A high resolution tidal model for the area around The Lofoten Islands, Northern Norway

H. Moe, A. Ommundsen, and B. Gjevik *
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Abstract

A numerical model with grid resolution 500 m has been used to simulate tides around The Lofoten Islands in northern Norway. The model spans more than 3° latitude and covers a sea area of approximately 1.2 · 10⁵ km². The fine spatial resolution resolves the important fine scale features of the bottom topography on the shelf and the complex coastline with fjords and islands. Boundary conditions at the oceanic sides of the model domain are obtained by interpolation from a large scale tidal model covering the Nordic Seas. The semi-diurnal components M_2 , S_2 and N_2 and the diurnal component K_1 are simulated. Harmonic constants for sea level are compared with observations from 21 stations. The best fit is found for the M_2 component with a standard deviation between the observed and modelled amplitude and phase of respectively 2.3 cm and 2.5 degrees. The standard deviation for the other smaller components ranges 1.5-2.8 cm and 5.3-16.7 degrees. Current fields from the model are compared with observations in four locations; the Moskenes sound, the Gimsøy channel, the Tjeldsund channel and the Sortland channel. Current speed is found to be in good agreement with observations. In the Sortland channel the model predicts a dominant diurnal K_1 current in agreement with observations.

1 Introduction

In the Vestfjorden area inside The Lofoten Islands in northern Norway the Arcto-Norwegian cod stock spawns from February to March. Here rich fisheries of great economic importance have taken place since early medieval times. In the 13th. century trading of cod products from Lofoten consolidated the influence and power of the Hanseatic League. The fact that oceanographic elements to a large extent determine the environment for cod spawning and development of eggs and larvae in the Vestfjorden area was realized early, (Eggvin 1932;1934; Sverdrup 1952). Since then there have been several studies of the hydrography and the general circulation in the area. The effect of atmospheric forcing was investigated by Furnes and Sundby (1981). McClimans and Nilsen (1991) studied the circulation by a laboratory model. An extensive NATO field measurement campaign, Rocky Water, has also been conducted (Jenserud 1995;1996) accompanied by data analysis and model simulations (Melsom 1997).

^{*}Department of Mathematics, University of Oslo, P.O. Box 1053, 0316 Blindern, Oslo, Norway

Although the tides represent an important part of the current variability in the area, no systematic study of the dynamics of the tides has been reported. Results from coarser grid modelling of tides on the Norwegian continental shelf can be found in Gjevik et al. (1990), Gjevik (1990) and some results of the high resolution model for the main semi-diurnal component M_2 have been published by Gjevik et al. (1997).

Outside The Lofoten Islands the main semi-diurnal tide is basically a northward propagating wave modified by the topography of the shelf and the coastline. The narrowing of the shelf from a relatively broad shelf south of Lofoten to a narrow shelf on the northern side of the islands and the deflection of the flow due to the island chain itself lead to strong cross-shelf tidal currents near The Lofoten Point (Lofotodden). This local topographic enhancement of the current may play an important role in the transport of eggs and larvae from Vestfjorden to the outer shelf where they are carried northward by the prevailing shelf edge current (Ådlandsvik and Sundby 1994; Ommundsen 1999).

In the Moskenes sound, between The Lofoten Point and the island Mosken, a particular strong tidal current, Moskstraumen, runs with speed up to 5 m/s (Norwegian Hydrographic Service 1986a). Also in the sounds between the islands east of Lofotodden there are strong tidal currents especially in Nappstraumen and Gimsøystraumen. Rumors of the strength and power of Moskstraumen inspired the authors Edgar Allen Poe and Jules Verne to fantasy descriptions of a Maelstrom whirlpool. Historic accounts of the Lofoten Maelstrom can be found in Gjevik et al. (1997) and Gjevik (1998). The fine structure of the current in the area has also been revealed by ERS-1 SAR (Wahl 1995; Dokken and Wahl 1995) and by SST signals from AVHRR imagery (Mitchelson-Jacob 1995). High resolution SAR images also show that wind waves and swell in the area around The Lofoten Point are strongly modified by depth and current refraction (Krogstad, private communication 1999; Neef 1999).

This paper gives a comprehensive presentation and documentation of the results obtained with a high resolution tidal model for the area. The model span more than 3° latitude and covers a sea area of approximately $1.2 \cdot 10^{5}$ km² (figure 1). With a spatial resolution of 500 m the model resolves both important fine scale features of the bottom topography on the shelf and the complex coastline with fjords and islands (figure 2). This enables a study of the transition of the tide from basically a northward progressive wave on the shelf to standing oscillations in the fjord basins, and the enhancement of the tidal current in the Moskenes sound and other major currents in the area.

High resolution tidal modelling for shelf and coastal areas with complex bathymetry and coastline is a challenging and rapidly developing subject. A review of the state of the art is given by Davies et al. (1997a;1997b). In particular the treatment of strong non-linear effects such as turbulence, flow separation and eddy formation is a difficult task which requires special precautions (Geyer 1993; Maddock and Pingree 1978). Although this model study aims specifically towards an understanding of the dynamics of the tides in the Lofoten area many of the problems accounted here are of wider interest.

A similar high resolution model, as used in this study, has recently been developed for the the coast of Møre and Trøndelag, Mid Norway (Moe et al. 2000).

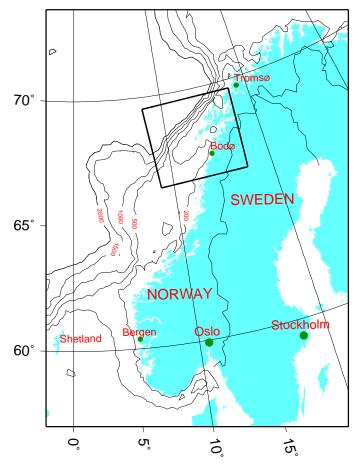


Figure 1: Map of Norwegian continental shelf with depth contours (meter) and model domain (rectangular box).

2 Model Equations

The depth integrated shallow water equations are formulated in flux form in a Cartesian coordinate system (x, y, z) with the x and y axis in the horizontal plane and the z axis vertical:

$$\frac{\partial U}{\partial t} + \frac{\partial}{\partial x} \left(\frac{U^2}{H}\right) + \frac{\partial}{\partial y} \left(\frac{UV}{H}\right) - fV = -gH \frac{\partial \eta}{\partial x} - c_D \frac{\sqrt{U^2 + V^2}}{H} \frac{U}{H} + B_x \tag{1}$$

$$\frac{\partial V}{\partial t} + \frac{\partial}{\partial x} \left(\frac{UV}{H}\right) + \frac{\partial}{\partial y} \left(\frac{V^2}{H}\right) + fU = -gH\frac{\partial \eta}{\partial y} - c_D \frac{\sqrt{U^2 + V^2}}{H} \frac{V}{H} + B_y \tag{2}$$

where (U, V) are the components of volume flux vector per unit length in the horizontal plane, η the vertical displacement of the sea surface from the mean sea level, $H = H_0 + \eta$ the total depth, H_0 the mean depth, g acceleration of gravity, f the Coriolis parameter, c_D the drag coefficient of the quadratic bottom shear stress, and (B_x, B_y) the components of the horizontal shear stress. In addition the continuity equation reads:

$$\frac{\partial \eta}{\partial t} = -\frac{\partial U}{\partial x} - \frac{\partial V}{\partial y} \tag{3}$$

