{2}$, (c) $3 \mathrm{H}_{\mathrm{b}}-\mathrm{MoSe}_{2}$, and (d) $2 \mathrm{~T}_{1}-\mathrm{MoSe}_{2}$ polymorphs in group A.


Figure 7. Phonon dispersion and phonon density of states for the 3 T-MoSe ${ }_{2}$ polymorph in group B. Phonon dispersion and phonon density of states for other polymorphs are given in Figure S4 of the Supporting Information. All of the polymorphs in group B hold negative frequencies, which means that they are dynamically unstable.
displacements. ${ }^{40}$ In general, all phonons have a genuine and positive frequency; here, six of the seven polymorphs in group A ( $1 \mathrm{H}-\mathrm{MoSe}_{2}, 2 \mathrm{H}-\mathrm{MoSe}_{2}, 2 \mathrm{~T}-\mathrm{MoSe}_{2}, 4 \mathrm{~T}-\mathrm{MoSe}_{2}$, and $3 \mathrm{H}_{\mathrm{b}}-$ $\mathrm{MoSe}_{2}$ ) show positive mode in our investigation, indicating that they are dynamically stable. The other group A polymorph $2 \mathrm{R}_{1}-\mathrm{MoSe}_{2}$ exhibits a negative/soft mode of frequencies or a negative eigenvalue, suggesting that they are dynamically unstable. ${ }^{41}$ Figure 6 shows positive phonon dispersion and phonon density of states for $1 \mathrm{H}-\mathrm{MoSe}_{2}, 2 \mathrm{H}-\mathrm{MoSe}_{2}, 3 \mathrm{H}_{\mathrm{b}}-$ $\mathrm{MoSe}_{2}$, and $2 \mathrm{~T}_{1}-\mathrm{MoSe}_{2}$ polymorphs. Phonon dispersion and phonon density of states of the other polymorphs in group A are given in Figure S3 of the Supporting Information on Page S5.

Phonon dispersions of dynamically stable polymorphs are divided into two branches: optical (upper branch) and acoustical (lower branch). Atoms in the optical branch move in different directions, but atoms in the acoustic branch displace in the same direction with the same amplitude and phase. Relating it to other polymorphs, $2 \mathrm{H}-\mathrm{MoSe}_{2}$ owned a high-frequency range of acoustic and optical modes in the region of 6 and 13 THz , respectively. Surprisingly, as shown in Figure 6, the wave vectors in phonon dispersion of the 1 H $\mathrm{MoSe}_{2}, 3 \mathrm{H}_{\mathrm{b}}-\mathrm{MoSe}_{2}$, and $2 \mathrm{~T}-\mathrm{MoSe}_{2}$ polymorphs in group A were comparable, proving that temperature and pressure may influence the transition from one phase to the other. This suggests that these polymorphs are well-suited for optical characteristics.
The stable polymorphs including the $3 \mathrm{H}_{\mathrm{b}}-\mathrm{MoSe}_{2}$ polymorph have a small variation in the $\Gamma$ point. The larger Mo atom dominates the higher frequencies (above 8 THz ) and the smaller atom, Se , dominates the lower frequencies in group A , while in $2 \mathrm{H}-\mathrm{MoSe}_{2}$ and $4 \mathrm{~T}-\mathrm{MoSe}_{2}$, the heavier Mo atom dominates the lower frequencies and the Se atom dominates reciprocally. Se atoms dominate the higher frequencies in group B polymorphs, while Mo atoms dominate the lower frequencies.
The stability of polymorphs changes as a result of a decrease in the potential energy near the equilibrium atomic position. All group B polymorphs include soft/negative modes of frequency, showing unstable dynamical properties for $1 \mathrm{~T}_{1^{-}}$ $\mathrm{MoSe}_{2}, 1 \mathrm{~T}_{2}-\mathrm{MoSe}_{2}, 3 \mathrm{~T}-\mathrm{MoSe}_{2}$, and $2 \mathrm{R}_{2}-\mathrm{MoSe}_{2}$ polymorphs. As a result, in nature, these polymorphs are less stable. Figure 7 shows the imaginary phonon dispersion and phonon density of state for 3T-MoSe 2 polymorphs. The other phonon dispersion and phonon density of states for group B are given in Figure S4 of the Supporting Information on Page S6.
2.5. Mechanical Stability. To get a better understanding of the mechanical stability of the $\mathrm{MoSe}_{2}$ polymorph the singlecrystal elastic constant was found. ${ }^{42,43}$ It helps us in finding a certain deformation for the given force. The strain must be applied to support a prescribed deformation. Each stress and strain have three tensile and three shear components. This $6 \times$ 6 symmetric matrix, which comprises 27 independent components, describes the elastic constant of the crystal. The number of components can be automatically reduced by selecting polymorphs with established symmetry. The bulk modulus, Poisson's coefficient, and Lame constant may all be calculated using the stiffness matrix $C_{i j}$. There are six elastic constants for hexagonal and trigonal polymorphs: $C_{11}, C_{12}, C_{13}$, $C_{14}, C_{33}, C_{44}, C_{55}$, and $C_{66}$. Theoretically, only a few polymorphs, such as $1 \mathrm{H}-\mathrm{MoSe}_{2}, 2 \mathrm{H}-\mathrm{MoSe}_{2}$, and $1 \mathrm{~T}-\mathrm{MoSe}_{2}$, are studied in terms of their mechanical properties. Both 2 H $\mathrm{MoSe}_{2}$ and $2 \mathrm{~T}-\mathrm{MoSe}_{2}$ suggest that an elastic constant is more
precisely determined than in earlier studies. ${ }^{39}$ This study for the first time investigated the mechanical stability of several $\mathrm{MoSe}_{2}$ polymorphs.