The depth mean current velocity is defined by

$$\overline{u} = \frac{U}{H}, \quad \overline{v} = \frac{V}{H}$$

In this model domain the direct effect of the tide generating forces is negligible, and the tidal motion is mainly driven by the boundary input i.e. sea surface elevation and volume fluxes. In the present problem these equations span a wide parameter range from weak tidal flows on the deeper part of the shelf to strong tidal currents near The Lofoten Islands. We introduce a velocity scale u_s , a time scale t_s corresponding to half the tidal period, a tidal amplitude a, a length scale for the spatial variation of the tidal flow l_s and a depth scale h_s . With this scaling we can define the tidal excursion $l_t = u_s t_s$ and the equations (1)-(2) can be recast into dimensionless form:

$$\frac{\partial U}{\partial t} + \alpha \left[\frac{\partial}{\partial x} \left(\frac{U^2}{H}\right) + \frac{\partial}{\partial y} \left(\frac{UV}{H}\right)\right] - \delta V = -\beta H \frac{\partial \eta}{\partial x} - \gamma \frac{\sqrt{U^2 + V^2}}{H} \frac{U}{H}$$
(4)

$$\frac{\partial V}{\partial t} + \alpha \left[\frac{\partial}{\partial x} \left(\frac{UV}{H}\right) + \frac{\partial}{\partial y} \left(\frac{V^2}{H}\right)\right] + \delta U = -\beta H \frac{\partial \eta}{\partial y} - \gamma \frac{\sqrt{U^2 + V^2}}{H} \frac{V}{H}$$
 (5)

with $B_x = B_y = 0$. The dimensionless form of the continuity equation reads:

$$\frac{\epsilon}{\alpha} \frac{\partial \eta}{\partial t} = -\frac{\partial U}{\partial x} - \frac{\partial V}{\partial y} \tag{6}$$

with $H = H_0 + \epsilon \eta$. The same symbols are here tacitly used for the dimensionless variables U, V, H and η as in the dimensional equations (1)-(3). The dimensionless parameters are defined by:

$$\alpha = \frac{l_t}{l_s}, \quad \beta = \frac{ga}{u_s^2} \frac{l_t}{l_s}, \quad \gamma = \frac{c_D l_t}{h_s}, \quad \delta = f t_s, \quad \epsilon = \frac{a}{h_s}$$
 (7)

Here α , and ϵ are measures of the importance of the convective terms and the non-linear surface elevation terms respectively. The parameters β , γ , and δ scale pressure, bottom friction and rotational effects respectively. In deep water α , ϵ and $\gamma \ll 1$ and the equations reduces to the linearized shallow water equation with negligible bottom friction. Near the coast, with strong tidal currents, α , β , γ are of O(1) and all terms in the equation of motion have to be retained. In not too shallow water $\epsilon \ll 1$ the left hand side of equation (3) may be neglected rendering a nearly non-divergent volume flux as long as α is of O(1).

In this paper we have tested the performance of a linear tidal model and made the approximations $\alpha = \epsilon = 0$ and ϵ/α of O(1). The equations are then discretized on a C-grid (Mesinger and Arakawa 1976) with a semi-implicit numerical scheme. This scheme is widely used for depth integrated ocean models. A discussion of its dispersion and stability properties is given e.g. by Martinsen et al. (1979) and Gjevik and Straume (1989). The stability criteria expressed by the numerical time step Δt is:

$$\Delta t \le \frac{\Delta x}{2\sqrt{2gH_{max}}}$$

where Δx is the grid size and H_{max} is the maximum depth in the model domain.

3 Model set up and boundary conditions

The depth matrix was evaluated on an UTM coordinate grid with $\Delta x = 0.5$ km resolution. Near the coast average depths for each grid box were read from Norwegian coastal charts most of them with scale 1 : 50000. Outside the zone covered by the coastal charts depths are from a bathymetric data base with 500 m spatial resolution provided by the Norwegian Hydrographic Service (NHS) or interpolated from a 4 × 4 km digital data base. The main part of the model domain is covered by the UTM zone 33W, which we for convenience have extended west of 12°E into UTM zone 32W. The resulting depth matrix of 810×725 grid points is depicted in figure 2. The Lofoten Islands stretch in northeastern direction from Røst towards Lødingen (map code 5, table 1). North of The Lofoten Islands, Vesterålen is located between Stokmarknes and Andenes. The wide fjord south of the Lofoten chain of islands, from Røst and Bodø eastward to Lødingen, is Vestfjorden. The general topography with a relatively wide shelf south of Lofoten and a narrow shelf west of Vesterålen and Andenes is clearly revealed by this map.

Boundary conditions for the model were obtained by interpolating surface elevation and volume fluxes from a large scale model of the Norwegian and the Barents Sea with 25 km grid resolution (Gjevik et al. 1990;1994). The interior solution was adjusted to the specified boundary conditions with the flow relaxation scheme (FRS), Martinsen and Engedahl (1987). The FRS softens the transition from an exterior solution (here the interpolated data) to an interior solution (model area) by use of a grid zone where the two solutions dominate at each ends respectively. The width of the FRS zone is here taken to be ten grid cells.

Two types of boundary forcing (exterior solutions) has been tested; i) only surface elevation specified and ii) both surface and and volume fluxes specified. Single or selected combinations of the tidal components M_2 , S_2 , N_2 and K_1 are used in the conditions i) and ii). The total simulation times are 85 hours when only semi-diurnal components are included and 96 hours if the diurnal component is present. At t=0 the boundary forcing is applied from rest at the oceanic sides of the model domain and the amplitudes grow according to $(1 - \exp(-\sigma t))$. We have used $\sigma = 4.6 \cdot 10^{-5} \text{ s}^{-1}$ which implies full effect of boundary conditions after about 12 hours.

The simulations are started from rest i.e. the internal solution $U = V = \eta = 0$. When the simulation has reached 72 hours full fields (all grid points) for current and elevation are stored with half an hour sampling. Time series recorded from t=0 at 45 stations within the model domain are examined to ensure that a steady state oscillation is reached. The surface elevation attained steady state rapidly in all stations, but for some stations time series for currents included noise due to the transient start. Longer simulations have been performed but for the results presented in this report 72 hours was sufficient to reach an acceptable steady state. Harmonic analysis is then performed on the full fields to determine the amplitude and phase for the appropriate tidal component. The simulations have normally been performed with a bottom friction coefficient of $c_D = 0.003$, but simulations are also done with $c_D = 0$ in order to investigate the effect of bottom friction. Generally, without bottom friction the simulations will need longer time to reach an acceptable steady state and bottom friction seems to be of minor importance regarding the modelled sea level. If not explicitly mentioned the results presented are from simulations with bottom friction included, single component forcing and boundary condition i).

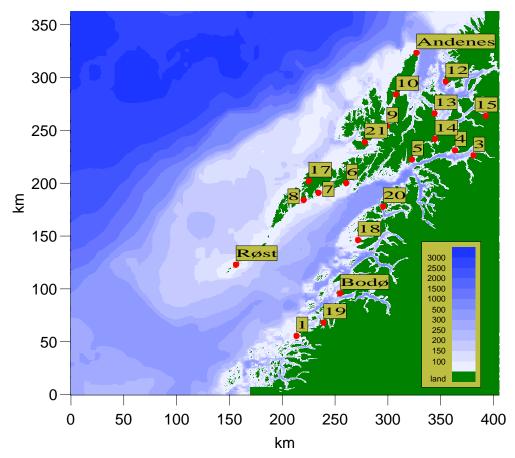


Figure 2: Model domain with 0.5 km grid resolution. Color depth-scale in meters. The position of the tidal stations, table 1, are marked with (red) dots and appropriate map codes.