The stability criteria of elastic constant for hexagonal polymorphs are ${ }^{44}$

$$
\begin{align*}
& B_{\mathrm{H}_{1}}=C_{11}>\left|C_{12}\right|  \tag{1}\\
& B_{\mathrm{H}_{2}}=\left(C_{11}+C_{12}\right) C_{33}>2 C_{13}^{2}  \tag{2}\\
& B_{\mathrm{H}_{3}}=C_{44}>0  \tag{3}\\
& B_{\mathrm{H}_{4}}=C_{66}>0 \tag{4}
\end{align*}
$$

The stability criteria of elastic constant for trigonal polymorphs are ${ }^{44}$

$$
\begin{align*}
& B_{\mathrm{T}_{1}}=C_{11}-C_{12}  \tag{5}\\
& B_{\mathrm{T}_{2}}=\left(C_{11}+C_{12}\right) C_{33}>2 C_{13}^{2}  \tag{6}\\
& B_{\mathrm{T}_{3}}=\left(C_{11}-C_{12}\right) C_{44}>2 C_{14}^{2}  \tag{7}\\
& B_{\mathrm{T}_{4}}=C_{44}>0 \tag{8}
\end{align*}
$$

Except for $3 \mathrm{H}_{\mathrm{a}}-\mathrm{MoSe}_{2}$ and $4 \mathrm{~T}_{1}-\mathrm{MoSe}_{2}$, all polymorphs in group A are mechanically stable and meet the Born stability requirement (Table 2). ${ }^{5}$ In group $A$, the $1 \mathrm{R}_{1}-\mathrm{MoSe}_{2}$ polymorph is mechanically stable but dynamically unstable; hence, it cannot be synthesized in the experiment. The phonon of the $4 \mathrm{~T}-\mathrm{MoSe}_{2}$ and $3 \mathrm{H}_{\mathrm{a}}-\mathrm{MoSe}_{2}$ polymorphs are stable, but due to their unstable mechanical qualities, these polymorphs are categorized as metastable polymorphs. Even though mechanically stable, all of the group B polymorphs are unstable due to phonon instability. Because of their mechanical and dynamic stability, 4 of the 11 polymorphs are considered stable polymorphs. Elastic constants for dynamically and mechanically stable structures are plotted as a graph for a better understanding of mechanical properties (see Figure 8). From the calculation, we found that the $3 \mathrm{H}_{\mathrm{b}}-\mathrm{MoSe}_{2}$ polymorph has the highest $C_{11}$ value, while the $1 \mathrm{H}-\mathrm{MoSe}_{2}$ polymorph has the lowest, which is clearly shown in Figure 8. In all polymorphs, the $C_{11}$ value is larger than the $C_{33}$ value, suggesting that the $x / y$ direction is stiffer than the $z$-direction. $C_{12}$ is greater than $C_{13}$ in all stable hexagonal arrangements. This implies that tension is distributed more along the $x$ - and $z$-axes and less along the $y$-axis. Because of the low $C_{44}$ value, shear deformation is easily accomplished in all stable polymorphs.

The Voigt (V), Reuss (R), and Hill (H) moduli over the elastic stiffness moduli are computed for all of the polymorphs by applying mechanical force. Table 3 shows the Voigt (V), Reuss (R), and Hill (H) moduli over the elastic stiffness moduli of the stable polymorphs. Additionally, averaging the single-crystal elastic constant leads to finding bulk modulus $B$ and shear modulus $G$. ${ }^{46}$

In Voigt approximation, bulk $B$ and shear $G$ can be defined as

$$
\begin{align*}
& B_{\mathrm{V}}=\left(2 C_{11}+2 C_{12}+4 C_{13}+C_{33}\right) / 9  \tag{9}\\
& G_{\mathrm{V}}=\left(7 C_{11}-5 C_{12}-4 C_{13}+2 C_{33}+4 C_{33}\right) / 30 \tag{10}
\end{align*}
$$

And the Reuss approximation of bulk and shear is defined as
Table 2. Calculated Single-Crystal Elastic Constants $C_{i j}$ (in GPa) and Born Criteria for All of the Polymorphs

trigonal

$1 \mathrm{~T}_{2}-\mathrm{MoSe}_{2}$

trigonal
trigonal
웅 \&

$4 \mathrm{~T}-\mathrm{MoSe}_{2} \quad$ 2T-MoSe $2 \quad 2 \mathrm{R}_{1}-\mathrm{MoSe}_{2}$
$2 \mathrm{R}_{1}-\mathrm{MoSe}_{2}$
rhombohedral

rhombohedral
182.81
trigonal
trigonal
106.39
106.39
23.24
0.13
0.07
0.07
0.13
0.003
41.56
$\stackrel{\circ}{n}$
trigonal
trigonal
-26527.6
-26 571.5
12985.6
1298
0.96
0.75
○ す읔$\stackrel{0}{0}$

$1 \mathrm{H}-\mathrm{MoSe}_{2}$
hexagonal

crystal system



Figure 8. Elastic constant values for the mechanically and dynamically stable polymorphs.

$$
\begin{align*}
B_{\mathrm{R}}= & {\left[\left(C_{11}+C_{12}\right) C_{33}-2 C_{12}^{2}\right] /\left(C_{11}+C_{12}+2 C_{33}\right.} \\
& \left.-4 C_{33}\right)  \tag{11}\\
G_{\mathrm{R}}= & (5 / 2)\left\{\left[\left(C_{11}+C_{12}\right) C_{33}-2 C_{12}^{2}\right] C_{55} C_{66}\right\} \\
& /\left\{3 B_{\mathrm{V}} C_{55} C_{66}+\left[\left(C_{11}+C_{12}\right) C_{33}-2 C_{12}^{2}\right] 2\right. \\
& \left.\left(C_{55}+C_{66}\right)\right\} \tag{12}
\end{align*}
$$

The Hill approximation is used widely for the effective result of the bulk modulus (B) and shear modulus ( $G$ ), which can be expressed as

$$
\begin{align*}
& B_{\mathrm{H}}=\left(B_{\mathrm{V}}+B_{\mathrm{R}}\right) / 2  \tag{13}\\
& G_{\mathrm{H}}=\left(G_{\mathrm{V}}+G_{\mathrm{R}}\right) / 2 \tag{14}
\end{align*}
$$

Further, on the basis of the bulk modulus ( $B$ ) and shear modulus ( $G$ ), Pugh ratio ( $G / B$ ), Poisson's ratio ( $\nu$ ), and Young's modulus ( $E$ ) are obtained using the following expression

$$
\begin{align*}
E & =9 B G /(3 B+G)  \tag{15}\\
\nu & =(3 B-2 G) /[2(3 B+G)] \tag{16}
\end{align*}
$$

Table 3 shows the findings of the elastic constant. Consequently, all of the stable polymorphs had $B>G$, showing that mechanical stability is restricted by shear modulus. The bulk modulus (B) and shear modulus ( $G$ ) can be used to predict the hardness of polymorphs. In the current study, the $3 \mathrm{H}_{\mathrm{b}}-\mathrm{MoSe}_{2}$ polymorph has higher bulk modulus and shear modulus values (see Table 3) These results reveal that the $3 \mathrm{H}_{\mathrm{b}}-\mathrm{MoSe}_{2}$ polymorph has higher hardness.

Another significant aspect of mechanical characteristics is the ability to distinguish between ductile and brittle behavior in stable polymorphs. Pugh's ratio (ratio of the shear modulus to the bulk modulus $(G / B)$ ) and Poisson's ratio $(\nu)$ are used to figure out the brittle/ductile behavior of polymorphs. The key value of Pugh's ratio was 0.5 , which allowed us to discriminate between ductile and brittle materials. If the material is more than (less than) 0.5 , it will be brittle (ductile). ${ }^{14,43}$ According to Pugh's ratio, all stable polymorphs have a value greater than 0.5 , suggesting that all polymorphs were brittle.