4 Results

The calculated harmonic constants for sea level amplitude, h_n , and phase relative Greenwich, g_n , are compared with observations from 21 stations (table 1 and figure 2). For Bodø, Narvik, Lødingen, Kabelvåg, Risøyhamna, Andenes, Harstad and Evenskjær (primary stations) the harmonic constants are evaluated from long time series of observed sea level (Norwegian Hydrographic Service 1998). For the other stations in table 1 (secondary stations) harmonic constants are calculated from shorter time series, typically 2-4 weeks. NHS has given us access to this data set, which previously has not been used for validation of tidal models. For the secondary stations NHS has also calculated correction factors for amplitude and time of high and low water relative to nearest primary station. By using these correction factors we have also deduced a set of derived harmonic constants for the secondary stations. Harmonic constants are listed in the tables 2-5 for both primary and secondary stations.

Current fields from the model are compared with observations in four locations: the Moskenes sound, the Gimsøy channel, the Tjeldsund channel and the Sortland channel. NHS has provided measurements of the tidal current in the areas around Gimsøy (G1-G2) and Sortland (S1-S5) and the University of Bergen the data for the stations in The Moskenes sound (L1-L4), figure 11 section 4.2. Where measurements from several depths were available we used the mean value for comparison with model current data from the nearest grid point.

Table 1: List of tidal stations.

Station	Coordinates	Map Code
Støtt	$66^{\circ}55'N, 13^{\circ}27'E$	1
Bodø	$67^{\circ}17'N, 14^{\circ}23'E$	Bod ø (2)
Narvik	$68^{\circ}26'N, 17^{\circ}25'E$	3
Bogen	$68^{\circ}29'N, 17^{\circ}00'E$	4
Lødingen	$68^{\circ}25'N, 16^{\circ}00'E$	5
Kabelvåg	$68^{\circ}13'N, 14^{\circ}30'E$	6
Stamsund	$68^{\circ}08'N, 13^{\circ}52'E$	7
Ballstad	$68^{\circ}04'N, 13^{\circ}32'E$	8
Sortland	$68^{\circ}42'N, 15^{\circ}26'E$	9
Risøyhamna	$68^{\circ}58'N, 15^{\circ}39'E$	10
Andenes	$69^{\circ}19'N, 16^{\circ}09'E$	Andenes(11)
Skrolsvik	$69^{\circ}04'N, 16^{\circ}50'E$	12
Harstad	$68^{\circ}48'N, 16^{\circ}33'E$	13
Evenskjær	$68^{\circ}35'N, 16^{\circ}33'E$	14
Røkenes	$68^{\circ}46'N, 17^{\circ}45'E$	15
Røst	$67^{\circ}30'N, 12^{\circ}04'E$	Røst(16)
Tangstad	$68^{\circ}13'N, 13^{\circ}38'E$	17
Helnessund	$67^{\circ}44'N, 14^{\circ}46'E$	18
Inndyr	$67^{\circ}02'N, 14^{\circ}02'E$	19
Skutvik	$68^{\circ}01'N, 15^{\circ}20'E$	20
Stokmarknes	$68^{\circ}33'N, 14^{\circ}54'E$	21

4.1 Sea level, semi-diurnal and diurnal components

4.1.1 The M_2 component

Contour lines for the M_2 sea level amplitude and phase are depicted in figure 3. The phase lines are approximately perpendicular to the shelf slope with gradually increasing phases north-east ward, showing that the M_2 wave component propagates basically in a north-easterly direction. Separation between phase lines are also larger north of The Lofoten Islands, where the shelf is narrow, which imply a larger propagation speed than south of Lofoten where the shelf is wider.

The 60 cm amplitude isoline follows the shelf slope and relatively low amplitudes are found in Vesterålen north of The Lofoten Islands where the shelf is narrow. South of Lofoten there is almost a linear increase in amplitude from the shelf edge towards the coast. The convergence of contour lines for the amplitude at Røst and The Lofoten Point is due to the scattering of the northward propagating wave by the Lofoten chain of islands. Due to the constraints of the coast line there is also an increase in amplitude by about 24 cm from the mouth of Vestfjorden near Røst eastward towards Narvik (map code 3) at the head of the fjord. Across the Lofoten chain of islands there is a difference in amplitude of 15-30 cm which drives the strong tidal currents in the channels between the islands. The general variation in amplitude and phase seen here is also reproduced to a large extend by an idealized model with a corresponding transition from a broad

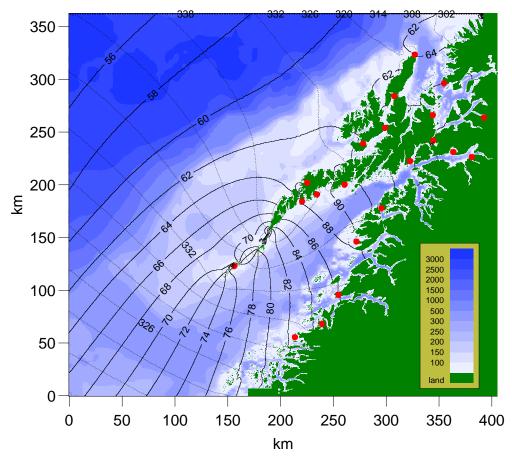


Figure 3: M_2 sea surface elevation. Isolines for amplitude (solid lines, 2-cm separation) and phase (broken lines, 2-degree separation). Tidal stations (table 1) marked by (red) dots. Shading shows depth with scale in legend (meter). Boundary forcing: only surface elevation.

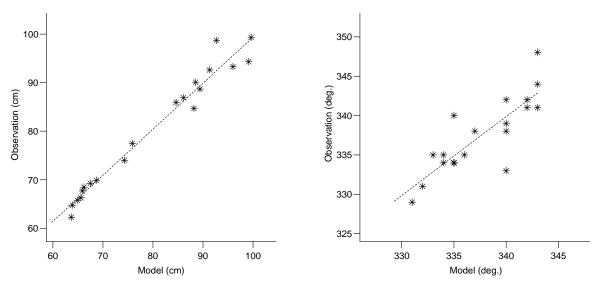


Figure 4: Scattering diagrams M_2 . Comparison between modelled and observed amplitude (left panel) and phase (right panel). The least squares regression line (dashed). The standard deviation estimate between model and observation is 2.29 cm (amplitude) and 2.54 degrees (phase). Boundary forcing: only surface elevation.

to a narrow shelf (Ommundsen and Gjevik 2000).

By comparing amplitudes and phases with observations, table 2 and figure 4, the best fit is found for the run with prescribed surface elevation at the open boundaries with a standard deviation of only 2.3 cm for amplitude and 2.5 degrees for phase. To obtain this good agreement we have made minor adjustments of the surface elevation at the open boundaries. This indicates that further improvements can be made by using more advanced optimization techniques, e.g. Lardner (1993). For the run with surface elevation and fluxes prescribed at the open boundaries the corresponding standard deviations are 3.8 cm and 5.9 degrees.

Table 2: Observed and modelled amplitude $(h_n \text{ cm})$ and phase $(g_n \text{ degree}, \text{GMT})$ of the M_2 tide. Model results with prescribed elevation at the open boundaries (*Elevation*) and elevation and fluxes at the open boundaries (*Elev.* & flux).

	Obse	rved	Der	ived	Mo	Model		del	
Station					Eleve	ation	Elev. & flux		
	h_n	${g}_n$	h_n	${g}_n$	h_n	${g}_n$	h_n	g_n	
Støtt			86.0	326	82.5	329	84.8	324	
Bodø	86.9	331			86.1	332	88.5	327	
Narvik	99.3	334			99.6	335	102.2	330	
Bogen	94.3	340	99.1	343	99.1	335	101.7	330	
Lødingen	93.3	334			96.0	335	98.6	330	
Kabelvåg	92.6	334			91.3	335	93.8	330	
Stamsund	88.7	335	91.2	336	89.4	336	91.9	331	
Ballstad	84.7	338	87.8	335	88.2	337	90.7	332	
Sortland	66.3	342	66.9	337	65.6	340	69.3	335	
Risøyhamna	67.7	342			65.9	342	70.3	336	
Andenes	64.8	341			63.9	342	69.2	336	
Skrolsvik	68.5	341	67.1	344	66.2	343	71.7	337	
Harstad	69.3	344			67.5	343	73.2	336	
Evenskjær	74.0	333			74.3	340	79.7	334	
Røkenes	69.9	348	64.6	348	68.7	343	74.4	337	
Røst	77.5	334		332	75.9	334	78.1	329	
Tangstad	62.3	339	65.2	336	63.7	340	66.7	334	
Helnessund	90.1	335			88.5	333	91.0	328	
Inndyr	85.9	329			84.6	331	87.0	325	
Skutvik	98.7	335		_	92.7	334	95.3	329	
Stokmarknes	65.8	338		339	64.9	340	68.4	335	

4.1.2 The S_2 component

The amplitude of the S_2 component is about one third of the M_2 and the general features of the variation of the amplitude and phase are similar (figure 5). The standard deviations between modelled and observed amplitude and phase are 2.8 cm and 5.3 degrees respectively for the S_2 simulations with surface elevation prescribed at the open boundary, table 3 and figure 6.

Table 3: Observed and modelled amplitude $(h_n \text{ cm})$ and phase $(g_n \text{ degree}, \text{GMT})$ of the S_2 tide. Model results with prescribed elevation at the open boundaries (*Elevation*).

	Obset	rved	Derived		Model	
Station					Eleva	tion
	h_n	${g}_n$	h_n	g_n	h_n	${g}_n$
Støtt			29.7	4	27.2	3
Bodø	30.5	9			28.5	6
Narvik	35.3	13			33.1	10
Bogen	38.2	21	34.8	21	32.9	10
Lødingen	32.2	11			31.8	10
Kabelvåg	32.6	13			30.2	10
Stamsund	32.3	12	32.0	14	29.6	11
Ballstad	35.2	15	30.8	13	29.1	11
Sortland	24.4	21	23.5	16	23.0	17
Risøyhamna	21.1	22			23.2	18
Andenes	22.0	20			22.5	18
Skrolsvik	23.2	21	22.1	24	23.3	20
Harstad	23.8	23			23.8	18
Evenskjær	26.1	11			26.2	15
Røkenes	22.1	16	21.3	29	24.3	19
Røst	27.6	13		10	25.2	9
Tangstad	24.8	18	22.9	14	22.2	16
Helnessund	32.5	15			29.2	8
Inndyr	30.2	8			27.9	5
Skutvik	36.3	24			30.7	9
Stokmarknes	22.1	15		18	22.9	17

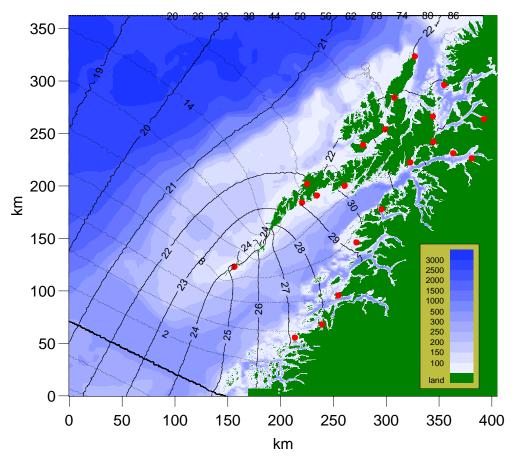


Figure 5: S_2 sea surface elevation. Isolines for amplitude (solid lines, 1-cm separation) and phase (broken lines, 2-degree separation). Tidal stations (table 1) marked by (red) dots. Shading shows depth with scale in legend (meter).

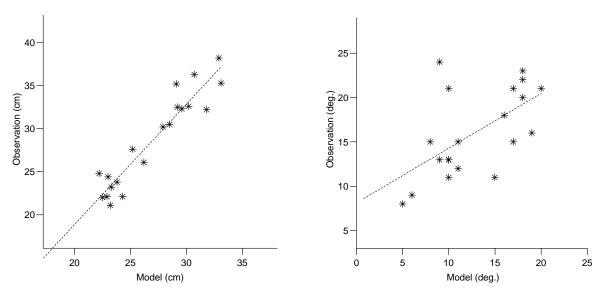


Figure 6: Scattering diagrams S_2 . Comparison between modelled and observed amplitude (left panel) and phase (right panel). The least squares regression line (dashed). The standard deviation estimate between model and observation is 2.8 cm (amplitude) and 5.3 degrees (phase).

4.1.3 The N_2 component

The amplitude of the N_2 component is about one fifth of the M_2 and the general features of the variation of the amplitude and phase are similar (figure 7). The standard deviations between modelled and observed amplitude and phase are 1.5 cm and 9.5 degrees respectively for the N_2 simulations with surface elevation prescribed at the open boundary, table 4 and figure 8.

Table 4: Observed and modelled amplitude $(h_n \text{ cm})$ and phase $(g_n \text{ degree}, \text{GMT})$ of the N_2 tide. Model results with prescribed elevation at the open boundaries (*Elevation*).

	Obse	rved	Derived		Model	
Station					Eleve	ition
	h_n	${g}_n$	h_n	${g}_n$	h_n	${g}_n$
Støtt			17.5	303	17.5	310
Bodø	17.7	307			18.3	313
Narvik	20.3	311			21.1	316
Bogen			20.2	318	21.0	316
Lødingen	20.3	314			20.4	316
Kabelvåg	18.9	311			19.4	317
Stamsund			18.6	311	19.0	317
Ballstad			17.9	310	18.8	318
Sortland	12.7	343	13.6	313	15.4	321
Risøyhamna	16.9	326			15.4	323
Andenes	13.2	317			15.1	323
Skrolsvik	14.3	315	13.6	321	15.6	324
Harstad	14.2	320			15.9	323
Evenskjær	15.1	310			17.3	321
Røkenes			13.1	325	16.2	324
Røst	16.2	310		308	16.3	315
Tangstad			13.3	311	14.8	320
Helnessund	17.7	315			18.8	314
Inndyr	17.6	304			17.9	312
Skutvik					19.7	316
Stokmarknes	12.6	339		315	15.1	321

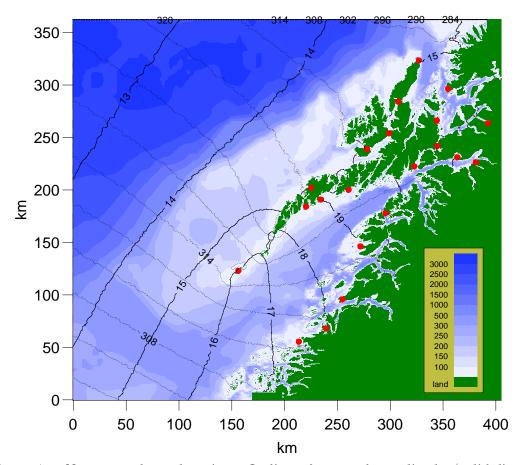


Figure 7: N_2 sea surface elevation. Isolines for equal amplitude (solid lines, 1-cm separation) and phase (broken lines, 2-degree separation). Tidal stations (table 1) marked by (red) dots. Shading shows depth with scale in legend (meter).