Table 3. Calculated Bulk Modulus B (in GPa), Shear Modulus G (in GPa), Poisson's Ratio ( $\nu$ ), Young's Modulus E (in GPa), and Pugh Ratio $(G / B)^{a}$

| polymorph | $B_{\mathrm{V}}$ | $B_{\mathrm{R}}$ | $B_{\mathrm{H}}$ | $G_{\mathrm{V}}$ | $G_{\mathrm{R}}$ | $G_{\mathrm{H}}$ | $\nu_{\mathrm{v}}$ | $\nu_{\mathrm{R}}$ | $\nu_{\mathrm{H}}$ | $E_{\mathrm{V}}$ | $E_{\mathrm{R}}$ | $E_{\mathrm{H}}$ | Pugh ratio |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $1 \mathrm{H}-\mathrm{MoSe}_{2}$ | 18.09 | 0.09 | 9.09 | 13.15 | 0.042 | 6.597 | 0.20 | 0.30 | 0.20 | 31.75 | 0.11 | 15.93 | 0.72 |
| $3 \mathrm{H}_{\mathrm{b}}-\mathrm{MoSe}_{2}$ | 53.26 | 18.69 | 35.98 | 38.91 | 14.26 | 26.59 | 0.20 | 0.19 | 0.20 | 93.88 | 34.11 | 64.00 |  |
| $2 \mathrm{H}-\mathrm{MoSe}_{2}$ | 50.07 | 9.66 | 29.86 | 34.15 | 2.95 | 18.55 | 0.22 | 0.36 | 0.24 | 83.48 | 8.04 | 46.12 | 0.63 |
| $2 \mathrm{~T}-\mathrm{MoSe}_{2}$ | 28.89 | 0.25 | 14.57 | 20.95 | 0.007 | 10.48 | 0.20 | 0.48 | 0.21 | 50.62 | 0.02 | 25.36 | 0.71 |

${ }^{a}$ Subscript V shows the Voigt bound, R shows the Reuss bound, and H shows the Hill bound.

Using Poisson's ratio ( $\nu$ ), we can distinguish between brittle and ductile materials. The Poisson's ratio ( $\nu$ ) for ductile materials should be larger than $0.26 .{ }^{43}$ All stable polymorphs are fragile in nature since their $\nu$ values are smaller than $0.26 .{ }^{43}$ Among stable polymorphs, the $2 \mathrm{H}-\mathrm{MoSe}_{2}$ polymorph has a higher Poisson's ratio (0.243). The $1 \mathrm{H}-\mathrm{MoSe}_{2}$ and $3 \mathrm{H}_{\mathrm{b}}-\mathrm{MoSe}_{2}$ Poisson's ratios ( $\nu$ ) are most obvious in the concrete range. The Poisson's ratio $(\nu)$ of the $2 \mathrm{H}-\mathrm{MoSe}_{2}$ polymorph is found in the cast iron range.

The fact that Young's modulus ( $E$ ) has a positive value suggests that the atoms in stable polymorphs are compressible. In this study, Young's modulus $(E)$ is lower for $1 \mathrm{H}-\mathrm{MoSe}_{2}$ and higher for $3 \mathrm{H}_{\mathrm{b}}-\mathrm{MoSe}_{2}$ polymorphs, implying that the atoms in $3 \mathrm{H}_{\mathrm{b}}-\mathrm{MoSe}_{2}$ polymorphs are more compressible than those in other polymorphs. The elastic stiffness moduli, Poisson's ratio $(\nu)$, Young's modulus ( $E$ ), and Pugh's ratio of unstable polymorphs are given in Table S3 in the Supporting Information on Page S6
2.6. Anisotropic. Elastic anisotropic are investigated for stable polymorphs. To understand the elastic anisotropic, shear anisotropic $\left(A_{\mathrm{G}}\right)$, anisotropic compressibility $\left(A_{\mathrm{B}}\right)$, and universal anisotropic ( $A^{\mathrm{u}}$ ) (see Table 4) are calculated for the mechanically and dynamically stable polymorphs. ${ }^{47}$

Table 4. Calculated Shear Anisotropic $A_{G}$, Anisotropic Compressibility $A_{\mathrm{B}}$, and Universal Anisotropic $A^{\mathrm{U}}$ for the Stable Polymorphs

| polymorphs | $A_{\mathrm{G}}$ | $A_{\mathrm{B}}$ | $A^{\mathrm{U}}$ |
| :--- | :---: | ---: | :--- |
| $1 \mathrm{H}-\mathrm{MoSe}_{2}$ | 1354.6 | 1882.23 | $\infty$ |
| $2 \mathrm{H}-\mathrm{MoSe}_{2}$ | 50.22 | 37.00 | 56.94 |
| $2 \mathrm{~T}-\mathrm{MoSe}_{2}$ | 1400.75 | 1049.92 | $\infty$ |
| $3 \mathrm{H}_{\mathrm{b}}-\mathrm{MoSe}_{2}$ | 8.679 | 13.72 | 10.490 |

The elastic anisotropic for compressibility and shear is expressed as

$$
\begin{align*}
& A_{\mathrm{B}}=\left(B_{\mathrm{V}}-B_{\mathrm{R}}\right) /\left(B_{\mathrm{V}}+B_{\mathrm{R}}\right)  \tag{17}\\
& A_{\mathrm{G}}=\left(G_{\mathrm{V}}-G_{\mathrm{R}}\right) /\left(G_{\mathrm{V}}+G_{\mathrm{R}}\right) \tag{18}
\end{align*}
$$

And universal anisotropic can be expressed as

$$
\begin{equation*}
A^{\mathrm{U}}=5 \frac{G_{\mathrm{V}}}{G_{\mathrm{R}}}+\frac{B_{\mathrm{V}}}{B_{\mathrm{R}}}-6 \tag{19}
\end{equation*}
$$

For isotropic materials, the value of $A^{\mathrm{U}}$ is zero, but a high value of $A^{\mathrm{U}}$ shows the presence of elastic anisotropy. The physical quantities and orientation of Young's modulus ( $E$ ) and Poisson's ratio ( $\nu$ ) can be used to show that polymorphs have isotropic characteristics. Young's modulus $(E)$ determines the polymorph's orientation, which is derived using the given elastic compliance constants. ${ }^{46}$ Young's modulus (E) surface should be perfectly spherical for isotropic materials. Figure 9 shows a three-dimensional (3D) plot of Young's modulus (E)
for dynamically stable polymorphs. Young's modulus $(E)$ is the highest for $3 \mathrm{H}_{\mathrm{b}}-\mathrm{MoSe}_{2}$, and the lowest Young's modulus $(E)$ is obtained for $1 \mathrm{H}-\mathrm{MoSe}_{2}$. ${ }^{43,47}$
2.7. Thermodynamical Properties. The effect of phonon on dynamically as well as mechanically stable structures has been examined through thermodynamic behavior ( $1 \mathrm{H}-\mathrm{MoSe}_{2}$, $2 \mathrm{H}-\mathrm{MoSe}_{2}, 3 \mathrm{H}_{\mathrm{b}}-\mathrm{MoSe}_{2}$, and $2 \mathrm{~T}-\mathrm{MoSe}_{2}$ ). For the stable polymorphs, temperature-dependent thermodynamic functions such as specific heat at constant volume " $C_{\mathrm{v}}$ ", entropy " $S$ ", internal energy " $E$ ", and vibrational free energy " $F$ " is computed. ${ }^{32}$ Figure 10 demonstrates how vibrational energy increases and free energy decreases exponentially, following Debye's law. Compared to the other stable polymorphs, the $2 \mathrm{H}-\mathrm{MoSe}_{2}$ polymorph shows high vibrational energy, and the free energy is high for the $2 \mathrm{H}-\mathrm{MoSe}_{2}$ polymorph. At extremely low temperatures, entropy stays constant for all polymorphs, and at an absolute zero, it becomes zero. ${ }^{46}$ At $1000 \mathrm{~K}, 2 \mathrm{~T}$ $\mathrm{MoSe}_{2}, 3 \mathrm{H}_{\mathrm{b}}-\mathrm{MoSe}_{2}$, and $1 \mathrm{H}-\mathrm{MoSe}_{2}$ polymorphs obtained the constant value $170 \mathrm{~J} \mathrm{~K}^{-1} \mathrm{~mol}^{-1}$, but $1 \mathrm{H}-\mathrm{MoSe}_{2}$ polymorph showed $140 \mathrm{~J} \mathrm{~K}^{-1} \mathrm{~mol}^{-1}$ of energy as a function of temperature. All of the stable polymorphs follow the third rule of thermodynamics by increasing entropy as the temperature rises.