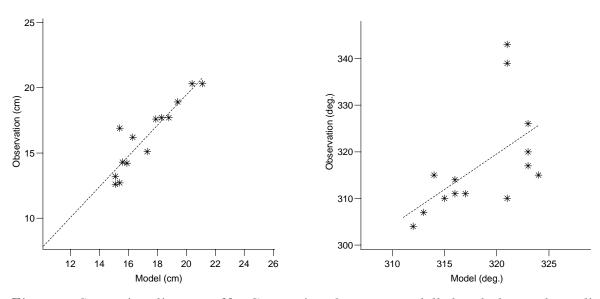


Figure 8: Scattering diagrams N_2 . Comparison between modelled and observed amplitude (left panel) and phase (right panel). The least squares regression line (dashed). The standard deviation estimate between model and observation is 1.5 cm (amplitude) and 9.5 degrees (phase).

4.1.4 The K_1 component

The amplitude of sea surface displacement for the largest diurnal component (K_1) is about one tenth to M_2 . The contour lines for amplitude and phase (figure 9) show an interesting picture with small local maxima in amplitude along the shelf slope particularly north of The Lofoten Islands where the shelf is narrow. The separation between these maxima is 25-75 km indicating that the diurnal tide in the area has the structure of shelf waves with short wave length.

A study of the propagation of diurnal tides by use of a model with idealized bottom topography in form of a transition from a broad to a narrow shelf shows the occurrence of shelf waves with short wave length on the narrow section of the shelf (Ommundsen and Gjevik 2000). Calculation of dispersion properties also show that the narrow shelf north of Lofoten will support shelf wave modes with diurnal period and wave lengths in the range 50-100 km.

The regression analysis between observed and modelled amplitude and phase shows a relatively large scatter particularly for phase (figure 10). Standard deviation is 2.5 cm for amplitude and 16.7 degrees for phase. Clearly a more optimal set of boundary conditions is required in order to reproduce the observed amplitude and phase for K_1 with a higher degree of accuracy.

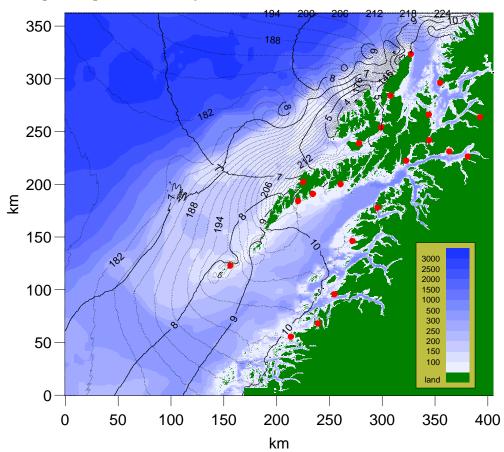


Figure 9: K_1 sea surface elevation. Isolines for amplitude (solid lines, 1-cm separation) and phase (broken lines, 2-degree separation). Tidal stations (table 1) marked by (red) dots. Shading shows depth with scale in legend (meter).

Table 5: Observed and modelled amplitude $(h_n \text{ cm})$ and phase $(g_n \text{ degree}, \text{GMT})$ of the K_1 tide. Model results with prescribed elevation at the open boundaries (*Elevation*).

	Obs	erved	Der	ived	Model		
Station					Elevation		
	h_n	g_n	h_n	g_n	h_n	g_n	
Støtt			8.0	177	10.3	192	
Bodø	10.3	194			10.1	195	
Narvik	11.2	197			10.4	197	
Bogen	12.5	197.3	11.7	200	10.4	197	
Lødingen	10.2	197			10.3	197	
Kabelvåg	10.9	195			10.2	198	
Stamsund	12.0	194	10.8	196	10.2	197	
Ballstad	8.8	190	10.4	196	10.3	198	
Sortland	6.7	237	7.9	197	4.5	195	
Risøyhamna	3.2	213			5.9	157	
Andenes	5.3	184			10.4	178	
Skrolsvik	6.8	186	5.7	200	10.4	180	
Harstad	5.9	197			10.5	180	
Evenskjær	6.5	192			10.6	184	
Røkenes	7.4	181	5.5	202	10.5	180	
Røst	9.3	193		194	8.5	194	
Tangstad	9.3	221	7.7	196	7.1	215	
Helnessund	11.4	195			10.1	196	
Inndyr	8.4	190			10.1	194	
Skutvik	10.3	187			10.3	197	
Stokmarknes	7.5	221		198	5.2	215	

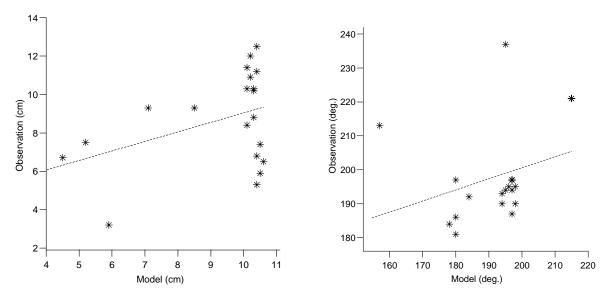


Figure 10: Scattering diagrams K_1 . Comparison between modelled and observed amplitude (left panel) and phase (right panel). The least squares regression line (dashed). The standard deviation estimate between model and observation is 2.5 cm (amplitude) and 16.7 degrees (phase).

4.2 Tidal currents

4.2.1 The Moskenes sound

The Moskenes sound, with the small island Mosken in the middle, is located between Værøy (V) and The Lofoten Point (L), figure 12. Here runs the famous Lofoten Maelstrom known worldwide for its strength and for the mystics which surrounds it (Gjevik et al. 1997; Gjevik 1998). This strong current combined with the background current in the region is an effective mechanism in the transport of eggs, larvae etc. out of Vestfjorden (Ådlandsvik and Sundby 1994; Ommundsen 1999).

In figure 12 the modelled M_2 current is depicted by its peak values and by the current ellipses. The maximum current is close to 200 cm/s. Four stations L1-L4, with measurements of the tidal current, are plotted in figure 11 and the observed and modelled parameters of the current ellipse are compared in table 6. The observations are in good agreement with the results of our model. For station L2 the model predicts clockwise rotation while observations show counterclockwise rotation. However it should be noted that L2 is located close the borderline (figure 12) between areas of opposite rotation.

In figure 13 the current fields at the time of peak M_2 outgoing and incoming volume flux are depicted. Based on the calculated volume flux for M_2 , through a cross-section area of $3.1 \cdot 10^5$ m² between (V) and (L), the model predicts a mean maximum current of 116 cm/s for the cross-section. Peak outgoing volume flux occurs about two hours after local high water in agreement with observations.

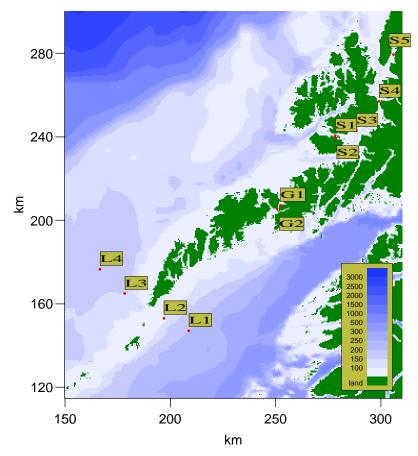


Figure 11: Location and map code for stations with measurements of tidal current. The Moskenes sound (L1-L4), the Gimsøy channel (G1-G2) and the Sortland channel (S1-S5).