At constant volume, specific heat $C_{\mathrm{v}}$ increases linearly with temperature, implying that all polymorphs follow Debye's $\mathrm{T}^{3}$ rule for constant volume and the conventional Dulong-Petit law for elevated temperatures. $1 \mathrm{H}-\mathrm{MoSe}_{2}, 2 \mathrm{~T}-\mathrm{MoSe}_{2}$, and $3 \mathrm{H}_{\mathrm{b}}$ $\mathrm{MoSe}_{2}$ have the same $C_{\mathrm{v}}{ }^{39}$ Our data for various temperatures obeys the two important laws of thermodynamics, implying that all examined polymorphs have thermodynamic stability even for greater pressure ranges. Although there have not been any findings, either theoretical or experimental, it is difficult to compare the outcomes.
2.8. IR and Raman Spectra. 2.8.1. IR Spectra. IR spectra are studied for the stable polymorphs, and the corresponding modes of representation are evaluated in this paper. ${ }^{46}$ Because of the $\mathrm{Se}-\mathrm{Mo}-\mathrm{Se}$ vibrations, modes of vibrations are prominent in high-frequency regions and some modes are found in low frequencies regions because of $\mathrm{Mo}-$ Se vibration (see Table 5). ${ }^{43}$ Surprisingly, all of the polymorphs are symmetric to the principal axis, and it is double degenerate, which is two-dimensional irreducible representations. Specifically, $1 \mathrm{H}-\mathrm{MoSe}_{2}$ polymorphs are antisymmetric for the reflection into the horizontal plane, and it shows $\mathrm{A}^{\prime \prime}{ }_{2}$ and $\mathrm{E}^{\prime}$ modes, which confirms that it is a single-layer material. From the crystal symmetric $2 \mathrm{H}-\mathrm{MoSe}_{2}, 3 \mathrm{H}_{\mathrm{b}}-\mathrm{MoSe}_{2}$ polymorphs displace in the bulk material modes $\mathrm{A}_{2 \mathrm{u}}$ and $\mathrm{E}_{1 \mathrm{u}} .2 \mathrm{~T}-\mathrm{MoSe}_{2}$ is active in $\mathrm{A}_{2 \mathrm{u}}$ and $\mathrm{E}_{\mathrm{u}}$ modes, which shows a double layer. Not to be surprised, $2 \mathrm{H}-\mathrm{MoSe}_{2}$ and $3 \mathrm{H}_{\mathrm{b}}-\mathrm{MoSe}_{2}$ have the same IR active modes, which show the same symmetric operators. Compared to the other polymorphs, $1 \mathrm{H}-\mathrm{MoSe}_{2}$ projects high frequency, as well as $2 \mathrm{~T}-\mathrm{MoSe}_{2}$ from Figure 11 shows a considerable number of IR active modes.


Figure 9. 3D-plot of Young's modulus (E) for stable polymorphs: (a) $1 \mathrm{H}-\mathrm{MoSe}_{2}$, (b) $2 \mathrm{H}-\mathrm{MoSe}_{2}$, (c) $2 \mathrm{~T}-\mathrm{MoSe}_{2}$, and (d) $3 \mathrm{H}_{\mathrm{b}}-\mathrm{MoSe}_{2}$.
2.8.2. Raman Spectra. Studied polymorphs show the signature Raman active modes, as shown in Figure 11. In our study, we noted that out-of-plane $\mathrm{A}_{1 \mathrm{~g}}$ mode dominates in $3 \mathrm{H}_{\mathrm{b}}-\mathrm{MoSe}_{2}$ and in $2 \mathrm{H}-\mathrm{MoSe}_{2}$ polymorphs, which show single degenerate wave functions. ${ }^{48,49}$ While the $2 \mathrm{~T}-\mathrm{MoSe}_{2}$ polymorph is dominated by the in-plane $\mathrm{E}_{\mathrm{g}}$ mode. We see that modes of polymorphs are red-shifted from approximately 40 $\mathrm{cm}^{-1}$ when compared to the modes of $1 \mathrm{H}-\mathrm{MoSe}_{2}$. The observed red shift is caused by larger interlayer distances, which lead to an increase in the dielectric screening of the long-range Coulomb forces and thus overall restoring force gets reduced on the atom. $2 \mathrm{H}-\mathrm{MoSe}_{2}$ and $3 \mathrm{H}_{\mathrm{b}}-\mathrm{MoSe}_{2}$ polymorphs in group A display Raman-active modes $\mathrm{E}_{1 \mathrm{~g}}$ and $\mathrm{A}_{1 \mathrm{~g}}$, as shown in Figure 11b. The polymorph $2 \mathrm{H}-\mathrm{MoSe}_{2}$ is double degenerate, indicating that it is bulk material. 2T$\mathrm{MoSe}_{2}$ polymorphs show many Raman-active modes and the highest mode of peak (Figure 11) compared to other polymorphs. ${ }^{49}$ We noted that Raman's active mode of the $2 \mathrm{H}-\mathrm{MoSe}_{2}$ polymorph is the same as the earlier reported value. But for the remaining polymorphs, there is still a lack of other theoretical IR studies in the literature on these polymorphs. This makes it difficult to verify this result due to a lack of literature data.