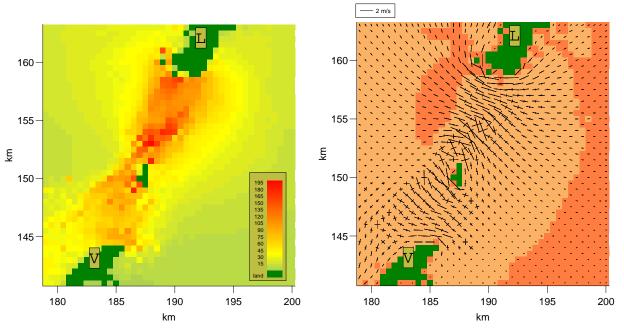


Figure 12: Left panel: Maximum M_2 current (major half axis) in the area between The Lofoten Point (L) and Værøy (V). Color scale in cm/s, legend. Right panel: Tidal ellipse and rotation of the M_2 current vector. Bright shadowing clockwise rotation, darker shadowing counterclockwise. The crosses show the major and minor axes.

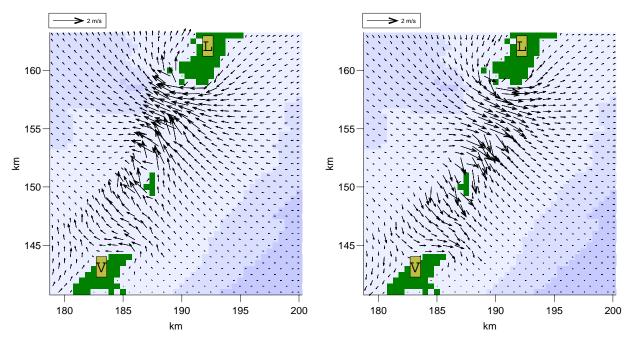


Figure 13: Left panel: M_2 current field at the time of peak outgoing volume flux between Værøy and The Lofoten Point. Right panel: M_2 current field at the time of peak incoming volume flux.

Table 6: Parameters for the M_2 current ellipse. A (cm/s), major half axis; B (cm/s), minor half axis; θ (deg.), orientation of major axis in degrees true; Rot., rotation direction for the current vector (+, clockwise; -, counterclockwise).

Station	Observed				Model			
(map code)	Α	В	θ	Rot.	A	В	θ	Rot.
L1	9.6	3.1	64	-	8.1	1.9	69	-
L2	21.2	1.2	291	-	22.0	1.8	277	+
L3	11.6	4.5	112	+	15.2	2.0	155	+
L4	7.3	1.7	355	+	9.0	1.0	344	+

4.2.2 The Tjeldsund channel

The Tjeldsund channel is a busy sailing route for north and south going sea traffic along the coast. For safety reasons it is important to know the current well in this area. Sandtorgstraumen, the main channel north-east of Tjeldøya, is the strongest current (coordinate (343,240), figure 14). In figure 14 the modelled current is depicted by its peak values and by the current ellipses. A complex pattern is visible in the rotation of the current vector, with local strong currents in Sandtorgstraumen, Balstadstraumen (north of Tjeldøya) and Steinslandstraumen (coordinate (346,249), figure 14)

According the pilot book, Norwegian Hydrographic Service (1986b), a maximum northward current in Sandtorgstraumen occurs approximately at high water running with a maximum speed of 206 cm/s at spring. Based on the calculated volume flux for M_2 the model predicts a maximum northward current, running with 168 cm/s, approximately one hour after high water (figure 16). Correspondingly the combined

effect of M_2 and S_2 is found to be 228 cm/s and $M_2 + S_2 + N_2 + K_1$ gives 314 cm/s. Figure 15 shows the current field at the time of peak M_2 volume flux in northward and southward direction respectively.

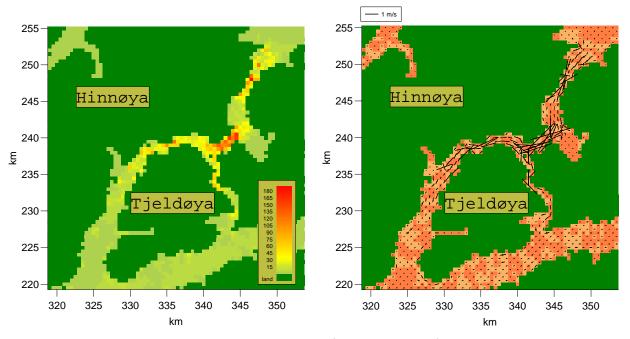


Figure 14: Left panel: Maximum M_2 current (major half axis) in the Tjelsund channel. Color scale in cm/s, legend. Right panel: Tidal ellipse and rotation of the M_2 current vector. Bright shadowing clockwise rotation, darker shadowing counterclockwise. The crosses show the major and minor axes.

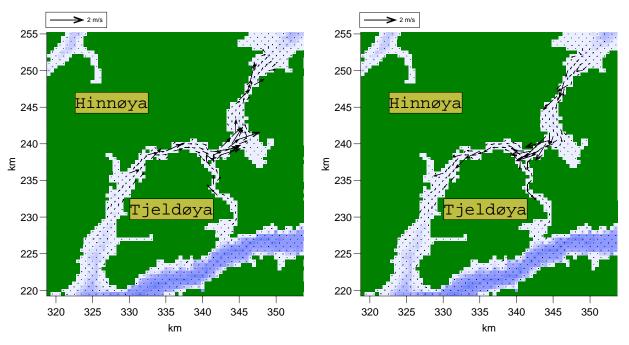


Figure 15: Left panel: Current field at the time of peak M_2 volume flux in northward direction in Sandorgstraumen between coordinates (342,241) and (345,237). Right panel: Current field at the time of peak M_2 volume flux in southward direction.

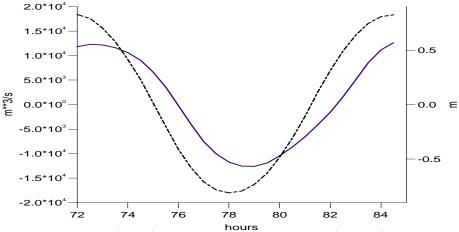


Figure 16: Volume flux (solid) and sea surface elevation (dotted) in Sandtorgstraumen, cross-section between coordinates (342,241) and (345,237). The total area of this cross-section is 7500 m² leading to a mean peak northward current of 168 cm/s.

4.2.3 The Sortland channel

Sortlandsundet is the name of the narrow channel between Sortland and Hinnøya, figure 17. Measurements by NHS show that the current field in Sortlandsundet is characterized by a strong K_1 component. At the station S4, located in Sortlandsundet, the K_1 major half axis was measured to 48.5 cm/s more than three times the M_2 major half axis (13.0 cm/s), table 7. The latter normally dominates along the Norwegian coast. The modelled current is depicted by its peak values and current ellipses for respectively the M_2 and K_1 components in figures 17 and 19. Five stations S1-S5, with measurements of the tidal current, are plotted in figure 11 and ellipse parameters for M_2 and K_1 (station S4) are listed in table 7. Observed and modelled current speed is in good agreement for all stations except S2, and captures the dominant K_1 component in station S4.

In figures 18 and 20 the current field at the time of peak northward and southward volume flux are shown for M_2 and K_1 respectively. The peak volume fluxes for the two components are 2888 m³/s and 12546 m³/s respectively. With a cross-section area of $26 \cdot 10^4$ m² for Sortlandsundet the corresponding peak mean current is 11 cm/s and 48 cm/s, which agrees well with observations.

A plot of the ratio between the major axis for K_1 and M_2 (figure 21) reveals a dominant diurnal current component on a wide area of the shelf north of Lofoten. In some cases for e.g. north of Vestvågøy the M_2 current is very small leading to a large ratio although K_1 is not particularly large. The situation in Sortlandsundet seems to be unique since both the M_2 and K_1 component are relatively large. The large diurnal current in the area is clearly an effect of transformation of the diurnal tide into shelf waves along the narrow shelf north-west of Lofoten (section 4.1.4).