## 3. CONCLUSIONS

Foremost 11 different $\mathrm{MoSe}_{2}$ polymorphs are put forward and studied using total-energy calculations, band structure analysis, phonon density of states, and elastic constants calculations in DFT. Our detailed study shows that polymorphs in group A have minimum energy, compared to group B polymorphs. The minimum energy of group A polymorphs is very close,
although with a varying range of volume. Polymorphs in group A are semiconductors with direct and indirect band gaps. $1 \mathrm{H}-$ $\mathrm{MoSe}_{2}$ and $3 \mathrm{H}_{\mathrm{a}}-\mathrm{MoSe}_{2}$ in group A show a direct band gap at 2 eV , and the remaining polymorphs in group A show an indirect band gap within the range of $1.6-1.8 \mathrm{eV}$. All polymorphs in group B are dynamically unstable. In group A, $1 \mathrm{H}-\mathrm{MoSe}_{2}, 2 \mathrm{H}-$ $\mathrm{MoSe}_{2}, 2 \mathrm{~T}-\mathrm{MoSe}_{2}$, and $3 \mathrm{H}_{\mathrm{b}}-\mathrm{MoSe}_{2}$ polymorphs are mechanically, dynamically, and thermodynamically stable. The metastable state is depicted for the $4 \mathrm{~T}-\mathrm{MoSe}_{2}$ and $3 \mathrm{H}_{\mathrm{a}}-$ $\mathrm{MoSe}_{2}$ polymorphs because of their unstable mechanical properties and stable phonon properties. When compared to other polymorphs, the $3 \mathrm{H}_{\mathrm{b}}-\mathrm{MoSe}_{2}$ polymorph in particular exhibits greater hardness. The thermal efficiency was highest for the $2 \mathrm{H}-\mathrm{MoSe}_{2}$ polymorph. It is concluded that four of the 11 polymorphs in group A will adhere to the stable criterion since they are simple to synthesize and suitable for viable applications like photocatalytic and photovoltaic.

## 4. METHODOLOGY

The VASP code is enforced for all calculations within the periodic density functional theory. ${ }^{20,50}$ The projector-augmented wave (PAW) method is used to describe the interaction of core and valence electrons. ${ }^{51-53}$ Initially, the structure of all of the polymorphs is optimized with the help of the Perdew-Burke-Ernzerhof (PBE) exchange-correlation functional. ${ }^{54}$ The DFT/vdw-df2 method is used to obtain the PBE-level optimized structure. The energy-volume curve was generated for the optimized structures to find their lowest energy. Only for the large e-cut, parameters of the structure can predict reliability, so we used a 550 eV energy cutoff. The screened hybrid function was used to find the electronic


Figure 10. Temperature as a function of specific heat at (a) constant volume " $C_{\mathrm{v}}$ ", (b) entropy " $S$ ", (c) internal energy " $E$ ", and (d) vibrational energy " $F$ " for dynamically stable polymorphs.

Table 5. Raman Active Modes and IR Active Modes for the Dynamically Stable Polymorphs

| polymorph | Raman active mode $\left(\mathrm{cm}^{-1}\right)$ | IR active mode $\left(\mathrm{cm}^{-1}\right)$ |
| :---: | :---: | :---: |
| $1 \mathrm{H}^{-M o S e_{2}}$ | $\mathrm{E}^{\prime}: 285$ | $\mathrm{E}^{\prime}: 285$ |
|  | $\mathrm{E}^{\prime \prime}: 167$ | $\mathrm{~A}^{\prime \prime}{ }_{2}: 350$ |
|  | $\mathrm{~A}_{1}^{\prime}: 240$ |  |
| $2 \mathrm{H}^{2}-\mathrm{MoSe}_{2}$ | ${ }^{2} \mathrm{E}_{2 \mathrm{~g}}: 28,381$ | $\mathrm{~A}_{2 \mathrm{u}}: 460$ |
|  | ${ }^{2} \mathrm{E}_{\mathrm{lg}}: 282$ | $\mathrm{E}_{\mathrm{lu}}: 380$ |
|  | ${ }^{1} \mathrm{~A}_{\mathrm{lg}}: 404$ |  |
| $3 \mathrm{H}_{\mathrm{b}}-\mathrm{MoSe}_{2}$ | ${ }^{2} \mathrm{E}_{2 \mathrm{~g}}: 36,379$ | $\mathrm{~A}_{2 \mathrm{u}}: 458$ |
|  | ${ }^{2} \mathrm{E}_{\mathrm{lg}}: 284$ | $\mathrm{E}_{\mathrm{lu}}: 380$ |
|  | $\mathrm{~A}_{\mathrm{lg}}: 404$ |  |
| $2 \mathrm{~T}^{2}-\mathrm{MoSe}_{2}$ | ${ }^{2} \mathrm{E}_{\mathrm{g}}: 26,284,381$ | ${ }^{2} \mathrm{E}_{\mathrm{u}}: 283,382$ |
|  | ${ }^{2} \mathrm{~A}_{\mathrm{lg}}: 41,403,464$ | ${ }^{2} \mathrm{~A}_{2 \mathrm{u}}: 401,463$ |

properties of polymorphs that are optimized at the PBE level; the screened hybrid function was proposed by Heyd, Scuseria, and Ernzerhof (HSE06). ${ }^{55,56}$ For the structural optimization and the electronic polymorph studies, we have used a Monkhorst-Pack $2 \times 2 \times 2$ as $k$-mesh. Bands of the polymorphs are computed by solving the periodic KohnSham equation on $10 k$-points along each direction of high symmetry of the irreducible part of the first Brillouin zone. Charge density, charge transfer, and electron localization
function (ELF) analyses were performed using the CASTEP code, and this helped to understand the bonding nature and interaction between the $\mathrm{MoSe}_{2}$ polymorphs. PHONOPY software is used to calculate phonon dispersion and phonon density of state for suitable supercell mode performed for the supercells of the polymorphs. ${ }^{39}$ The force constant on the supercell is calculated with the help of the VASP code. ${ }^{51,53,57}$ Every atom in the binary system is displaced by applying a finite displacement of $0.007 \AA$ in the $x, y$, and $z$ directions to get the matrices to form the force constant. After obtaining the force constant, we construct a dynamical matrix for different q vectors in the Brillouin zone. The dynamical matrices are solved to get the result of eigenvalues of phonon frequency and eigenvectors of phonon mode. Suitable supercell mode and Monkhorst-Pack grid is given in Table S4 of the Supporting Information on Page S7. The dynamical stability of all polymorphs is checked by remarking imaginary and real modes of polymorphs. Thermal properties are obtained for the studied polymorphs including heat capacity, free energy, and entropy of the system. ${ }^{39}$ In this present work, the mechanical stability of all polymorphs is understood by computing singlecrystal elastic constants. Each crystal system has applied a set of strains ( $-0.015,-0.010,-0.005,0.000,0.005,0.010$, and 0.015 ), and the stress tensor is calculated. VASPKIT is used to


Figure 11. (a) IR intensity as a function of wavenumber and (b) Raman intensity as a function of wavenumber for dynamically stable polymorphs.
evaluate the elastic constants by linear fitting of the stressstrain curve. ${ }^{50}$ The CASTEP package is used to obtain the Raman and IR spectra for all of the polymorphs of $\mathrm{MoSe}_{2} \cdot{ }^{49}$ We used an optimized structure for the CASTEP computational code to get an accurate result. ${ }^{58}$

## - ASSOCIATED CONTENT

## (5) Supporting Information

The Supporting Information is available free of charge at https://pubs.acs.org/doi/10.1021/acsomega.2c08217.

Minimum energy; formation energy of all of the polymorphs; electronic structure; mechanical property data in detail; phonon dispersion relation and band structure of polymorphs; and $k$-grid and supercell size of $\mathrm{MoSe}_{2}$ polymorphs (PDF)

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## Notes

The authors declare no competing financial interest.

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After this paper was published ASAP April 5, 2023, a minor correction was made to the title. The corrected version was reposted April 18, 2023.

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