Lønseth and Schjølberg (1993) report a dominant diurnal current component near the shelf edge in Vesterålen (station water depth 450 m) approximately located in map coordinate (222,288). Measured mean values for instrument depths less than 300 m for the major half axes for M_2 and K_1 are 1.0 cm/s and 2.0 cm/s respectively. The modelled values for the major axes for M_2 and K_1 in this location are 1.1 cm/s and 5.5 cm/s respectively.

Table 7: Parameters for the M_2 and K_1 (station S4) current ellipse. A (cm/s), major half axis; B (cm/s), minor half axis; θ (deg.), orientation of major axis in degrees true; Rot., rotation direction for the current vector (+, clockwise; -, counterclockwise).

Station		Observed				Model			
(map code)	A	В	θ	Rot.	A	В	θ	Rot.	
S1	9.8	0.2	85	-	7.3	0.1	99	+	
S2	26.9	0.4	25	+	9.9	0.1	316	+	
S3	1.7	0.1	53	-	1.8	0.0	45	+	
S4	13.0	0.3	10	-	10.2	0.9	2	-	
S5	3.5	0.2	198	-	8.5	0.5	194	+	
$S4(K_1)$	48.5	0.3	8	-	45.6	3.8	359	-	

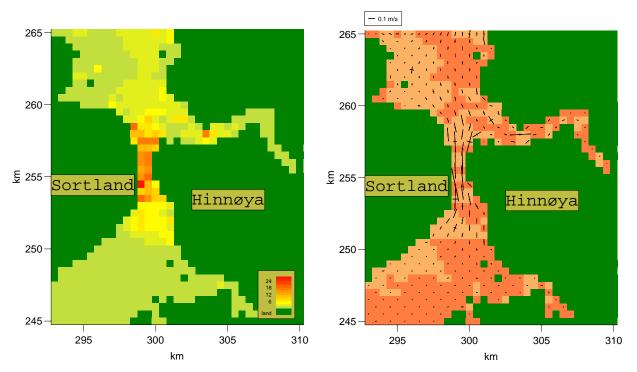


Figure 17: Left panel: Maximum M_2 current (major half axis) in Sortlandsundet between Sortland and Hinnøya. Color scale in cm/s, legend. Right panel: Tidal ellipse and rotation of the M_2 current vector. Bright shadowing clockwise rotation, darker shadowing counterclockwise. The crosses show the major and minor axes.

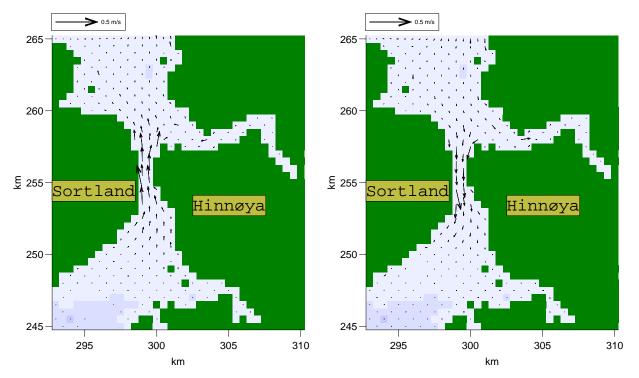


Figure 18: Left panel: Current field at the time of peak M_2 volume flux in northward direction in Sortlandsundet between coordinates (297,254) and (302,254). Right panel: Current field at the time of peak M_2 volume flux in southward direction.

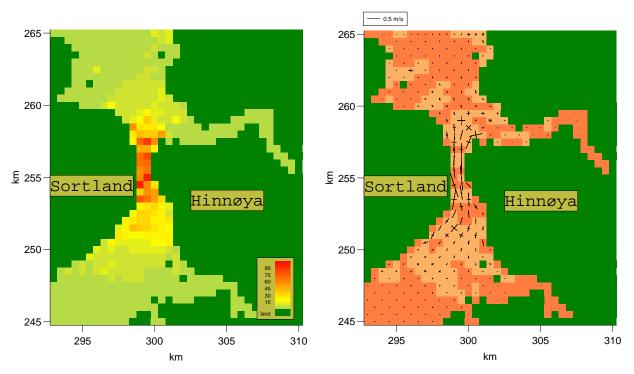


Figure 19: Left panel: Maximum K_1 current (major half axis) in Sortlandsundet. Color scale in cm/s, legend. Right panel: The rotation of the K_1 current vector. Bright shadowing depicts region with clockwise rotation, darker shadowing counterclockwise rotation. The crosses show the major and minor axes.

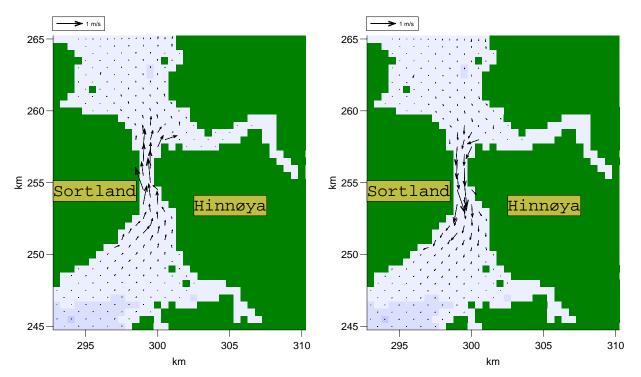


Figure 20: Left panel: Current field at the time of peak K_1 volume flux in Sortland-sundet between coordinates (297,254) and (302,254). Right panel: Current field at the time of peak K_1 volume flux in southward direction.

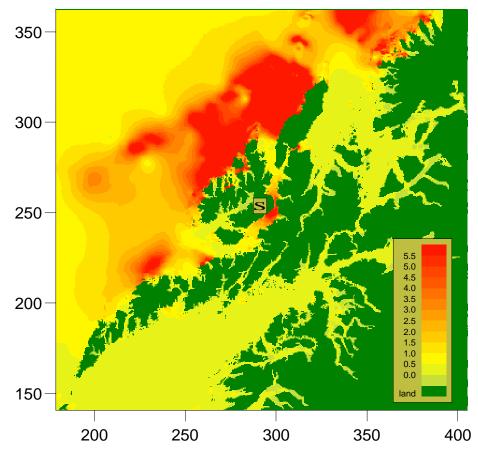


Figure 21: The ratio between the major axes of the current ellipses for the K_1 and M_2 components. Sortlandsundet (S) in the center. Color scale in legend.

4.2.4 The Gimsøy channel

The Gimsøy channel is located between the Lofoten islands Vestvågøy and Austvågøy with the island Gimsøy in the middle. A strong current, Gimsøystraumen, runs in the narrows between Gimsøy and Austvågøy and another current, Sundklakkstraumen, in the narrow channel between Gimsøy and Vestvågøy.

In figure 22 the modelled current is depicted by its peak values and by the current ellipses. A complex pattern is visible in the rotation of the current vector, with strong currents in Sundklakkstraumen and Gimsøystraumen. The two available stations with current measurements, G1 and G2 (table 8 and figure 11), are located in Gimsøystraumen. The model results shown in table 8 are comparable to the observed, but with a 500 m grid resolution in the narrow channel representative grid positions for the stations are difficult to obtain. We have used data from the nearest grid point with approximately the same depth as in the measurement station.

The pilot book, Norwegian Hydrographic Service (1986a), predicts maximum northward current in Gimsøystraumen approximately one hour after high water running with a speed of 231 cm/s at spring. Based on the calculated volume flux for M_2 the model predicts a maximum northward current in Gimsøystraumen of 115 cm/s (figure 24) approximately one hour after high water. Correspondingly the combined effect of M_2 and S_2 is 158 cm/s while $M_2 + S_2 + N_2 + K_1$ gives 233 cm/s. Figure 23 shows the current field at the time of peak M_2 volume flux in northward and southward direction.

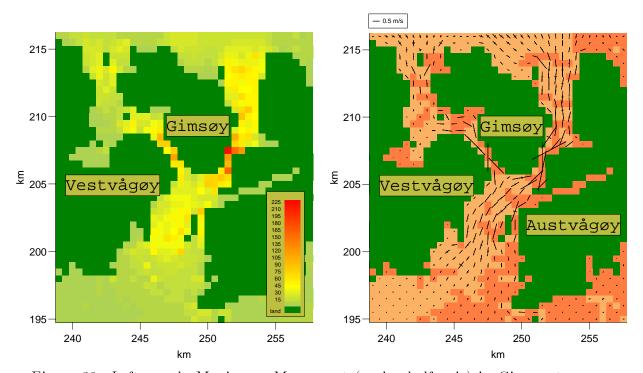


Figure 22: Left panel: Maximum M_2 current (major half axis) in Gimsøystraumen. Color scale in cm/s, legend. Right panel: Tidal ellipse and rotation of the M_2 current vector. Bright shadowing clockwise rotation, darker shadowing counterclockwise. The crosses show the major and minor axes.

Table 8: Parameters for the M_2 current ellipse. A (cm/s), major half axis; B (cm/s), minor half axis; θ (deg.), orientation of major axis in degrees true; Rot., rotation direction for the current vector (+, clockwise; -, counterclockwise).

Station	Observed					Mod	del	
(map code)	Α	В	θ	Rot.	A	В	θ	Rot.
G1	83.3	1.2	216	-	118.0	0.0	0	non
G2	113.9	12.6	41	-	71.0	3.0	68	-

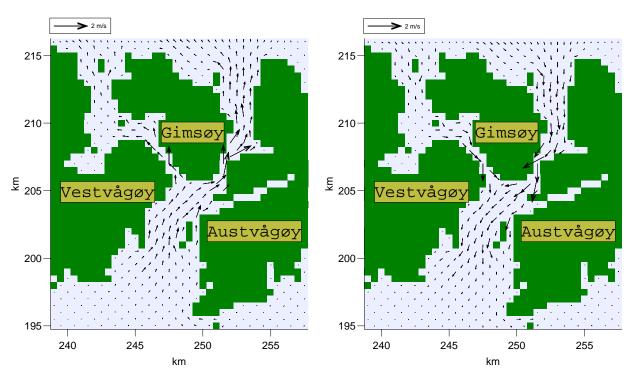


Figure 23: Left panel: Current field at the time of peak M_2 volume flux in northward direction in broad channel between coordinates (245,203) and (252,203). Right panel: Current field at the time of peak M_2 volume flux in southward direction.

The modelled maximum M_2 current is in fair agreement with observations from stations G1 and G2, table 8. Based on the calculated volume flux in Sundklakkstraumen between coordinates (245,207) and (250,207), a slightly slower M_2 mean current of 1.0 m/s is found.

The major axis of the M_4 component (period 6.2 hours), which is due to nonlinear interaction, is measured to be 13.6 cm/s at 5 meter depth at station G1. In our model with only nonlinear bottom friction terms included, a smaller M_4 current of about 4 cm/s is found in the same location. This indicates that nonlinear advection terms are of importance in this region.

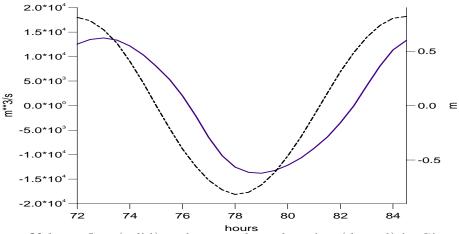


Figure 24: Volume flux (solid) and sea surface elevation (dotted) in Gimsøystraumen, cross-section between coordinates (250,207) and (253,207). The area of this cross-section is 12000 m^2 leading to a mean peak northward current of 115 cm/s

4.2.5 Visual observation of current shift

During the period 12-14 July 1996 one of the authors (Gjevik) observed visually the shift in direction of the tidal current in Gimsøystraumen and Sundklakkstraumen, (see section 4.2.4). He also made similar observations in two other channels, Nappstraumen and Sundstraumen, further west in Lofoten. The time of the current shift, i.e slack water, were estimated following the drift of markers (sea weed, jellyfish etc.) floating in the surface. In Gimsøystraumen and Sundklakkstraumen the bridges across provided convenient platforms for the observations. The drift of the markers could not be estimated well unless the current was above a certain level. The fact that the current did not turn simultaneously across the channel made it difficult to estimate the exact time of the turning. In most cases it was only possible to determine the time of turning within an interval of 30-60 minutes for slack water. The observations are compared with the predicted time of current shift in the channels from a model simulation including all four components M_2 , S_2 , N_2 , and K_1 (table 9). In view of the relatively large uncertainty in the observational data the agreement with model prediction is good.

Table 9: Observed and modelled time (UTC) for slack water 12–14 July 1996

	12 July		13 Ju	ly	14 Ju	14 July		
Location	Mod	Obs	Mod	Obs	Mod	Obs		
	Time Dir.	Time	Time Dir.	Time	Time Dir.	Time		
Gimsøystraumen	1330 NE→SW	1300-1400	0845 SW→NE	0805-0835				
(226, 206)	1945 SW→NE	1910-1930						
Sundklakkstraumen	1230 N→S	1200-1300	$0745 \text{ S} \rightarrow \text{N}$	0725 - 0850				
(247, 207)	1900 S→N	1930-1925						
Nappstraumen			$1445~{ m NE}{ ightarrow}{ m SW}$	1430-1445				
(218, 194)			$2045~\mathrm{SW}{ ightarrow}\mathrm{NE}$	2000-2125				
Sundstraumen					1345 NW→SE	1240-1320		
(205, 182)					1945 SE→NW	-2100		

5 Concluding remarks

The high resolution depth integrated model is found to reveal important features of the dynamics of the tides around The Lofoten Islands. Due to the bottom topography of the shelf and the geometry of the coastline a characteristic variation in tidal amplitude is found with relatively larger amplitudes south of the islands than north of the islands where the shelf is narrow. This large scale variation in sea level amplitude and phase for the three semi-diurnal constituents M_2 , S_2 , and N_2 is in good agreement with observations. For the main diurnal component (K_1) , with sea level amplitude of about one tenth of the dominant semi-diurnal component (M_2) , the difference between model and observation is larger. The simulations show that the diurnal tide transform into shelf wave modes on the narrow shelf north of The Lofoten Islands leading to a dominance of the diurnal current component in this area of the shelf and in some channels along the coast. This surprising result is also confirmed by measurements. Although the agreement between model and observation are generally very good we have seen systematic deviations, specially for the diurnal component, which can be improved with the use of optimization techniques.

The success of the model in predicting the speed and the time of shift of the current in main channels between The Lofoten Islands show that the local tidal conditions are to a large extent determined by the large scale dynamics of the tide in deep water where non-linear effects are negligible. In order to simulate the current field in channels with strong tidal current turbulence, flow separation and eddy formation need to be represented in a more realistic way in the model. This will require use of adaptive grid or nesting of finer grid models in certain areas. Also, particularly at certain times of the year, density stratifications may have a considerable effect on the tidal current and need therefore to be incorporated in the model in order to provide accurate prediction of currents.

Despite these limitations the results of the simulations with this barotropic tidal model stand by their own right and could serve as a starting point for more advanced modelling exercises and as a guidance for future measurement programs.

Acknowledgements

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